



1

#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

### GS-2012 (Physics)

#### TATA INSTITUTE OF FUNDAMENTAL RESEARCH

Written Test in **PHYSICS** - December 9, 2012

Duration: Three hours (3 hours)

Name:	Ref. Code:
	·

#### Please read all instructions carefully before you attempt the questions.

- 1. Please fill-in details about name, reference code etc. on the question paper and answer sheet. The Answer Sheet is machine-readable. Read the instructions given on the reverse of the answer sheet before you start filling it up. Use only HB pencils to fill-in the answer sheet.
- 2. Indicate your ANSWER ON THE ANSWER SHEET by blackening the appropriate circle for each question. *Do not mark more than one circle for any question*: this will be treated as a wrong answer.
- 3. This test comes in two sections, **Section A, Section B** and **Section C.** Test paper contain multiple choice-type questions. Only ONE of the options given at the end of each question is correct. Section A contains 25 questions Section B and Section C contain 15 questions each. Marking shall be as follows:
- (i) If the answer is **correct**: +3 marks
- (ii) If the answer is *incorrect:* -1
- (iii) If the answer is **not attempted**: 0 marks
- (iv) If more than one box is **marked**: 0 marks

Note that negative marking as indicated above will be implemented.

Website: <a href="http://www.physicsbyfiziks.com">http://www.physicsbyfiziks.com</a>
Email: fiziks.physics@gmail.com



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

- 4. As a rough guideline, the time spent on questions in Section A should be about 5 minutes each; questions in Section B and Section C should take about 8 minutes each. Obviously, some questions may take a little less time while others may require a little more.
- 5. We advise you to first mark the correct answers on the QUESTION PAPER and then to TRANSFER these to the ANSWER SHEET only when you are sure of your choice.
- 6. Rough work may be done on blank pages of the question paper. If needed, you may ask for extra rough sheets from an Invigilator.
- 7. **Use of calculators is permitted**. Calculator which plots graphs is NOT allowed. Multiple-use devices such as cell phones, smart phones etc., CANNOT be used for this purpose.
- 8. Do NOT ask for clarifications from the invigilators regarding the questions. They have been instructed not to respond to any such inquiries from candidates. In case a Correction/clarification is deemed necessary; the invigilator(s) will announce it publicly.



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

#### GS-2013-Y (Physics)

#### **Section A**

#### To be attempted by ALL candidates

Q1. The value of the integral

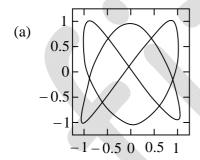
$$\int_{0}^{\infty} dx x^{9} \exp(-x^{2}) \text{ is}$$

- (a) 20160
- (b) 24
- (c) 18
- (d) 12

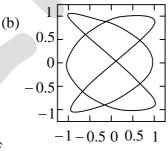
Q2. A two-dimensional vector  $\vec{A}(t)$  is given by

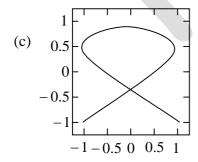
$$\vec{A}(t) = \hat{l} \sin 2t + \hat{j} \cos 3t$$

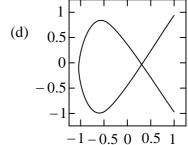
Which of the following graphs best describes the locus of the tip of the vector, as t is varied from 0 to  $2\pi$ ?











Website: <a href="http://www.physicsbyfiziks.com">http://www.physicsbyfiziks.com</a> Email: fiziks.physics@gmail.com



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q3. The differential equation

$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = 0$$

has the complete solution, in terms of arbitrary constants A and B,

(a) 
$$A \exp x + B \exp (-x)$$

(b) 
$$A \exp x + Bx \exp (-x)$$

(c) 
$$x\{A \exp x + B \exp (-x)\}$$

(d) 
$$A \exp x + Bx \exp x$$

Q4. A stone is dropped vertically from the top of a tower of height 40m. At the same time a gun is aimed directly at the stone from the ground at a horizontal distance 30m from the base of the tower and fired. If the bullet from the gun is to hit the stone before it reaches the ground, the minimum velocity of the bullet must be approximately.

(c) 
$$17.7 \text{ ms}^{-1}$$

Q5. Consider the uniform solid right cone depicted in the figure on the right. This cone has mass M and a circular base of radius r. If the moment of inertia of the cone about an axis passing through the centre of mass  $O_{C.M.}$ (see figure) is given by

$$\frac{3}{80}M(4r^2+h^2)$$

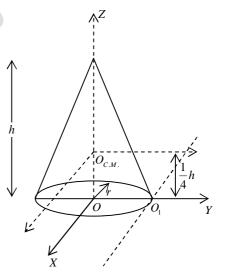
then the moment of inertia about another axis parallel to the X axis, but passing through the point  $O_1$  (see figure), is

(a) 
$$\frac{3}{80}M(4r^2+h^2)$$

(a) 
$$\frac{3}{80}M(4r^2+h^2)$$
 (b)  $\frac{1}{20}M(23r^2+2h^2)$ 

(c) 
$$\frac{3}{40}M(2r^2+h^2)$$

(c) 
$$\frac{3}{40}M(2r^2+h^2)$$
 (d)  $\frac{1}{30}M(15r^2+4h^2)$ 





#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q6. Two planets A and B move around the Sun in elliptic orbits with time periods  $T_A$  and  $T_B$  respectively. If the eccentricity of the orbit of B is  $\varepsilon$  and its distance of closest approach to the Sun is R, then the maximum possible distance between the planets is

[Eccentricity of an ellipse:  $\varepsilon = \frac{r_{\max} - r_{\min}}{r_{\max} + r_{\min}}$ ]

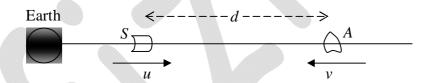
(a) 
$$\frac{1+\varepsilon^2}{1-\varepsilon^2} \left(1 + \frac{T_A^{3/2}}{T_B^{3/2}}\right) R$$

(b) 
$$\sqrt{\frac{1+\varepsilon^2}{1-\varepsilon^2}} \left( 1 + \frac{T_A^{2/3}}{T_R^{2/3}} \right) R$$

(c) 
$$\sqrt{\frac{1+\varepsilon}{1-\varepsilon}\left(1+\frac{T_A^3}{T_B^3}\right)}R$$

(d) 
$$\frac{1+\varepsilon}{1-\varepsilon} \left( 1 + \frac{T_A^{2/3}}{T_B^{2/3}} \right) R$$

Q7. A spaceship S blasts off from the Earth. After some time, Earth station informs the crew that they have settled into a constant velocity 0.28c radially outwards from the Earth, but unfortunately they are on a head-on collision course with an asteroid A at a distance of 15 light-minutes coming in towards the Earth along the same radius (see figure below)



Instruments on-board the spaceship immediately estimate the speed of the asteroid to have a constant value 0.24c. It follows that the maximum time (in minutes) available to the crew to evacuate the ship before the collision is

- (a) 29
- (c)60
- (d) 63

Q8. A point charge q sits at a corner of a cube of side a, as shown in the figure on the right. The flux of the electric field vector through the shaded side (region A) is



- (a)  $\frac{q}{24\varepsilon_0}$
- (b)  $\frac{q}{16\varepsilon_0}$  (c)  $\frac{q}{8\varepsilon_0}$
- (d)  $\frac{q}{6\varepsilon_0}$



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q9. A parallel plate capacitor of circular cross section with radius r >> d, where d is the spacing between the plates, is charged to a potential V and then disconnected from the charging circuit. If, now, the plates are slowly pulled apart (keeping them parallel) so that their separation is increased from d to d', the work done will be

(a) 
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \left( 1 - \frac{d}{d'} \right)$$

(b) 
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \left( \frac{d'}{d} - 1 \right)$$

(c) 
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \frac{d'}{d}$$

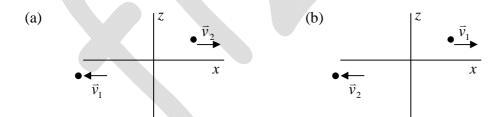
(d) 
$$\frac{\pi \varepsilon_0 r^2 V^2}{2d} \frac{d}{d'}$$

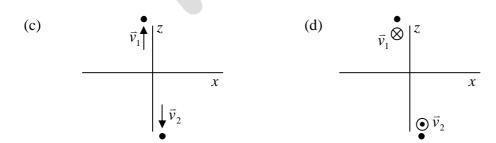
Q10. In the laboratory frame two electrons are shot at each other with equal and opposite velocities  $\vec{u}_1$  and  $\vec{u}_2$  respectively, but not along the same straight line, as shown below.



Each electron will be acted on by the Coulomb repulsion due to the other, as well as the Lorentz force due to its own motion in the magnetic field created by the other. Which of the diagrams given below best describes the final velocities  $\vec{v}_1$  and  $\vec{v}_2$  of these electrons?

[You may assume that the electrons are distinguishable.]





Website: <a href="http://www.physicsbyfiziks.com">http://www.physicsbyfiziks.com</a> Email: fiziks.physics@gmail.com



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q11. A certain amount of fluid with heat capacity C<sub>F</sub> Joules/°C is initially at a temperature 0° C. It is then brought into contact with a heat bath at a temperature of 100° C, and the system is allowed to come into equilibrium. In this process, the entropy (in Joules/°C) of the Universe changes by

- (a)  $100 C_F$
- (b)  $0.044 \, C_{\rm F}$
- (c)  $0.055 C_F$
- (d) 0

Q12. A monatomic gas is described by the equation of state

$$p(V-bn)=nRT$$

where b and R are constants and other quantities have their usual meanings. The maximum density (in moles per unit volume) to which this gas can be compressed is

- (a)  $\frac{1}{h}$
- (b) b
- (c)  $\frac{1}{bn}$
- (d) infinity

Q13. In a quantum mechanical system, an observable A is represented by an operator  $\hat{A}$ . If  $|\psi\rangle$  is a state of the system, but not an eigenstate of  $\hat{A}$ , then the quantity

$$r = \langle \psi | \hat{A} | \psi \rangle^2 - \langle \psi | \hat{A}^2 | \psi \rangle$$

satisfies the relation

- (a) r > 0
- (b) r = 0
- (c) r < 0
- (d)  $r \leq 0$

Q14. Consider a quantum mechanical system with three linear operators  $\hat{A}$ ,  $\hat{B}$  and  $\hat{C}$ , which are related by

$$\hat{A}\hat{B} - \hat{C} = \hat{I}$$

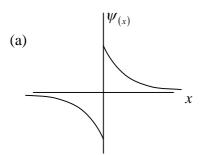
where  $\hat{I}$  is he unit operator. If  $\hat{A} = \frac{d}{dx}$  and  $\hat{B} = x$ , then  $\hat{C}$  must be

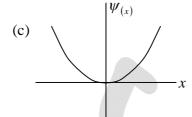
- (a) zero

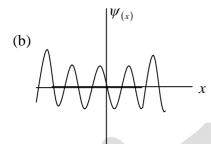
- (b)  $\frac{d}{dx}$  (c)  $x\frac{d}{dx}$  (d)  $-x\frac{d}{dx}$

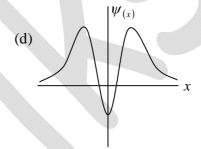
#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q15. A particle of energy E moves in one dimension under the influence of a potential V(x). If E > V(x) for some range of x, which of the following graphs can represent a bound state wave function of the particle?









Q16. In a Davisson-Germer experiment, a collimated beam of electrons of energy 54 eV, at normal incidence on a given crystal, shows a peak at a reflection angle of 40°. If the electron beam is replaced by a neutron beam, and the peak appears at the same value of reflection angle, then the energy of the neutrons must be

- (a) 33 eV
- (b) 0.03 eV
- (c) 0.3 eV
- (d) 330 eV

Q17. The velocity of an electron in the ground state of a hydrogen atom is  $v_H$ . If  $v_p$  be the velocity of an electron in the ground state of positronium, then

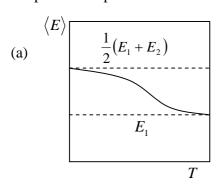
- (a)  $v_p = v_H$

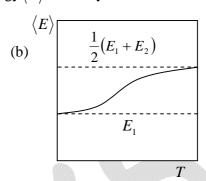
- (b)  $v_p = 2v_H$  (c)  $v_p = \frac{v_H}{2}$  (d)  $v_p = \sqrt{2}v_H$

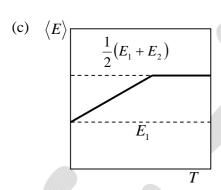


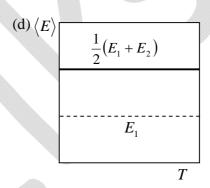
#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q18. Consider an ensemble of microscopic quantum mechanical systems with two energy levels  $E_1$  and  $E_2$ , where  $E_1 < E_2$ . Which of the following graphs best describes the temperature dependence of the average energy  $\langle E \rangle$  of the system?

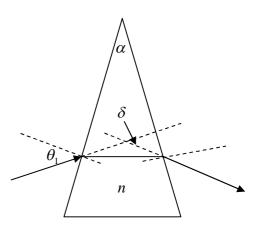








Q19. A ray of light is incident on the surface of a thin prism at a small angle  $\theta_1$  with the normal, as shown in the figure on the right. The material of the prism has refractive index n and you may assume the outside refractive index to be unity. If the (small) apex angle of the prism is  $\alpha$ , the deviation angle  $\delta$  (angle between the incident and exited ray; see figure) is given by

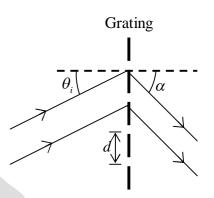


- (a)  $\alpha$
- (b)  $\alpha n$
- (c)  $\alpha(n-1)$
- (d)  $\alpha(n+1)$



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q20. A parallel beam of light of wavelength  $\lambda$  is incident on a transmission grating with groove spacing d, at an angle  $\theta_i$ , as shown in the figure. The plane of incidence is normal to the grooves. After diffraction, the transmitted beam is seen to be at an angle a relative to the normal. Which of the following conditions must be satisfied for this to happen?



(a) 
$$d(\sin \theta_i + \sin \alpha) = n\lambda$$

(b) 
$$d(\sin \theta_i - \sin \alpha) = n\lambda$$

(c) 
$$2d\sin(\theta_i - \alpha) = n\lambda$$

(d) 
$$2d\sin(\theta_i + \alpha) = n\lambda$$

Q21. Let  $E_N$  be the energy released when one mole of pure  $^{235}$ U undergoes controlled fission, and  $E_C$  be the energy released when one mole of pure carbon undergoes complete combustion. The ratio  $E_N/E_C$  will have the order of magnitude

(a) 
$$10^4$$

(b) 
$$10^8$$

(c) 
$$10^9$$

(d) 
$$10^6$$

Q22. The entropy S of a black hole is known to be of the form

$$S = \alpha k_B A$$

where A is the surface area of the black hole and  $\alpha$  is a constant, which can be written in terms of c (velocity of light in vacuum),  $\hbar$  (reduced Plank's constant) and  $G_N$  (Newton's constant of gravitation). Taking the radius of the black hole as

$$R = \frac{2G_N M}{c^2}$$

it follows that the entropy S is

 $[\lambda \text{ is a numerical constant}]$ 

(a) 
$$\frac{G_N^2 M^2 k_B}{\lambda (\hbar c)^4}$$

(b) 
$$\frac{\hbar c k_B}{\lambda G_N M}$$

(c) 
$$\frac{G_N^2 M^2 k_B}{\lambda \hbar c^4}$$

(c) 
$$\frac{G_N^2 M^2 k_B}{\lambda \hbar c^4}$$
 (d)  $\frac{G_N M^2 k_B}{\lambda \hbar c}$ 



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q23. The circuit depicted on the right has been made with a silicon n-p-n transistor.

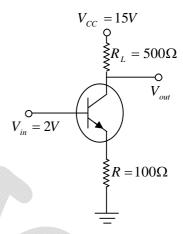
Assuming that there will be a 0.7 V drop across a forward-biased silicon p-n junction, the power dissipated across the transistor will be, approximately,



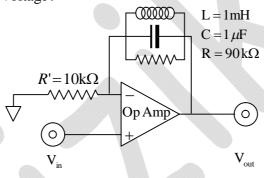
(b) 94 mW

(c) 17 mW

(d) 67 mW



Q24. An input of 1.0 V DC is given to the ideal Op-Amp circuit depicted below. What will be the output voltage?



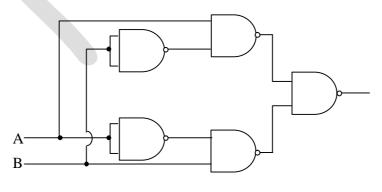
(a) 10.0 V

(b) 1.0 V

(c) 0 V

(d) - 9.0 V

Q25. The circuit below uses only NAND gates. Find the final output.



(a) A XOR B

(b) A OR B

(c) A AND B

(d) A NOR B



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

#### GS - 2013 - Y (Physics)

#### **Section B**

#### To be attempted only by candidates for Integrated Ph.D. programme.

(Candidate for Ph.D. programme will get no credit for attempting this section.)

Q26. Consider the surface corresponding to the equation

$$4x^2 + y^2 + z = 0$$

A possible unit tangent to this surface at the point (1, 2, -8) is

(a) 
$$-\frac{1}{\sqrt{5}}\hat{i} + \frac{3}{\sqrt{5}}\hat{j} - \frac{4}{\sqrt{5}}\hat{k}$$

(b) 
$$\frac{1}{5}\hat{j} - \frac{4}{5}\hat{k}$$

(c) 
$$\frac{4}{9}\hat{i} - \frac{8}{9}\hat{j} + \frac{1}{9}\hat{k}$$

(d) 
$$\frac{1}{\sqrt{5}}\hat{i} - \frac{2}{\sqrt{5}}\hat{j}$$

Q27. A particle with time-varying mass  $m(t) = m_0 \left(1 - \frac{t}{\tau}\right)$ , where  $m_0$  and  $\tau$  are positive

constants, moves along the x-axis under the action of a constant positive force F for  $0 \le t < \tau$ . If the particle is at rest at time t = 0, then at time t = t, its velocity v will be

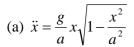
(a) 
$$-\frac{\tau F}{m_0} \log \left(1 - \frac{t}{\tau}\right)$$

(b) 
$$-\frac{Ft}{m_0}\log\frac{t}{\tau}$$

(c) 
$$\frac{Ft}{m_0} \left(1 - \frac{t}{\tau}\right)^{-1}$$

(d) 
$$\frac{\tau F}{m_0} \left( 1 - \frac{t}{\tau} \right)$$

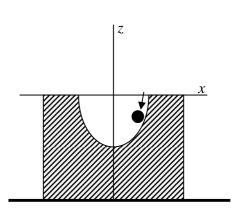
Q28. A ball of mass m slides under gravity without friction inside a semicircular depression of radius a inside a fixed block placed on a horizontal surface, as shown in the figure. The equation of motion of the ball in the *x*-direction will be



(a) 
$$\ddot{x} = \frac{g}{a} x \sqrt{1 - \frac{x^2}{a^2}}$$
 (b)  $\ddot{x} = -\frac{g}{a} x \sqrt{1 - \frac{x^2}{a^2}}$ 

(c) 
$$\ddot{x} = -\frac{g}{a}x$$

(d) 
$$\ddot{x} = \frac{g}{a}x$$





#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q29. A particle P, of rest mass M and energy E, suddenly decays into two particles A and B of rest masses  $m_A$  and  $m_B$  respectively, and both particles move along the straight line in which P was moving. A possible energy  $E_A$  of the particle A will be

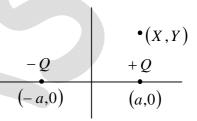
(a) 
$$\frac{E}{2} \left\{ 1 + \left( \frac{m_A - m_B}{M} \right)^2 \right\}$$

(b) 
$$\frac{E}{2} \left\{ 1 - \left( \frac{m_A^2 - m_B^2}{M^2} \right)^2 \right\}$$

(c) 
$$\frac{E}{2} \left\{ 1 + \left( \frac{m_A + m_B}{M} \right)^2 \right\}$$

(d) 
$$\frac{E}{2} \left\{ 1 + \left( \frac{m_A^2 - m_B^2}{M^2} \right) \right\}$$

Q30. Consider two charges +Q and -Q placed at the points (a, 0) and (-a, 0) in a place, as shown in the figure on the right. If the origin is moved to the point (X, Y), the magnitude of the dipole moment of the given charge distribution with respect to this origin will be



(a) 
$$Q\sqrt{(a-X)^2+y^2}-Q\sqrt{(a+X)^2+y^2}$$

(c) 
$$Q(a-X)-Q(-a+X)$$

(d) 
$$2Qa\sqrt{X^2 + Y^2}$$

Q31. A plane electromagnetic wave traveling in a vacuum is characterized by the electric and magnetic fields

$$\vec{E} = \hat{i} (30\pi V m^{-1}) \exp i(\omega t + kz)$$

$$\vec{H} = \hat{j} (H_0 A m^{-1}) \exp i(\omega t + kz)$$

If  $\omega$ , k > 0, the value of  $H_0$  must be

- (a) 0.25
- (b) 0.67
- (c) 0.94
- (d)  $2\pi$

Q32. Which of the following classic experiments provides unambiguous proof that the Earth is a non-inertial frame of reference with respect to the fixed stars?

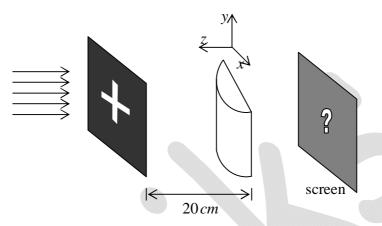
- (a) Fizeau's rotating wheel experiment
- (b) Michelson-Morley experiment
- (c) Foucault's pendulum experiment
- (d) Newton's coin-and-feather experiment



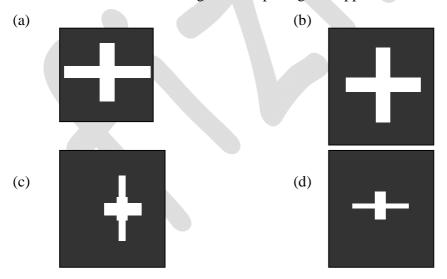


#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q33. A cross-shaped opening is illuminated by a parallel beam of white light. A thin plano-convex cylindrical glass lens is placed 20 cm in front of it, as shown in the figure below.



The radius of curvature of the curved surface of the lens is 5 cm and 1.5 is the refractive index of glass. On a screen placed as shown at the plane where a real image forms on the other side of the lens, the image of the opening will appear as



Email: fiziks.physics@gmail.com

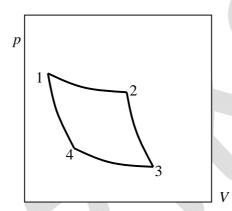


#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q34. A classical ideal gas, consisting of N particle  $(N \to \infty)$  is confined in a box of volume V at temperature T and pressure p. The probability that, at any instant of time, a small sub-volume  $v_0$  becomes totally void (i.e. no particles inside), due to a spontaneous statistical fluctuation, is

- (a)  $\exp\left(\frac{-v_0}{V}\right)$
- (b)  $\frac{pv_0}{NT}$  (c)  $\frac{v_0}{V} \exp\left(\frac{-pV}{NT}\right)$  (d)  $\exp\left(-\frac{Nv_0}{V}\right)$

Q35. The pV diagram for a Carnot cycle executed by an ideal gas with  $C_P/C_V = \gamma > 1$  is shown below. Note that 1, 2, 3 and 4 label the change over points in the cycle



If, for this cycle,

$$\frac{T_2}{T_3} = \left(\frac{p_2}{p_3}\right)^X$$

then X =

- (a)  $1 \frac{1}{\gamma}$
- (b) 0
- (c) 1
- (d)  $-\frac{1}{v}$

Q36. A harmonic oscillator has the wave function,

$$\psi(x,t) = \frac{1}{5} \left[ 3\varphi_0(x,t) - 2\sqrt{2}\varphi_1(x,t) + 2\sqrt{2}\varphi_2(x,t) \right]$$

where  $\varphi_n(x,t)$  is the eigenfunction belonging to the  $n^{\text{th}}$  energy eigenvalue  $\left(n+\frac{1}{2}\right)\hbar\omega$ .

The expectation value  $\langle E \rangle$  of energy for the state  $\psi(x,t)$  is

- (a)  $1.58 \hbar \omega$
- (b)  $0.46 \, \hbar \omega$
- (c)  $\hbar\omega$
- (d) 1.46  $\hbar\omega$



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q37. An energy eigenstate of the Hydrogen atom has the wave function

$$\psi_{n\ell m}(r,\theta,\varphi) = \frac{1}{81\sqrt{\pi}} \left(\frac{1}{a_0}\right)^{3/2} \sin\theta \cos\theta \exp\left[-\left(\frac{r}{3a_0} + i\varphi\right)\right]$$

where  $a_0$  is the Bohr radius. The principal (n), azimuthal ( $\ell$ ) and magnetic (m) quantum numbers corresponding to this wave function are

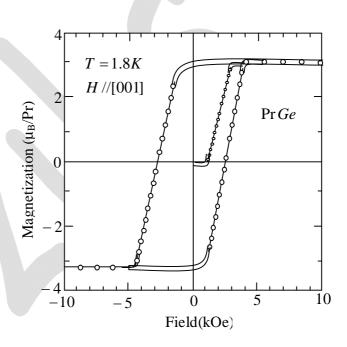
(a) 
$$n = 3$$
,  $\ell = 2$ ,  $m = 1$ 

(b) 
$$n = 2$$
,  $\ell = 1$ ,  $m = 1$ 

(c) 
$$n = 3$$
,  $\ell = 2$ ,  $m = -1$ 

(d) 
$$n = 2$$
,  $\ell = 1$ ,  $m = \pm 1$ 

The Curie temperature of a single crystal of PrGe is known to be 41 K. The magnetization data of this sample is measured at 1.8 K for the magnetic field applied parallel to the [001] direction is shown in the figure on the right. At a temperature of 38 K, the hysteresis loop in the figure will



- (a) increase in width
- (b) decrease in width
- (c) have the same width
- (d) shrink to a line
- Q39. Consider two energies of a free electron gas in a metal at an absolute temperature T, viz.,

$$E_{\pm} = E_F \pm \Delta$$

where  $E_F$  is the Fermi level. If the corresponding electron populations  $n(E_{\pm})$  satisfy the relation  $n(E_{-}) / n(E_{+}) = 2$ , then  $\Delta =$ 

(a)  $k_BT$ 

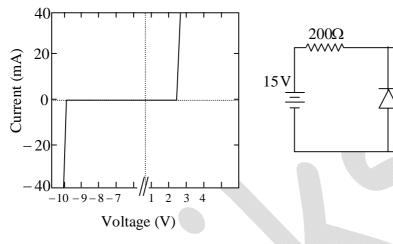
(b)  $k_B T \ln 2$  (c)  $\frac{k_B T}{2}$ 

(d)  $2 k_B T$ 



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q40. The figure below shows the current voltage characteristics of a diode over a range of voltage and current where it is safe to operate the diode.



When this diode is used in the circuit on the extreme right, the approximate current, in mA, through the diode will be

- (a) 8.3
- (b) 16.7
- (c) 25
- (d) 0

 $\xi$ 600 $\Omega$ 

Website: <a href="http://www.physicsbyfiziks.com">http://www.physicsbyfiziks.com</a> Email: fiziks.physics@gmail.com





#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

#### GS-2013-Y (Physics)

#### **Section C**

#### To be attempted only by candidates for Ph.D. programme.

(Candidate for Integrated Ph.D. programme will get no credit for attempting this section.)

Q41. The integral

$$\int_{-\infty}^{\infty} dx \, \delta(x^2 - \pi^2) \cos x$$

evaluates to

- (a) -1
- (b) 0
- $(c) \frac{1}{\pi}$
- (d)  $\frac{1}{\pi}$

Q42. If z = x + iy then function

$$f(x, y) = (1 + x + y)(1 + x - y) + a(x^2 - y^2) - 1 + 2iy(1 - x - ax)$$

where a is a real parameter, is analytic in the complex z plane if a =

- (a) -1
- (b) +1
- (c) (
- (d) i

Q43. A particle of mass m moves in one dimension under the influence of a potential energy

$$V(x) = -a\left(\frac{x}{I}\right)^2 + b\left(\frac{x}{I}\right)^4$$

where a and b are positive constants and  $\ell$  is a characteristic length. The frequency of small oscillations about a point of stable equilibrium is

(a)  $\frac{1}{2\pi\ell}\sqrt{\frac{b}{m}}$ 

(b)  $\frac{1}{\pi \ell} \sqrt{\frac{a^2}{mb}}$ 

(c)  $\frac{2b}{\pi \ell} \sqrt{\frac{1}{ma}}$ 

(d)  $\frac{1}{\pi \ell} \sqrt{\frac{a}{m}}$ 



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q44. If a central force acting on a particle of mass m is given by

$$F(r) = -\frac{k}{r^2}$$

where r is the distance of the particle from the origin and k is a positive constant, the Hamiltonian for the system, in spherical polar coordinates, will have the form

(a) 
$$\frac{1}{2}m(\dot{r}^2 + r^2\dot{\theta}^2 + r^2\sin^2\theta\dot{\varphi}^2) + \frac{k}{r}$$

(b) 
$$\frac{1}{2mr^2} (r^2 p_r^2 + p_\theta^2 + p_\phi^2 + 2mkr)$$

(c) 
$$\frac{p_r^2}{2m} + \frac{p_\theta^2}{2mr^2} + \frac{p_\phi^2 \csc^2 \theta}{2mr^2} + \frac{k}{r}$$

(d) 
$$\frac{p_r^2}{2m} + \frac{p_\theta^2}{2m} + \frac{p_\phi^2}{2m} + \frac{k}{r}$$

Q45. The magnetic vector potential  $\vec{A}(\vec{r})$  corresponding to a uniform magnetic field  $\vec{B}$  is taken in the form

$$\vec{A} = \frac{1}{2}\vec{B} \times \vec{r}$$

where  $\vec{r}$  is the position vector. If the electric field has the time-dependent form  $\vec{E} = \vec{E}_0(\vec{r})e^{i\omega t}$ , where  $\omega$  is a constant, the gauge choice corresponding to this potential is a

(a) non-linear gauge

(b) Lorenz gauge

(c) time-varying gauge

(d) Coulomb gauge

Q46. A binary star is observed to consist of a blue star B (peak wavelength 400 nm) and a red star R (peak wavelength 800 nm) orbiting each other. As observed from the Earth, B and R appear equally bright. Assuming that the stars radiate as perfect blackbodies, it follows that the ratio of volumes  $V_B / V_R$  of the two stars is

(a) 64

(b) 1/64

(c) 16

(d) 1/16



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q47. An system at temperature T has three energy states  $0, \pm \varepsilon$ . The entropy of the system in the low temperature  $(T \to 0)$  and high temperature  $(T \to \infty)$  limits are, respectively,

- (a)  $S_{T\to 0} = 0$  and  $S_{T\to \infty} = k_B \ln 3$
- (b)  $S_{T\to 0} = S_{T\to \infty} = k_B \ln 3$
- (c)  $S_{T\to 0} = 0$  and  $S_{T\to \infty} = k_B \exp(-3)$
- (d)  $S_{T\rightarrow 0} = 0$  and  $S_{T\rightarrow \infty} = 3k_B/2$

Q48. The state  $|\psi\rangle$  of a quantum mechanical system, in a certain basis, is represented by the column vector

$$\left|\psi\right\rangle = \begin{pmatrix} 1/\sqrt{2} \\ 0 \\ 1/\sqrt{2} \end{pmatrix}$$

The operator  $\hat{A}$  corresponding to a dynamical variable A, is given, in the same basis, by the matrix

$$\hat{A} = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 2 \end{pmatrix}$$

If, now a measurement of the variable A is made on the system in the state  $|\psi\rangle$ , the probability that the result will be +1 is

- (a)  $\frac{1}{4}$
- (b)  $\frac{1}{\sqrt{2}}$
- (c)  $\frac{1}{2}$
- (d) 1

Q49. A spin ½ particle A decays to two other particles B and C. If B and C are of spin ½ and spin-1 respectively, then a complete list of the possible values of the orbital angular momentum of the final state (i.e. B + C) is

- (a) 0, 1
- (b)  $\frac{1}{2}, \frac{3}{2}$
- (c) 0, 1, 2
- (d)  $0, \pm 1$



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q50. When a pure element is vaporized and placed in a uniform magnetic field  $B_0$ , it is seen that a particular spectral line of wavelength  $\lambda$ , corresponding to a  $J=1 \to J=0$  transition, gets split into three components  $\lambda$ ,  $\lambda \pm \Delta \lambda$ . It follows that the Lande g-factor for the transition  $J=1 \to J=0$  is given by

(a) 
$$g = \frac{hc}{\mu_B B_0} \frac{\Delta \lambda^2}{\lambda}$$

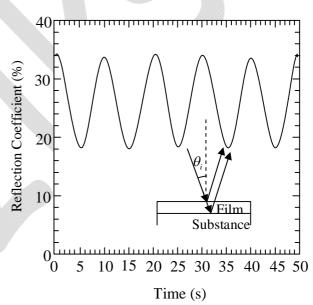
(b) 
$$g = \frac{hc}{\mu_B B_0} \frac{\Delta \lambda}{\lambda^2}$$

(c) 
$$g = \frac{hc}{\mu_B B_0} \frac{\lambda^2}{\Delta \lambda}$$

(d) 
$$g = \frac{hc}{\mu_B B_0} \frac{\lambda}{\Delta \lambda^2}$$

Q51. The rate of deposition of a dielectric thin film on a thick dielectric substrate was

monitored by the following experiment: a laser beam of wavelength  $\lambda = 633$  nm, at near-normal incidence  $\theta_i$ , was reflected from the thin film (see figure), and the reflection coefficient R was measured. As the film thickness increased R varied with time as shown in the figure. The refractive index of the film is 3.07 and is less than that of the substrate. Using the graph, the approximate thickness of the film at the end of 25 seconds can be estimated to be



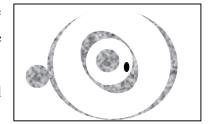
- (a) 0.017 μm
- (b)  $0.51 \, \mu m$
- (c)  $0.26 \, \mu m$
- (d)  $2.2 \, \mu m$



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

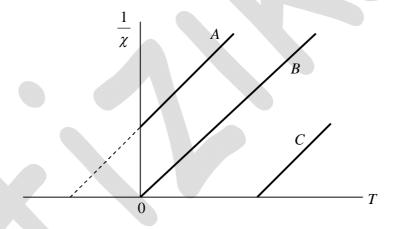
Q52. The negative image on the right represents a very small portion of the night sky at a

very high resolution. Notice the broken ring(s) around the central bright object in the middle of the picture. These are most likely to be due to



- (a) gravitational lensing of a distant object by the central massive object
- (b) gas clouds forming the remnant of a supernova explosion
- (c) debris from a smaller object torn apart by tidal forces
- (d) ice collected on the lens used for taking the picture

Q53. The magnetic susceptibility  $\chi$  of three sample A, B and C, is measured as a function of their absolute temperature T, leading to the graphs shown below.



From these graphs, the magnetic nature of the samples can be inferred to be

(a) A: anti-ferromagnet B: diamagnet C: paramagnet

(b) A: diamagnet B: paramagnet C: anti-ferromagnet

(c) A: paramagnet B: anti-ferromagnet C: ferromagnet

(d) A: anti-ferromagnet B: paramagnet C: ferromagnet

Email: fiziks.physics@gmail.com



#### Forum for CSIR-UGC JRF/NET, GATE, IIT-JAM, GRE in PHYSICAL SCIENCES

Q54. A gold foil, having N(0) number of <sup>197</sup>Au nuclides per cm<sup>2</sup>, is irradiated by a beam of thermal neutrons with a flux of F neutrons-cm<sup>-2</sup>-s<sup>-1</sup>. As a result, the nuclide  $^{198}$ Au, with a half life  $\tau$  of several years, is produced by the reaction

$$^{197}$$
Au +  $n \rightarrow ^{198}$ Au +  $\gamma$ 

which has a cross section of  $\sigma$  cm<sup>2</sup>. Assuming that the gold foil has 100% abundancy of <sup>197</sup>Au nuclides, the maximum number of <sup>198</sup>Au nuclides that can accumulate at any time in the foil is proportional to

(a) 
$$\frac{\sigma F}{\tau} N(0)$$

(b) 
$$\frac{1}{\sigma \tau F} N(0)$$
 (c)  $\frac{\tau}{\sigma F} N(0)$ 

(c) 
$$\frac{\tau}{\sigma F} N(0)$$

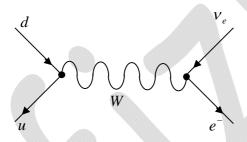
(d) 
$$\sigma \tau FN(0)$$

The process of electron capture

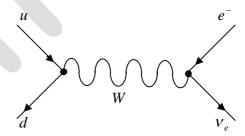
$$p + e^{-} \rightarrow n + v_{e}$$

takes place at the quark level through the Feynman diagram

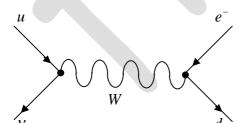
(a)



(b)



(c)



(d)

