

TC-21

Statistical Techniques (Paper-V)

Time : 3 Hours]

[Total Marks : 70

Marking : (1) සෑම ප්‍රශ්නයක් සඳහාම «සලකුණු» දීමට ඉඩ ඇත
 (2) සෑම ප්‍රශ්නයක් සඳහාම ඉන්ද්‍රියයක් සඳහාම වෙනම පිටපත් කළ කොටස් දීමට ඉඩ ඇත

1. (a) සමස්තයක සාමාන්‍යය සහ ව්‍යුහය සඳහා වන විචලනය සඳහා වන සූත්‍ර දෙකක් සඳහා වන සාධාරණීකරණය සඳහා 7
- (b) «සමස්තයක සාමාන්‍යය සහ ව්‍යුහය සඳහා වන විචලනය සඳහා වන සූත්‍ර දෙකක් සඳහා වන සාධාරණීකරණය සඳහා 7

$$V(\bar{y}) = \frac{N-n}{N} \frac{S^2}{n}$$

විචලනය

1. (a) සමස්තයක සාමාන්‍යය සහ ව්‍යුහය සඳහා වන විචලනය සඳහා වන සූත්‍ර දෙකක් සඳහා වන සාධාරණීකරණය සඳහා 7

$$V(\bar{y}_{st}) = \frac{1}{N^2} \sum_{h=1}^l N_h(N_h - n_h) \frac{S_h^2}{n_h}$$

- (b) 0, 1, 5, 8, 12, 15 යනු 19 යුගල සඳහා වන සාමාන්‍යය සහ ව්‍යුහය සඳහා වන විචලනය සඳහා වන සූත්‍ර දෙකක් සඳහා වන සාධාරණීකරණය සඳහා 7

(1) $E(\bar{y}) = \bar{Y}$

(2) $E(s^2) = S^2$

(3) $V(\bar{y}) = \left(\frac{1}{n} - \frac{1}{N}\right) S^2$

2. (a) සමස්තයක සාමාන්‍යය සහ ව්‍යුහය සඳහා වන විචලනය සඳහා වන සූත්‍ර දෙකක් සඳහා වන සාධාරණීකරණය සඳහා 7

(1) Wf_{st}

(2) පොදු Wf_{st}

(3) සමස්තයක සාමාන්‍යය සහ ව්‍යුහය සඳහා වන විචලනය සඳහා වන සූත්‍ර දෙකක් සඳහා වන සාධාරණීකරණය සඳහා 7

- (b) Lke [lukk Mkn8/4 ykPksLkLkk «S okiVLke heikúke {pðku :
Lke [lúke phikkúku ykÁeLk

7

$$Z = 5x_1 + 3x_2 \quad \text{Lku } \{n\}k\{ \text{ çkLkkòku}$$

S. to

$$\begin{aligned} x_1 + 2x_2 &\leq 52 \\ 2x_1 + 3x_2 &= 84 \\ x_1, x_2 &\geq 0 \end{aligned}$$

yúðk

2. (a) íf yk=ú þp Mkn8/4 ykPksLkLkk «S {kt íku fE heiku WÁkPkkøke AP

7

- (b) Lke [lukk Mkn8/4 ykPksLkLkk «S Lkku íf {pðe íkúku MkeBÁk=úLke heikúke Wfú= {pðku
Lke [lúke phikkúku ykÁeLk

7

$$Z = 2x_1 + 2x_2 \quad \text{Lku LPkkík\{ çkLkkòku :}$$

S.to

$$\begin{aligned} 2x_1 + 4x_2 &= 1 \\ x_1 + 2x_2 &= 1 \\ 2x_1 + x_2 &= 1 \\ x_1, x_2 &\geq 0 \end{aligned}$$

3. (a) yf rLkÉþuk ÞksLkk rðMíkkhúke M{òðku

7

- (b) Lke [lúke rí-rLkÉþuk ÞksLkkLke M{sáke ykÁkku

7

$N = 2000, n_1 = 50, c_1 = 0, n_2 = 100, C_2 = 2$
òu $p' = 0.005$, nkþ íkku ÁkkþMkLk rðíkhýLkku WÁkPkkøk fheLku

(1) MðefjrikLke M8/4kðLkk (P_a)

(2) AOQ {pðkuþþkt

ÁkkþMkLk rðíkhýLke Mkt[þe M8/4kðLkkýku Lke [u {sçk Au :

	0	1	2
0.25	0.779	0.974	0.998
0.50	0.607	0.910	0.986

yúðk

3. (a) rí-rLkÉþuk ÞksLkk {kxu Lke [lukk ÁkÉku M{òðku

8

(1) AOQ (2) AOQL (3) ASN (4) ATI

- (b) 2200 ðMíknykúkk yf sákkúke 225 ðMíknykúkk yf rLkÉþo ðkk{kt ykðu Au òu sákk{kt 14 yúðk
íkkúke ykÁe 3/4{eðkæe ðMíknyku nkþ íkku sákkLkku Mðefkh fhðk{kt ykðu Au Lkn^a íkku íkkúku yMðefkh
fhðk{kt ykðu Au íkku OC, ATI yLku AOQ ðçku Ékku yLku AOQL Lke f^a{ík Áký {pðku

6

4. (a) yif-öknyÄ{eP ðökefhýLke heík rðMíkkhúke Mk{òðku 7

(b) Lke [Lke ÷axLk [kñMk PksLkkLkv Äkj]k-hý fhku 7

A 12	C 19	B 10	D 8
C 18	B 12	D 6	A 7
B 22	D 10	A 5	C 21
D 12	A 7	C 27	B 17

yúðk

4. (a) rí-öknyÄ{eP વગલકરણની heík rðMíkkhúke Mk{òðku 7

(b) Lke [Lke MkÄkyó PááA PksLkkLkv Äkj]k-hý fhku : 7

{kðsíkku	WÄkòu				
	1	2	3	4	5
A	55	49	42	21	52
B	61	112	30	89	63
C	42	97	81	95	92
D	169	137	169	85	154

5. (a) sÚkk rLkPky yx÷u pP íkukk ÷k¼ku yLku økn÷k¼ku ðýðku EOQ Lke Òpk'Pk ykÄku 7

(b) yif fÄkLke yif ðMíkkke ðkSkf {kñk 9000 yif{ku Au Èhf yif{Lke WíÄkkÈLk ¶{ík 3.10 Au ðhÈe {fðkLke ¶{ík 3. 8 Au yLku sÚkk Äkhý ¼[o yif{ ÈeX 1 3[ayì Au íku{s ðhÈe {æððkLke ¶{ík 3.18 Au íku Eüík{ ¼heÈ sÚkkku {æðku fæ- Lpíkík{ ¼[o pñ úkpu íku Äký {æðku 7

yúðk

5. (a) sÚkk rLkPkyLke Mk{Mpk Mkúku Mkf÷kPæ-k rðrðÄ ¼[koyku Mk{òðku 7

(b) næke fÄkLke ðkSkf 50,000 yif{ku yif ðMíkkk ðkÄkhu Au sLke WíÄkkÈLk fª{ík 3.20 yif{ ÈeX Au ðhÈe {fðkLkku ¼[o 3.100 Au yLku sÚkk Äkhý ¼[o sÚkkLke ¶{íLkk 15% Au EOQ pkÄku 7

TC-21**Statistical Techniques (Paper-V)****Time : 3 Hours]****[Total Marks : 70**

- Instructions :** (1) Figures to the right indicate marks of each question.
 (2) Use of simple calculator and statistical tables is allowed.

1. (a) What is sampling? Why do you need sampling? What are the characteristics of a good sample? **7**
 (b) In usual notations prove that for SRSWOR, **7**

OR

1. (a) For stratified random sampling prove that **7**

$$V(\bar{y}_{st}) = \frac{1}{N^2} \sum_{h=1}^l N_h (N_h - n_h) \frac{S_h^2}{n_h} \text{ in usual notations } V(\bar{y}) = \frac{N-n}{N} \frac{S^2}{n}$$

- (b) If 1, 5, 8, 12, 15 and 19 are the observations of a population, form all possible samples of size “2” units without replacement and verify the following results : **7**

$$(1) E(\bar{y}) = \bar{Y}$$

$$(2) E(s^2) = S^2$$

$$(3) V(\bar{y}) = \left(\frac{1}{n} - \frac{1}{N} \right) S^2$$

2. (a) Define a linear programming problem in its general form. Also define **7**
 (1) a solution
 (2) a feasible solution
 (3) an optimum solution for such a problem.

- (b) Solve the following linear programming problem by graphical method : 7

$$\begin{aligned} \text{Maximize :} \quad & Z = 5x_1 + 3x_2 \\ \text{S. to} \quad & x_1 + 2x_2 \leq 52 \\ & 2x_1 + 3x_2 \leq 84 \\ & x_1, x_2 \geq 0 \end{aligned}$$

OR

2. (a) What is Duality? How is it useful in solving a Linear Programming problem ? 7

- (b) Convert the following Linear Programming problem into its dual and then solve it by Simplex method : 7

$$\begin{aligned} \text{Minimize :} \quad & Z = 2x_1 + 2x_2 \\ \text{S. to} \quad & 2x_1 + 4x_2 \leq 1 \\ & x_1 + 2x_2 \leq 1 \\ & 2x_1 + x_2 \leq 1 \\ & x_1, x_2 \geq 0 \end{aligned}$$

3. (a) Explain in detail Single Sampling plan. 7

- (b) Interpret the following Double Sampling plan : 7

$$N = 2000, n_1 = 50, c_1 = 0, n_2 = 100, C_2 = 2$$

If $p' = 0.005$, then using Poisson distribution, calculate :

(1) Probability of acceptance (P_a)

(2) AOQ

Cumulative Probability of Poisson distributions :

	0	1	2
0.25	0.779	0.974	0.998
0.50	0.607	0.910	0.986

OR

3. (a) Explain the following terms for a Double Sampling plan : 8

(1) AOQ (2) AOQL (3) ASN (4) ATI

- (b) From a lot of 2200 items, a sample of size 225 is taken. If it contains 14 or less defectives, the lot is accepted, otherwise it is rejected. Plot the OC, ATI and AOQ curves. Also obtain the value of AOQL. 6

4. (a) Explain in detail the technique of One-way classification. 7
 (b) Analyse the following Latin Square Design. 7

A 12	C 19	B 10	D 8
C 18	B 12	D 6	A 7
B 22	D 10	A 5	C 21
D 12	A 7	C 27	B 17

OR

4. (a) Explain in detail two-way classification. 7
 (b) Analyse the following completely Randomised Design : 7

Treatments	Yields				
	1	2	3	4	5
A	55	49	42	21	52
B	61	112	30	89	63
C	42	97	81	95	92
D	169	137	169	85	154

5. (a) What is inventory control? What are its advantages and disadvantages? 7
 Define EOQ.
 (b) A product of a company has an annual demand of 9000 units. The unit manufacturing cost is Rs.10. The cost of placing an order is Rs.8 and inventory carrying cost is Re.1 per unit, whereas cost of receiving an order from outside is Rs.18. Find optimum purchase quantity. What will be the total minimum cost? 7

OR

5. (a) Explain in detail the various costs associated with an inventory control problem. 7
 (b) A Harshal company uses annually 50,000 units whose cost price is Rs.20 per unit. Cost of placing an order is Rs.100 and inventory carrying costs are 15% of the value per unit. Find EOQ. 7