

Mathematics
Class X
Past Year Paper - 2013

Time: 2½ hour

Total Marks: 80

1. Answer to this paper must be written on the paper provided separately.
2. You will NOT be allowed to write during the first 15 minutes. This time is to be spent in reading the question paper.
3. The time given at the head of this paper is the time allowed for writing the answers.
4. This question paper is divided into two Sections.
Attempt all questions from Section A and any four questions from Section B.
5. Intended marks for questions or parts of questions are given in brackets along the questions.
6. All working, including rough work, must be clearly shown and should be done on the same sheet as the rest of the answer. Omission of essential working will result in loss of marks.
7. Mathematical tables are provided.

SECTION - B (40 marks)

Q. 1

(a) Given $A = \begin{bmatrix} 2 & -6 \\ 2 & 0 \end{bmatrix}$, $B = \begin{bmatrix} -3 & 2 \\ 4 & 0 \end{bmatrix}$, $C = \begin{bmatrix} 4 & 0 \\ 0 & 2 \end{bmatrix}$

Find the matrix X such that $A + 2X = 2B + C$. (3)

(b) At what rate % p.a. will a sum of ₹ 4000 yield ₹ 1324 as compound interest in 3 years? (3)

(c) The median of the following observations
11, 12, 14, (x - 2), (x + 4), (x + 9), 32, 38, 47 arranged in ascending order is 24.
Find the value of x and hence find the mean. (4)

Q. 2

(a) What number must be added to each of the numbers 6, 15, 20 and 43 to make them proportional? (3)

(b) If (x - 2) is a factor of the expression $2x^3 + ax^2 + bx - 14$ and when the expression is divided by (x - 3), it leaves a remainder 52, find the values of a and b. (3)

- (c) Draw a histogram from the following frequency distribution and find the mode from the graph: (4)

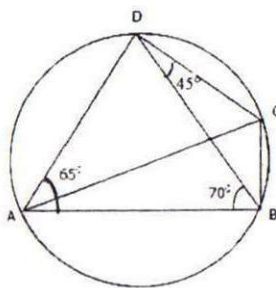
Class	0-5	5-10	10-15	15-20	20-25	25-30
Frequency	2	5	18	14	8	5

Q. 3

- (a) Without using tables evaluate:

$$3 \cos 80^\circ \cdot \operatorname{cosec} 10^\circ + 2 \sin 59^\circ \sec 31^\circ. \quad (3)$$

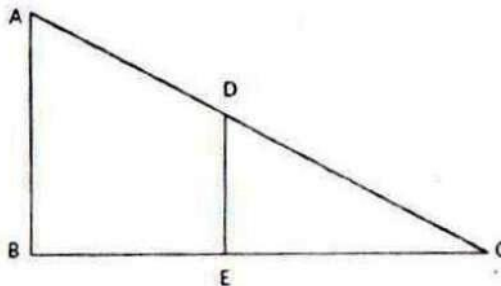
- (b) In the given figure, $\angle BAD = 65^\circ$
 $\angle ABD = 70^\circ$, $\angle BDC = 45^\circ$



- (i) Prove that AC is a diameter of the circle.
(ii) Find $\angle ACB$ (3)
- (c) AB is a diameter of a circle with centre C = (-2, 5). If A = (3, -7). Find
(i) the length of radius AC
(ii) the coordinates of B. (4)

Q. 4

- (a) Solve the following equation and calculate the answer correct to two decimal places:
 $x^2 - 5x - 10 = 0$.
- (b) In the given figure, AB and DE are perpendicular to BC.



- (i) Prove that $\triangle ABC \sim \triangle DEC$
(ii) If AB = 6 cm; DE = 4 cm and AC = 15 cm. Calculate CD.

- (iii) Find the ratio of area of $\triangle ABC$: area of $\triangle DEC$.
- (c) Using a graph paper, plot the points A(6,4) and B(0,4).
 (i) Reflect A and B in the origin to get the images A' and B'.
 (ii) Write the co-ordinates of A' and B'.
 (iii) State the geometrical name for the figure ABA' B'.
 (iv) Find its perimeter.

SECTION – B (40 marks)

Q. 5

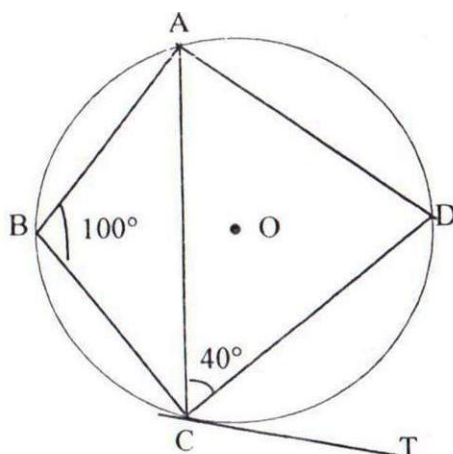
- (a) Solve the following inequation, write the solution set and represent it on the

$$\text{number line: } -\frac{x}{3} \leq \frac{x}{2} - 1 \frac{1}{3} < \frac{1}{6}, x \in \mathbb{R} \quad (3)$$

- (b) Mr. Britto deposits a certain sum of money each month in a Recurring Deposit Account of a bank. It the rate of interest is of 8% per annum and Mr. Britto gets ₹ 8088 from the bank after 3 years, find the value of his monthly instalment. (3)
- (c) Salman buys 50 shares of face value ₹ 100 available at ₹ 132.
 (i) What is his investment?
 (ii) If the dividend is 7.5%, what will be his annual income?
 (iii) If he wants to increase his annual income by ₹ 150, how many extra shares should he buy? (4)

Q. 6

- (a) Show that $\sqrt{\frac{1 - \cos A}{1 + \cos A}} = \frac{\sin A}{1 + \cos A}$. (3)
- (b) In the given circle with centre O, $\angle ABC = 100^\circ$, $\angle ACD = 40^\circ$ and CT is a tangent to the circle at C. Find $\angle ADC$ and $\angle DCT$. (3)



(c) Given below are the entries in a Saving Bank A/c pass book.

Date	Particulars	Withdrawals	Deposit	Balance
Feb 8	B/F	-	-	₹ 8500
Feb 18	To self	₹ 4000	-	
April 12	By cash	-	₹ 2230	
June 15	To self	₹ 5000	-	
July 8	By cash	-	₹ 6000	

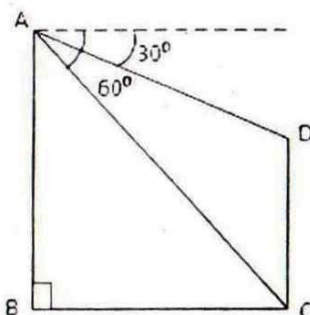
Calculate the interest for six months from February to July at 6% p.a. (4)

Q.7

(a) In $\triangle ABC$, $A(3,5)$, $B(7,8)$ and $C(1,-10)$. Find the equation of the median through A. (3)

(b) A shopkeeper sells an article at the listed price of ₹ 1500 and the rate of VAT is 12% at each stage of sale. If the shopkeeper pays a VAT of ₹ 36 to the Government, what was the price, inclusive to TAX, at which the shopkeeper purchased the article from the wholesaler? (3)

(c) In the figure given, from the top of a building $AB = 60$ m high, the angles of depression of the top and bottom of a vertical lamp post CD are observed to 30° and 60° respectively. Find:



(i) The horizontal distance between AB and CD.

(ii) The height of the lamp post.

(4)

Q. 8

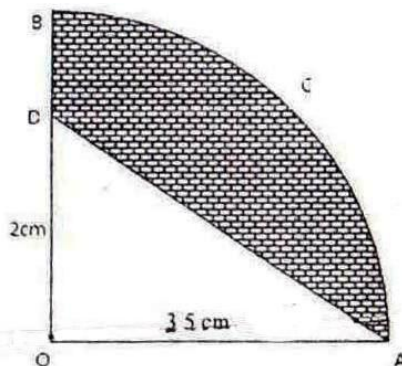
(a) Find x and y if $\begin{bmatrix} x & 3x \\ y & 4y \end{bmatrix} \begin{bmatrix} 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 5 \\ 12 \end{bmatrix}$. (3)

(b) A solid sphere of radius 15 cm is melted and recast into solid right circular cones of radius 2.5 cm and height 8 cm. Calculate the number of cones recast. (3)

(c) Without solving the following quadratic equation, find the value of 'p' for which the given equation has real and equal roots:
 $x^2 + (p - 3)x + p = 0$. (4)

Q. 9

(a) In the figure alongside, OAB is a quadrant of a circle. The radius OA = 3.5 cm and OD = 2 cm. Calculate the area of the shaded portion. (Take $\pi = \frac{22}{7}$). (3)



(b) A box contains some black balls and 30 white balls. If the probability of drawing a black ball is two-fifths of a white ball, find the number of black balls in the box. (3)

(c) Find the mean of the following distribution by step deviation method: (4)

Class interval	20-30	30-40	40-50	50-60	60-70	70-80
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Frequency	10	6	8	12	5	9
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Q. 10

(a) Using a ruler and compasses only:

(i) Construct a triangle ABC with the following data:

AB = 3.5 cm, BC = 6 cm and $\angle ABC = 120^\circ$

(ii) In the same diagram, draw a circle with BC as diameter. Find a point P on the circumference of the circle which is equidistant from AB and BC.

(iii) Measure $\angle BCP$.

(4)

(b) The marks obtained by 120 students in a test are given below:

Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80	80-90	90-100
No of students	5	9	16	22	26	18	11	6	4	3

Draw an ogive for the given distribution on a graph sheet.

Use suitable scale for ogive to estimate the following:

(i) The median.

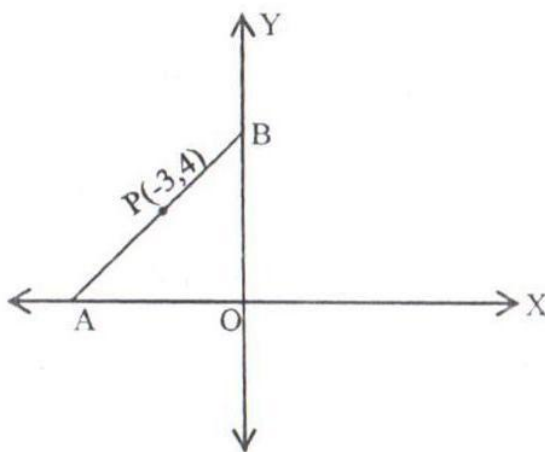
(ii) The number of students who obtained more than 75% marks in the test.

(iii) The number of students who did not pass the test if minimum marks required to pass is 40.

(6)

Q. 11

(a) In the figure given below, the line segment AB meets X-axis at A and Y-axis at B. The point P(-3,4) on AB divides it in the ratio 2:3. Find the coordinates of A and B. (3)



(b) Using the properties of proportion, solve for x, given

$$\frac{x^4 + 1}{2x^2} = \frac{17}{8}$$

(3)

(c) A shopkeeper purchases a certain number of books for ₹ 960. If the cost per book was ₹ 8 less, the number of books that could be purchased for ₹ 960 would be 4

more. Write an equation, taking the original cost of each book to be ₹ x , and solve it to find the original cost of the books. (3)