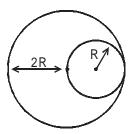
Physics

41. A circular disc of radius R is removed from a bigger circular disc of radius 2R such that the circumferences of the discs coincide. The centre of mass of the the new disc is $\frac{\alpha}{R}$ from the center of the bigger disc. The value of α is

(1)
$$\frac{1}{4}$$
 (2) $\frac{1}{3}$ (3) $\frac{1}{2}$ (4) $\frac{1}{6}$

Sol. (2)



Let the mass of the larger disc be M. Then mass of the smaller disc $=\frac{M}{4R^2} \times R^2 = \frac{M}{4}$

Mass of remaining part = $\frac{3M}{4}$

If the position of the centre of mass of the remaining disc be (x, 0) with respect to the centre of the larger disc, then

$$\frac{3M}{4}(x) + \frac{M}{4}(R) = M(0)$$

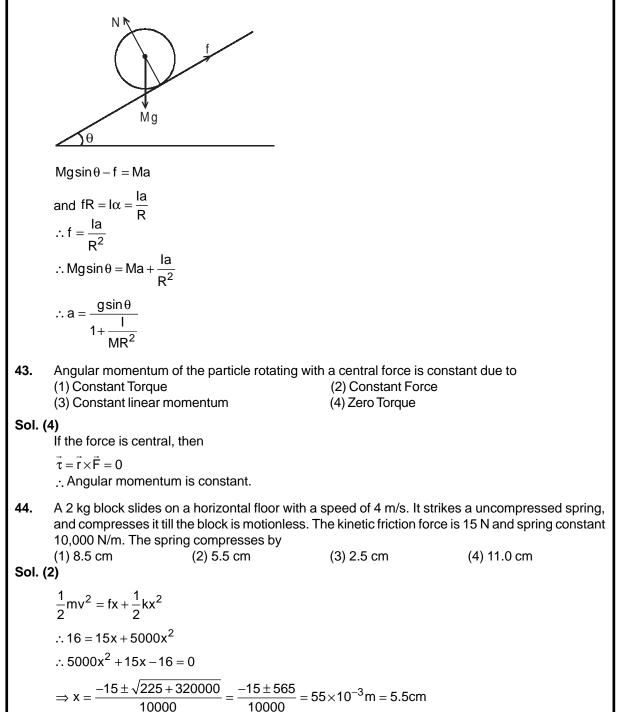
$$\therefore x = \frac{-R}{3}$$

"If the centre of mass of the new disc is αR from the centre of the bigger disc, then $\alpha = \frac{1}{2}$ "

- **42.** A round uniform body of radius R, mass M and moment of inertia 'l', rolls down (without slipping) an inclined plane making an angle θ with the horizontal. Then its acceleration is
 - (1) $\frac{g \sin \theta}{1 MR^2 / I}$ (2) $\frac{g \sin \theta}{1 + I / MR^2}$ (3) $\frac{g \sin \theta}{1 + MR^2 / I}$ (4) $\frac{g \sin \theta}{1 I / MR^2}$



Sol. (2)



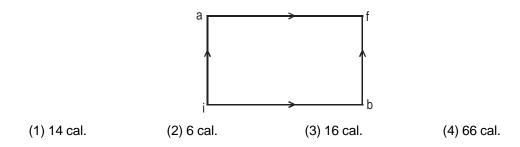
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45.	A particle is projected at 60° to the horizontal with a kinetic energy K. The kinetic energy at highest point is							
	(1) K / 2	(2) K	(3) Zero	(4) K / 4				
Sol. (4)								
	If v ₀ is the velocity of projection, then the velocity at the highest point is v ₀ cos 60° = $\frac{v_0}{2}$							
	$\therefore k = \frac{1}{2}mv_0^2$							
	$\frac{1}{2} \kappa = \frac{1}{2} m v_0^2$ At the highest point							
	K.E. $=\frac{1}{2}m\left(\frac{v_0}{2}\right)^2 = \frac{K}{4}$							
46.	In the Young's double slit experiment the intensity at a point where the path-difference is $rac{\lambda}{6}$							
	(λ being the wavelength of the light used) is I. If I_0 denotes the maximum intensity, $\frac{1}{I_0}$ is equal to							
	(1) $\frac{3}{4}$	(2) $\frac{1}{\sqrt{2}}$	(3) $\frac{\sqrt{3}}{2}$	(4) $\frac{1}{2}$				
Sol.	(1)							
	Phase difference, $\phi = \left(\frac{\Delta x}{\lambda}\right) \cdot 2\pi = \frac{\pi}{3}$							
	$I = I' + I' + 2\sqrt{I' \cdot I'} \cos \frac{\pi}{3} = 3I'$							
	But $I_0 = 4I' (\phi = 0)$							
	$\therefore \frac{1}{I_0} = \frac{3}{4}$							
47.	Two springs, of force constant k_1 and k_2 , are connected to a mass m as shown. The frequency of oscillation of the mass is f. If both k_1 and k_2 are made four times their original values, the frequency of oscillation becomes							
	L							
	(1) 2f	(2) f / 2	(3) f / 4	l (4) 4f				



Sol. (1)

$$f = \sqrt{\frac{k_{eff}}{m}} = \sqrt{\frac{k_1 + k_2}{m}}$$
$$f' = \sqrt{\frac{4k_1 + 4k_2}{m}} = 2\sqrt{\frac{k_1 + k_2}{m}} = 2f$$

48. When a system is taken from state i to state f along the path iaf, it is found that Q = 50 cal and W = 20 cal. Along the path ibf Q = 36 cal. W along the path ibf is



Sol. (2)

 ΔU for both the paths will be the same.

$$\begin{split} \therefore \Delta U_{iaf} &= \Delta U_{ibf} \\ \therefore Q_{iaf} - W_{iaf} &= Q_{ibf} - W_{ibf} \\ \text{or } 50 - 20 &= 36 - W_{ibf} \\ \therefore w_{ibf} &= 6 \text{ cal} \end{split}$$

- **49.** A particle of mass m executes simple harmonic motion with amplitude 'a' and frequency 'v'. The average kinetic energy during its motion from the position of equilibrium to the end is
 - (1) $2\pi^2 \text{ m } a^2 v^2$ (2) $\pi^2 \text{ m } a^2 v^2$ (3) $\frac{1}{4} \text{ m } a^2 v^2$ (4) $4\pi^2 \text{ m } a^2 v^2$

Let $y = a \sin \omega t$

$$\therefore v = \frac{dy}{dt} = a\omega \cos \omega t$$
$$\therefore k = \frac{1}{2}mv^2 = \frac{1}{2}ma^2\omega^2 \cos^2 \omega t$$
$$\therefore \text{ Average KE:}$$

Code : N

$$K_{avg} = \int_{0}^{T/4} \frac{kdt}{\int_{0}^{1} dt} = \frac{\frac{1}{2}ma^{2}\omega^{2}\int_{0}^{T/4} \cos^{2} \omega dt}{T/4}$$

$$= \frac{ma^{2}\omega^{2}}{T} \frac{1}{2} \int_{0}^{1/4} (1 + \cos 2\omega t) dt = \frac{ma^{2}\omega^{2}}{2T} \left[t + \frac{\sin 2\omega t}{2\omega} \right]_{0}^{T/4}$$

$$= \frac{ma^{2}\omega^{2}}{2T} \left[\frac{T}{4} + \frac{\sin \omega^{T}/2}{2\omega} \right] = \frac{1}{4}ma^{2}\omega^{2} (: \omega T = 2\pi)$$

$$= \frac{1}{4}ma^{2} (4\pi^{2}v^{2}) = \pi^{2}ma^{2}v^{2}$$
50. The displacement of an object attached to a spring and executing simple harmonic motion is given
by x = 2 \times 10^{-2} \cos \pi t metres. The time at which the maximum speed first occurs is
(1) 0.25 s (2) 0.5 s (3) 0.75 s (4) 0.125 s
Sol (2)
x = 2 \times 10^{-2} \cos(\pi t); SHM with particle at extreme position at t = 0.
 \Rightarrow Velocity is maximum for the 1s⁴ time when it crosses the origin i.e. $t = \frac{T}{4}$
 $\omega = \pi$
or $\frac{2\pi}{T} = \pi$ $\Rightarrow t = \frac{T}{4} = 0.5 s$
51. In an a.c. circuit the voltage applied is E = E₀ sin ω t. The resulting current in the circuit is
 $1 = l_{0} \sin(\omega - \frac{\pi}{2})$. The power consumption in the circuit is given by
(1) $P = \sqrt{2} E_{0} l_{0}$ (2) $P = \frac{E_{0} l_{0}}{\sqrt{2}}$ (3) $P = zero$ (4) $P = \frac{E_{0} l_{0}}{2}$
Sol (3)
 $P = \frac{E_{0} l_{0}}{2} \cos \pi / 2 = 0$

52. An electric charge $10^{-3} \mu c$ is placed at the origin (0, 0) of X – Y co-ordinate system. Two points A and B are situated at $(\sqrt{2}, \sqrt{2})$ and (2, 0) respectively. The potential difference between the points A and B will be (1) 4.5 volt (2) 9 volt (3) zero (4) 2 volt

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Sol. (3)

I

$$A (\sqrt{2}, \sqrt{2})$$

$$(0, 0) r_2 (2, 0) B$$

$$V_A = \frac{k \cdot q}{r}$$

$$V_{B} = \frac{k \cdot q}{r_{2}}$$

$$V_{A} - V_{B} = \frac{kq}{r_{1}} - \frac{kq}{r_{2}} = 9 \times 10^{9} \times 10^{-9} \left\{ \frac{1}{2} - \frac{1}{2} \right\} = 0$$

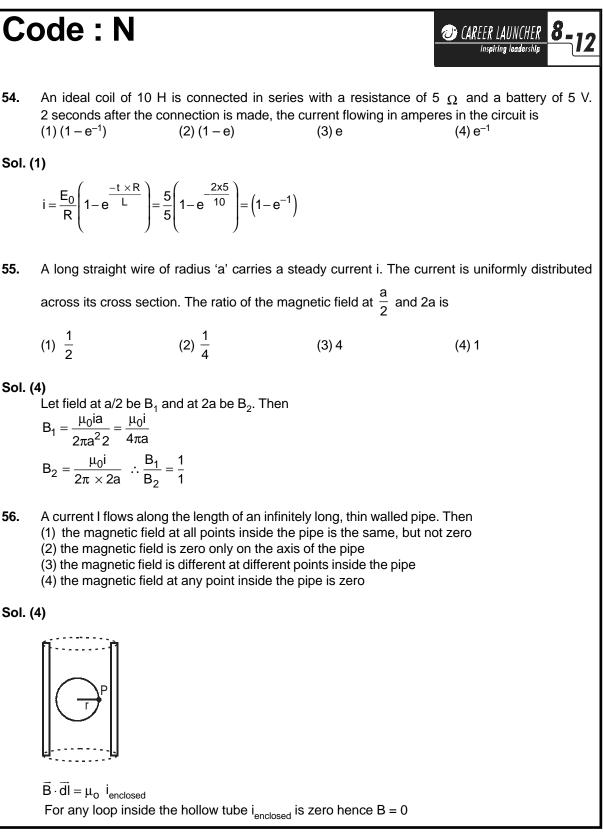
53. A battery is used to charge a parallel plate capacitor till the potential difference between the plates becomes equal to the electromotive force of the battery. The ratio of the energy stored in the capacitor and the work done by the battery will be

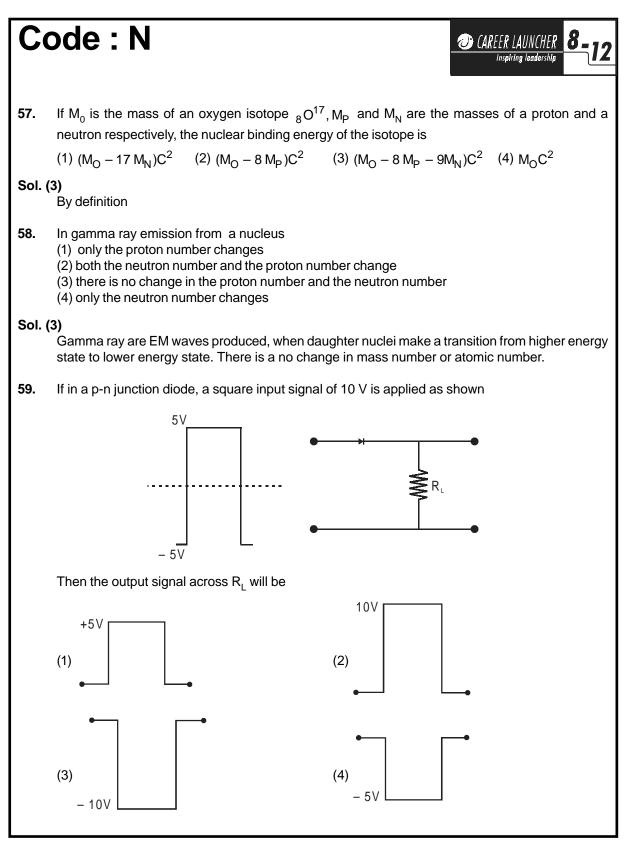
(1)
$$\frac{1}{2}$$
 (2) 1 (3) 2 (4) $\frac{1}{4}$

Sol. (1)

Energy shared in the battery $=\frac{1}{2}$ QV Work done by the battery = QV

ratio =
$$\frac{\frac{1}{2}QV}{QV} = \frac{1}{2}$$



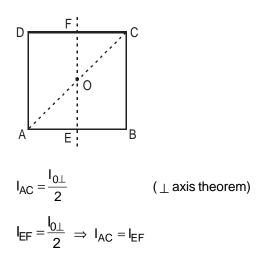


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Code : N 🕗 CAREER LAUNCHER 👌 Sol. (1) Half wave rectification Photon of frequency ν has a momentum associated with it. If c is the velocity of light, the 60. momentum is (4) h v/c² (1) h v/c (2) v/c (3) hvc Sol. (1) $P = \frac{h}{\lambda} = \frac{h \cdot v}{c}$ The velocity of a particle is $v = v_0 + gt + ft^2$. If its position is x = 0 at t = 0, then its displacement 61. after unit time (t = 1) is (1) $v_0 + g/2 + f$ (3) $v_0 + g/2 + f/3$ (2) $v_0 + 2g + 3f$ (4) $v_0 + g + f$ Sol. (3) $v = v_0 + gt + ft^2$ $x = x_0 + v_0 t + \frac{1}{2}gt^2 + \frac{ft^3}{3}$ $x\big|_{t=0} = 0$ $\Rightarrow x_0 = 0$ $x\Big|_{t=1} = v_0 + \frac{g}{2} + \frac{f}{3}$ 62. For the given uniform square lamina ABCD, whose centre is O, D С В E (1) $I_{AC} = \sqrt{2} I_{FF}$ (2) $\sqrt{2}I_{AC} = I_{FF}$ (3) $I_{AD} = 3I_{FF}$ (4) $I_{AC} = I_{EF}$



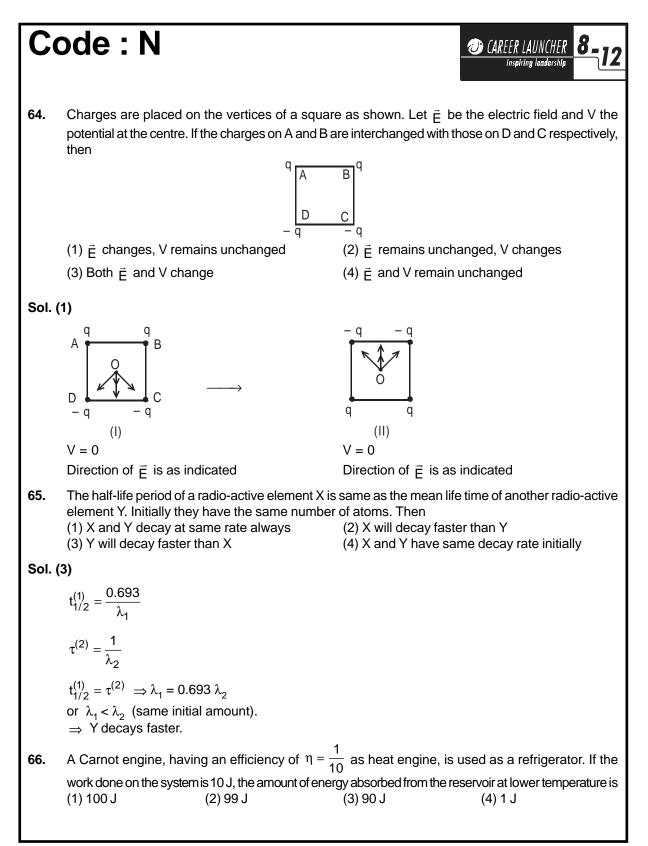
Sol. (4)



- **63.** A point mass oscillates along the x-axis according to the law $x = x_0 \cos(\omega t \pi/4)$. If the acceleration of the particle is written as $a = A\cos(\omega t + \delta)$, then
 - (1) $A = x_0 \omega^2$, $\delta = \frac{3\pi}{4}$ (2) $A = x_0$, $\delta = -\frac{\pi}{4}$ (3) $A = x_0 \omega^2$, $\delta = \frac{\pi}{4}$ (4) $A = x_0 \omega^2$, $\delta = -\frac{\pi}{4}$

Sol. (4)

$$x = x_0 \cos\left(\cot - \frac{\pi}{4}\right)$$
$$\frac{dx}{dt} = -x_0 \omega^2 \sin\left(\omega t - \frac{\pi}{4}\right)$$
$$\frac{d^2 x}{dt^2} = -x_0 \omega^2 \cos\left(\omega t - \frac{\pi}{4}\right)$$
$$\Rightarrow A = x_0 \omega^2; \ \delta = -\frac{\pi}{4}$$





Sol. (3)

For a heat engine

$$\eta = \frac{W}{Q_H}$$

$$\Rightarrow Q_{H} = \frac{W}{\eta} = 100 J$$

$$Q_{H} = Q_{L} + W$$

 $Q_L = 90 J$

When the same engine is used as a refrigerator, heat will be absorbed from the system at lower temperature. Hence heat absorbed at lower temperature = $Q_1 = 90 \text{ J}$

- **67.** Carbon, silicon and germanium have four valence electrons each. At room temperature which one of the following statements is most appropriate?
 - (1) The number of free electrons for conduction is significant only in Si and Ge but small in C.
 - (2) The number of free conduction electrons is significant in C but small in Si and Ge.
 - (3) The number of free conduction electrons is negligibly small in all the three.
 - (4) The number of free electrons for conduction is significant in all the three.

Sol. (1)

The 4 bonding electrons of C, Si or Ge lie, respectively, in the second, third and fourth orbit. Hence, energy required to take out an electron from these atoms (i.e. ionisation energy E_g) will be least for Ge, followed by Si and highest for C. Hence, number of free electrons for conduction in Ge and Si are significant but negligibly small for C. (NCERT Book – XII, Page – 415)

68. A charge particle with charge q enters a region of constant, uniform and mutually orthogonal fields \vec{E} and \vec{B} with a velocity \vec{v} perpendicular to both \vec{E} and \vec{B} , and comes out without any change in magnitude or direction of \vec{v} . Then

(1) $\vec{v} = \vec{B} \times \vec{E} / E^2$	(2) $\vec{v} = \vec{E} \times \vec{B} / B^2$
(3) $\vec{v} = \vec{B} \times \vec{E} / B^2$	$(4) \ \vec{v} = \vec{E} \times \vec{B} / E^2$



Sol. (2)

$$\vec{V} \bigoplus \vec{E}$$

$$\vec{F}_{e} = q\vec{E}$$

$$\vec{F}_{B} = q\vec{v} \times \vec{B}$$

$$q\vec{E} + q\vec{v} \times \vec{B} = 0 \implies \vec{E} \times \vec{B} + \vec{v} \times \vec{B} \times \vec{B} = 0$$

$$\vec{E} \times \vec{B} + (\vec{B} \cdot \vec{v})\vec{B} - (\vec{B} \cdot \vec{B})\vec{v} = 0$$
or $\vec{v} = \frac{\vec{E} \times \vec{B}}{B^{2}}$

69. The potential at a point x (measure in μ m) due to some charges situated on the x-axis is given by V(x) = 20 / (x² - 4) Volts

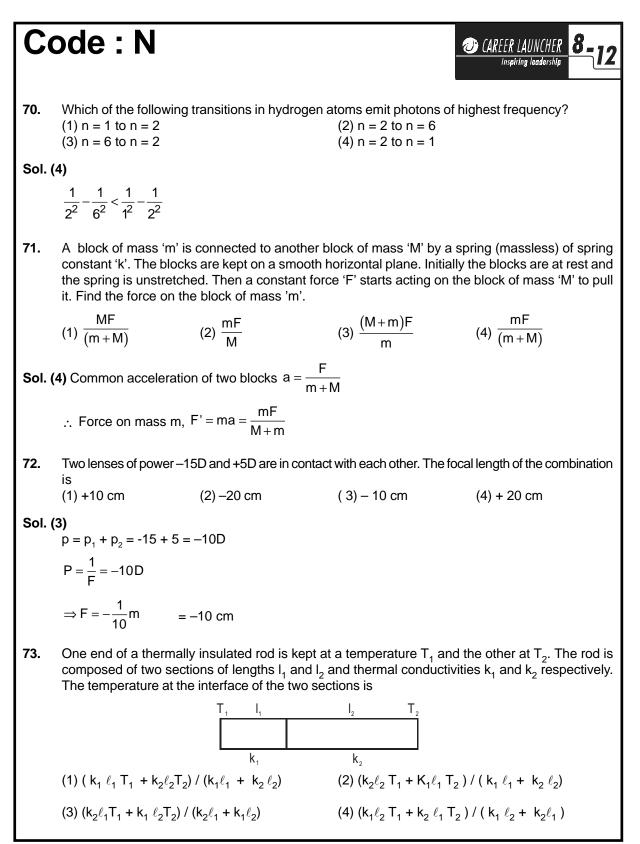
The electric field E at $x = 4 \mu m$ is given by

(1) 10/9 Volt/ μ m in the +ve x direction

- (2) 5/3 Volt/ μ m and in the –ve x direction
- (3) 5/3 Volt/ μ m and in the +ve x direction
- (4) 10/9 Volt/ μm and in the ve x direction

Sol. (1)

$$V(x) = \frac{20}{x^2 - 4} = \frac{20}{4} \left\{ \frac{1}{x - 2} - \frac{1}{x + 2} \right\}$$
$$= 5 \left\{ \frac{1}{x - 2} - \frac{1}{x + 2} \right\}$$
$$E(x) = -\frac{dV}{dx} = \frac{5}{(x - 2)^2} - \frac{5}{(x + 2)^2}$$
$$E(x = 4) = \left(\frac{5}{4} - \frac{5}{36} \right) \frac{V}{\mu m} = \frac{8 \times 5}{36} \frac{V}{\mu m}$$
$$= \frac{10}{9} \frac{V}{\mu m}$$





Sol. (4)

Let the temperature at the interface is T

$$\therefore \frac{T_1 - T}{\frac{l_1}{k_1 A}} = \frac{T - T_2}{\frac{l_2}{k_2 A}}$$
$$\Rightarrow T\left[\frac{k_1}{l_1} + \frac{k_2}{l_2}\right] = \frac{T_1 k_1}{l_1} + \frac{T_2 k_2}{l_2}$$
$$\Rightarrow T = \frac{k_1 l_2 T_1 + k_2 l_1 T_2}{k_1 l_2 + k_2 l_1}$$

74.A sound absorber attenuates the sound level by 20 dB. The intensity decreases by a factor of
(1) 100(2) 1000(3) 10000(4) 10

Sol. (1)

$$\beta = (10dB)\log\left(\frac{l}{l_0}\right)$$
$$\beta_2 - \beta_1 = 10\log\left(\frac{l_2}{l_1}\right)$$
$$\Rightarrow 20 = 10\log\left(\frac{l_2}{l_1}\right)$$
$$\Rightarrow \log\left(\frac{l_2}{l_1}\right) = 2$$
$$\Rightarrow \frac{l_2}{l_1} = 10^2 = 100$$

75. If C_p and C_v denote the specific heats of nitrogen per unit mass at constant pressure and constant volume respectively, then

(1) $C_p - C_v = 28 R$ (2) $C_p - C_v = R / 28$ (3) $C_p - C_v = R/14$ (4) $C_p - C_v = R$

Sol. (2)

 C_{P} and C_{V} are specific heats per unit mole, C_{P} − C_{V} = R $\Rightarrow M(C_{P} - C_{V}) = R$ $\Rightarrow C_{P} - C_{V} = \frac{R}{M} = \frac{R}{28}$

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79.	 A parallel plate condenser with a dielectric of dielectric constant K between the plate capacity C and is charged to a potential V volts. The dielectric slab is slowly remobetween the plates and then reinserted. The net work done by the system in this proc (1) zero (2) 1/2 (K - 1) CV² (3) CV² (K - 1) / K (4) (K - 1) CV² 							
Sol.	Sol. (1) work done (insert) = – work done (removed)							
80.	If g_E and g_m are the accelerations due to gravity on the surfaces of the earth and the moon respectively and if Millikan's oil drop experiment could be performed on the two surfaces, one will							
	find the ratio	electronic charge on the relectronic charge on the electronic charge on	noon earth					
	(1) $g_{M}^{}/g_{E}^{}$	(2) 1	(3) 0	(4) g _E / g _M				
Sol. (2) Charge is independent of gravity.								