

7210/A21

OCTOBER 2008

DISCRETE MATHEMATICS

Time : Three hours

Maximum : 100 marks

PART A — (6 × 5 = 30 marks)

Answer any SIX questions.

1. Write the properties of a relation.
2. Show that $f(x, y) = x^y$ is a primitive recursive function.
3. What is the disjunctive normal form of $p \vee (p \wedge q)$?
4. Symbolise "X is the father of the mother of Y".
5. Write any two applications of recurrence relations.
6. Write the algorithm for solving Non-homogeneous finite order linear relation.
7. Define Rooted binary tree, spanning tree, weighted graph.
8. Write PRIM'S algorithm

BCA II year



PART C — (2 × 15 = 30 marks)

Answer any TWO questions.

17. (a) Explain Warshall's algorithm.
 (b) Explain all the four normal forms with examples.
18. (a) Solve $S(k) + 5S(k-1) = 9, S(0) = 6$ in all categories.
 (b) Explain travelling salesmen problem.
19. Construct the logic circuit for

$$f(x_1, x_2, x_3) = [(x_1 \wedge x_2) \vee x_3] \wedge [(x_2 \vee x_3) \vee x_3]$$

9. Explain duality in lattices with example.
10. Write a short note on boolean functions.

PART B — (4 × 10 = 40 marks)

Answer any FOUR questions.

11. Let $R = \{(1, 2), (3, 4), (2, 2)\}$ and $S = \{(4, 2), (2, 5), (3, 1), (1, 3)\}$ find

RoS, SoR, RoR, SoS, RoSoR.

12. Show that $P \rightarrow (Q \rightarrow R) \Leftrightarrow P \rightarrow (\neg Q \vee R) \Leftrightarrow (P \wedge Q) \rightarrow R$ without using truth table.
13. Show that $(\exists x) m(x)$ follows logically from the premises $(x)[H(x) \rightarrow M(x)]$ and $(\exists x)H(x)$.
14. Solve the recurrence relation $a(n) = a(n-1) + 2(n-1), a(1) = 2$.
15. Prove that a graph is a tree iff it is minimally connected.
16. State and prove distributive inequalities of a lattice.