



ENGINEERING & MANAGEMENT EXAMINATIONS, JUNE - 2009
FORMAL LANGUAGE & AUTOMATA THEORY
SEMESTER - 4

Time : 3 Hours]

[Full Marks : 70

GROUP - A**(Multiple Choice Type Questions)**

1. Choose the correct alternatives of the following :

10 × 1 = 10

i) $L = \{ a^n b^n c^n, \text{ where } n \in \mathbb{N} \}$ is

- a) regular
- b) context free but not regular
- c) context sensitive but not context free
- d) none of these.

ii) Which is true of the following ?

- a) Merger graph is a directed graph
- b) Compatible graph is a directed graph
- c) Both are directed
- d) None of these.

iii) The intersection of a CFL and regular language is

- a) context free
- b) regular but not context free
- c) neither context free nor regular
- d) both regular and context free.

iv) $a^* (a + b)^*$ is equivalent to

- a) $a^* + b^*$
- b) $(ab)^*$
- c) $a^* b^*$
- d) None of these.



GROUP - B

(Short Answer Type Questions)

Answer any three of the following.

3 × 5 = 15

2. In response to an unknown input sequence, the machine given below produces the output sequence 1110000010. Find the input sequence to the machine if it is known that its initial state is A and final state is F. 5

PS	NS, z	
	x = 0	x = 1
A	B, 1	C, 0
B	D, 1	B, 1
C	E, 1	B, 0
D	A, 0	E, 0
E	F, 0	D, 1
F	D, 0	A, 1

3. What is the basic difference between Mealy machine and Moore machine? Construct a Mealy machine which is equivalent to the Moore machine given below : 2 + 3

PS	NS		z
	x = 0	x = 1	
q ₀	q ₁	q ₂	1
q ₁	q ₃	q ₂	0
q ₂	q ₂	q ₁	1
q ₃	q ₀	q ₃	1

4. Show that $L = \{ a^p \mid p \text{ is prime} \}$ is not regular. 5



5. Let G be the grammar $S \rightarrow aB/ba$, $A \rightarrow a/aS/bAA$, $B \rightarrow b/bS/aBB$. For the string $aaabbabbba$ find a. 2 + 2 + 1

- a) leftmost derivation
- b) rightmost derivation
- c) parse tree.

6. Is the following machine information lossless? If yes, find the order of losslessness. 4 + 1

PS	NS, z	
	x = 0	x = 1
A	A, 0	B, 0
B	C, 0	D, 0
C	D, 1	C, 1
D	B, 1	A, 1

GROUP - C

(Long Answer Type Questions)

Answer any three of the following.

3 × 15 = 45

7. a) State the difference between DFA and NFA. 2
- b) Design an NFA which accepts set of all binary strings containing 1100 or 1010 as substrings. 3
- c) What is regular language? 2
- d) Find regular expressions over $\Sigma = \{ a, b \}$ for the languages defined as follows :
 - i) $L1 = \{ a^m b^m : m > 0 \}$
 - ii) $L2 = \{ a^{2n} b^{2m+1} \mid n \geq 0, m \geq 0 \}$
 - iii) $L3 = \{ b^m a b^n : m > 0, n > 0 \}$ 1 + 1 + 1



- c) Minimize the following machine by partitioning the distinguishable states : 7

Present State	i/p = 0		i/p = 1	
	Next State	o/p	Next State	o/p
A	E	0	D	1
B	F	0	D	0
C	E	0	B	1
D	F	0	B	0
E	G	0	F	1
F	B	0	C	0
G	C	1	H	0
H	A	1	G	0

- d) Give definition of lossy and lossless machine.

$2 \times 1\frac{1}{2}$

10. Draw the merger graph, merger table, compatibility graph and then minimize the following machine : $4 + 4 + 3 + 4$

Present State	Next State, o/p		Next State, o/p	
	i/p = 0	i/p = 1	i/p = 2	i/p = 3
A	--	C, 1	E, 1	B, 1
B	E, 0	--	--	--
C	F, 0	F, 1	--	-, 1
D	--	--	B, 1	--
E	--	F, 0	A, 0	D, -
F	C, -	--	B, 0	C, 1

11. a) Convert grammars to Greibach Normal Form (GNF).

i) $S \rightarrow aSa \mid aSb \mid \epsilon$

ii) $S \rightarrow aSB \mid aSbS \mid \epsilon$.

- b) Find a reduced grammar equivalent to the grammar $S \rightarrow aAa, A \rightarrow bBB, B \rightarrow ab, C \rightarrow aB$.

- c) Explain the concept of 2-way finite automata.

$5 + 6 + 4$

END