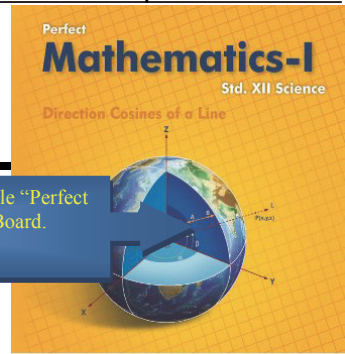


BOARD QUESTION PAPER: MARCH 2014

MATHEMATICS – I (12th Sci., HSC, Maharashtra)

**Note:**

- All questions are compulsory.
- Figures to the right indicate full marks.
- Graph of L.P.P. should be drawn on graph paper only.
- Answers to both sections must be written in one answer book.
- Answer to every new question must be written on a new page.

This question paper is an extract from our title "Perfect Mathematics - I" for Std. XII Science, MH Board. Visit www.targetpublications.org to know more

SECTION – I

Q.1. (A) Select and write the correct answer from the given alternatives in each of the following:

(6) [12]

- Which of the following represents direction cosines of the line?

(A) $0, \frac{1}{\sqrt{2}}, \frac{1}{2}$	(B) $0, \frac{-\sqrt{3}}{2}, \frac{1}{\sqrt{2}}$
(C) $0, \frac{\sqrt{3}}{2}, \frac{1}{2}$	(D) $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$
- $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ and $A(\text{adj } A) = KI$, then the value of 'K' is _____

(A) 2	(B) -2
(C) 10	(D) -10
- The general solution of the trigonometric equation $\tan^2\theta = 1$ is _____

(A) $\theta = n\pi \pm \frac{\pi}{3}, n \in Z$	(B) $\theta = n\pi \pm \frac{\pi}{6}, n \in Z$
(C) $\theta = n\pi \pm \frac{\pi}{4}, n \in Z$	(D) $\theta = n\pi, n \in Z$

(B) Attempt any THREE of the following:

(6)

- If $\vec{a}, \vec{b}, \vec{c}$ are the position vectors of the points A, B, C respectively and $2\vec{a} + 3\vec{b} - 5\vec{c} = \vec{0}$, then find the ratio in which the point C divides the line segment AB.
- The cartesian equation of a line is $\frac{x-6}{2} = \frac{y+4}{7} = \frac{z-5}{3}$, find its vector equation.
- Equation of a plane is $\vec{r} \cdot (3\hat{i} - 4\hat{j} + 12\hat{k}) = 8$. Find the length of the perpendicular from the origin to the plane.
- Find the acute angle between the lines whose direction ratios are 5, 12, -13 and 3, -4, 5.
- Write the dual of the following statements:
 - $(p \vee q) \wedge T$

(2) Madhuri has curly hair and brown eyes.

Q.2. (A) Attempt any TWO of the following: (6)[14]

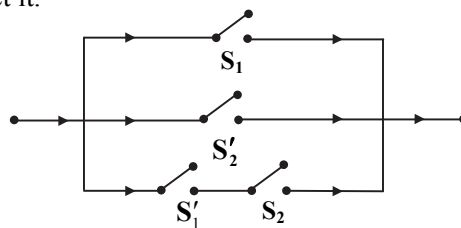
- i. If the lines $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$ and $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1}$ intersect, then find the value of k.
- ii. Prove that three vectors \bar{a} , \bar{b} and \bar{c} are coplanar, if and only if, there exists a non-zero linear combination $x\bar{a} + y\bar{b} + z\bar{c} = \bar{0}$.
- iii. Using truth table prove that $\sim p \wedge q \equiv (p \vee q) \wedge \sim p$

(B) Attempt any TWO of the following: (8)

- i. In any ΔABC , with usual notations, prove that $b^2 = c^2 + a^2 - 2ca \cos B$.
- ii. Show that the equation $x^2 - 6xy + 5y^2 + 10x - 14y + 9 = 0$ represents a pair of lines. Find the acute angle between them. Also find the point of intersection of the lines.
- iii. Express the following equations in the matrix form and solve them by the method of reduction:
 $2x - y + z = 1, x + 2y + 3z = 8, 3x + y - 4z = 1$

Q.3. (A) Attempt any TWO of the following: (6)[14]

- i. Prove that a homogeneous equation of degree two in x and y (i.e., $ax^2 + 2hxy + by^2 = 0$), represents a pair of lines through the origin if $h^2 - ab \geq 0$.
- ii. Find the symbolic form of the following switching circuit, construct its switching table and interpret it.



- iii. If A, B, C, D are (1, 1, 1), (2, 1, 3), (3, 2, 2), (3, 3, 4) respectively, then find the volume of the parallelepiped with AB, AC and AD as the concurrent edges.

(B) Attempt any TWO of the following: (8)

- i. Find the equation of the plane passing through the line of intersection of the planes $2x - y + z = 3, 4x - 3y + 5z + 9 = 0$ and parallel to the line $\frac{x+1}{2} = \frac{y+3}{4} = \frac{z-3}{5}$.
- ii. Minimize: $Z = 6x + 4y$
 Subject to: $3x + 2y \geq 12,$
 $x + y \geq 5,$
 $0 \leq x \leq 4,$
 $0 \leq y \leq 4.$
- iii. Show that: $\cos^{-1}\left(\frac{4}{5}\right) + \cos^{-1}\left(\frac{12}{13}\right) = \cos^{-1}\left(\frac{33}{65}\right).$