## Quick Quant Pocket Guide Pocket mein Rocket

A) A MATHEMATICAL EXPRESSION MAY, SOMETIMES,INVOLVES THE APPLICATION OF. ALGEBRAIC FORMULAE. THESE FORMULAE ARE LISTED BELOW:

1) $(\mathrm{a}+\mathrm{b})^{2}=a^{2}+2 \mathrm{ab}+b^{2}$
2) $(a-b)^{2}=a^{2}-2 \mathrm{ab}+b^{2}$
3) $(a+b)^{3}=a^{3}+3 a^{2} \mathrm{~b}+3 \mathrm{a} b^{2}+b^{3}=a^{3}+b^{3}+3 \mathrm{ab}(\mathrm{a}+\mathrm{b})$
4) $(a-b)^{3}=a^{3}-3 a^{2} \mathrm{~b}+3 \mathrm{a}^{2}-b^{3}=a^{3}-b^{3}-3 \mathrm{ab}(\mathrm{a}-\mathrm{b})$
5) $\left(a^{2}-b^{2}\right)=(a+b)(a-b)$
6) $\left(a^{3}+b^{3}\right)=(\mathrm{a}+\mathrm{b})\left(a^{2}-\mathrm{ab}+b^{2}\right)$
7) $\left(a^{3}-b^{3}\right)=(\mathrm{a}-\mathrm{b})\left(a^{2}+\mathrm{ab}+b^{2}\right)$
B) A MATHEMATICAL EXPRESSION MAY, SOMETIMES,INVOLVES THE RULES OF DISTRIBUTION. THESE ARE LISTED BELOW:
8) $a(b+c)=a b+a c$
9) $a(b-c)=a b-b c$
10) $(a+b)(c+d)=a c+b c+b d$
11) $\frac{a+b+c}{d}=\frac{a}{d}+\frac{b}{d}+\frac{c}{d}$
C) SQUARES AND CUBES:

| No. | Square | Cube |
| :--- | :---: | :---: |
| 1 | 1 | 1 |
| 2 | 4 | 8 |
| 3 | 9 | 27 |
| 4 | 16 | 64 |
| 5 | 25 | 125 |
| 6 | 36 | 216 |
| 7 | 49 | 343 |
| 8 | 64 | 512 |
| 9 | 81 | 729 |
| 10 | 100 | 1000 |
| 11 | 121 | 1331 |
| 12 | 144 | 1728 |
| 13 | 169 | 2197 |
| 14 | 196 | 2744 |
| 15 | 225 | 3375 |


| No. | Square |
| :---: | :---: |
| 16 | 256 |
| 17 | 289 |
| 18 | 324 |
| 19 | 361 |
| 20 | 400 |
| 21 | 441 |
| 22 | 484 |
| 23 | 529 |
| 24 | 576 |
| 25 | 625 |
| 26 | 676 |
| 27 | 729 |
| 28 | 784 |
| 29 | 841 |
| 30 | 900 |

D) TABLES (from 1 to 15):

| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 | 26 | 28 | 30 |
| 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 | 33 | 36 | 39 | 42 | 45 |
| 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 | 44 | 48 | 52 | 56 | 60 |
| 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 |
| 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 | 60 | 66 | 72 | 78 | 84 | 90 |
| 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 | 70 | 77 | 84 | 91 | 98 | 105 |
| 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 | 88 | 96 | 104 | 112 | 120 |
| 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 | 90 | 99 | 108 | 117 | 126 | 135 |
| 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 | 110 | 120 | 130 | 140 | 150 |

TABLES (from 16 to 30) :

| $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | $\mathbf{2 5}$ | $\mathbf{2 6}$ | $\mathbf{2 7}$ | $\mathbf{2 8}$ | $\mathbf{2 9}$ | $\mathbf{3 0}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 32 | 34 | 36 | 38 | 40 | 42 | 44 | 46 | 48 | 50 | 52 | 54 | 56 | 58 | 60 |
| 48 | 51 | 54 | 57 | 60 | 63 | 66 | 69 | 72 | 75 | 78 | 81 | 84 | 87 | 90 |
| 64 | 68 | 72 | 76 | 80 | 84 | 88 | 92 | 96 | 100 | 104 | 108 | 112 | 116 | 120 |
| 80 | 85 | 90 | 95 | 100 | 105 | 110 | 115 | 120 | 125 | 130 | 135 | 140 | 145 | 150 |
| 96 | 102 | 108 | 114 | 120 | 126 | 132 | 138 | 144 | 150 | 156 | 162 | 168 | 174 | 180 |
| 112 | 119 | 126 | 133 | 140 | 147 | 154 | 161 | 168 | 175 | 182 | 189 | 196 | 203 | 210 |
| 128 | 136 | 144 | 152 | 160 | 168 | 176 | 184 | 192 | 200 | 208 | 216 | 224 | 232 | 240 |
| 144 | 153 | 162 | 171 | 180 | 189 | 198 | 207 | 216 | 225 | 234 | 243 | 252 | 261 | 270 |
| 160 | 170 | 180 | 190 | 200 | 210 | 220 | 230 | 240 | 250 | 260 | 270 | 280 | 290 | 300 |

E) COMMONLY-USED CONVERSION OF PERCENTAGES TO FRACTIONS ARE GIVEN BELOW :
(A) Dividing $\mathbf{1 0 0 \%}$ into equal 10 equal parts.

1) $10 \%=\frac{1}{10}=0.1$
2) $20 \%=\frac{1}{5}=0.2$
3) $30 \%=\frac{3}{10}=0.3$
4) $40 \%=\frac{2}{5}=0.4$
5) $50 \%=\frac{1}{2}=0.5$
6) $60 \%=\frac{3}{5}=0.6$
7) $70 \%=\frac{7}{10}=0.7$
8) $80 \%=\frac{4}{5}=0.8$
9) $90 \%=\frac{9}{10}=0.9$
10) $100 \%=1.0$

Sometimes, $5 \%=\frac{5}{100}=\frac{1}{20}=0.05$ is also useful to remember
(B) Dividing $100 \%$ into 6 equal parts.

1) $16 \frac{2}{3} \%=\frac{1}{6}$
2) $33 \frac{1}{3} \%=\frac{2}{6}=\frac{1}{3}$
3) $66 \frac{2}{3} \%=\frac{4}{6}=\frac{2}{3}$
4) $83 \frac{1}{2} \%=\frac{5}{6}$
5) $100 \frac{6}{6} \%=1$

Sometimes, $8 \frac{1}{3} \%=\frac{1}{12}$ is our useful to remember.
(C) Dividing $100 \%$ into 8 equal parts.

1) $12 \frac{1}{2} \%=\frac{1}{8}$
2) $25 \%=\frac{2}{8}=\frac{1}{4}$
3) $37 \frac{1}{2} \%=\frac{3}{8}$
4) $50 \%=\frac{4}{8}=\frac{1}{2}$
5) $62 \frac{1}{2} \%=\frac{5}{8}$
6) $75 \%=\frac{6}{8}=\frac{3}{4}$
7) $87 \frac{1}{2} \%=\frac{7}{8}$
8) $100 \%=\frac{8}{8}=1$

Sometimes, $6 \frac{1}{4} \%=\frac{1}{16}$ is also useful to remember.
(D) Non-conventional percentages

1) $11 \frac{1}{9} \%=\frac{1}{9}$
2) $9 \frac{1}{11} \%=\frac{1}{11}$
F) MULTIPLICATION COMMONLY-USED IN COMPETITIVE EXAMINATIONS :
3) $16 \times 12=192$
4) $\mathbf{1 5} \times \mathbf{2 5}=\mathbf{3 7 5}$
5) $\mathbf{1 6} \times \mathbf{2 5}=\mathbf{4 0 0}$
6) $3 \times 37=111$ *

* : Note that $3 \times 37=111 \rightarrow 111 \div 37=3$. Thus, a question based on this relationship may get framed as, say,
$888 \div 37+1=\sqrt{?}$
here, one must be able to perform the division ( $888 \div 37$ ) as equal to $3 \times \mathbf{8 = 2 4}$,
Because $888=111 \times 8$ and $111 \div 37=3$.

Thus, the apparently strange(unkown) numbers become friendly (known ones) and the above equation can be solved as:
$\sqrt{?}=24+1=25 . \therefore ?=25=625$.

## G) FRACTION - ASCENDING/DESCENDING ORDER :

A given set of fractions can be arranged in ascending / descending order ( by value) by application of any of the following methods :
(A) Calculate the decimal value of each and compare.
(B) Make the base equal and compare the numerators.
(C) arrange the given fractions in same order ( by judgement) and compare any two of them by cross-multiplication. The same relationship then holds good for the remaining fractions also.

In competitive examinations, method (C) above gives the answer fast while method $(A)$ is the longest ,time wise.

## Illustrative Examples :

1. Write the following fractions in ascending order.

$$
\frac{13}{19}, \frac{25}{31}, \frac{31}{37}, \frac{19}{25}, \frac{7}{13}
$$

Here, instead of calculating the decimal values of each fractions, we observe that there is some order in the above set. Observe that the difference between the numerator and the denominator numbers is constant(6). We therefore, write these fractions as follows :

$$
\frac{7}{13}, \frac{13}{19}, \frac{19}{25}, \frac{25}{31}, \frac{31}{37}
$$

Now, compare any two (consecutive) fraction (say, $\frac{7}{13}, \frac{13}{19}$ ) by cross-multiplication.
$7 * 19=133$ and $13 * 13=169$

Since 133 is less then 169 , we have ,

$$
\frac{7}{13}<\frac{13}{19} \quad \text { same relationship will now hold for the remaining fraction as }
$$

well.

Thus, $\quad \frac{7}{13}<\frac{13}{19}<\frac{19}{25}<\frac{25}{31}<\frac{31}{37}$
(Note that we have not calculated the individual values of the fractions, but have judged the relationship between the fractions).
2. Which of the following fractions is the largest ?
(3/7), (13/17), (15/19), (23/27), (29/33)

## 

Here, observe that the difference between the numerator and denominator of each fraction is the same(4). In such cases, the highest value of the fraction would be for the one which has bigger numbers in Numerator \& Denominator. Thus, in this example, the value of the fraction (29/33) would be the largest.

## H) UNITS OF MEASUREMENT AND CONVERSION FACTORS :

1. Majority of the units can be visualised from the following :
a) mili

* d) meter/litre/gram
b) centi
e) deca
c) deci
f) hecto
g) kilo
* The three terms meter/litre/gram denote the unit of measurement of distance, volume and weight respectively.

The table can now be read as follows :

1) For the use of units of distance : millimetre, centimetre, decimetre, meter, decametre, hectometre,kilometre.
2) for the use of the units of volume : militre, centilitre, decilitre,litre,decalitre,hectolitre,kilolitre
3) for the use of units of weight : milligram, centigram, centigram, decigram, gram, decagram, hectogram, kilogram.

Each higher step is obtained by multiplying the earlier (immediately preceding) one by 10 . Thus, 1Centimeter $=10$ milimeter, 1 litre $=10 \times 10 \times 10=1000$ mililitres, 1 kilogram = $10 \times 10 \times 10=1000$ grams, 1 kilogram $=10 \times 10 \times 10 \times 10 \times 10 \times 10=1,000,000$ miligrams, etc.
2.Apart from these, various other units can be listed ( alongwith their conversion factors) as follows :

1) 1 foot $=12$ inches $=30.48$ milimetres.
2) 1 inch $=24.5$ milimetres $=2.54$ centimetres.
3) 1 fathom $=6$ feet.
4) 1 mile $=900$ fathoms $=8$ furlongs $=1.609$ kilometres.
5) 1 yard = 3 feet.
6) 1 nautical mile $=1.852 \mathrm{kms}$. used for navigation.
7) 1 acre $=4,000$ square metres $=40$ gunthas $=43,560$ sq.ft.
8) 1 hectare $=2.5$ acre = 10,000 sq.metres.
9) 1 quintal $=100$ kilograms..
10) 1 metric ton $=1,000$ kilograms.
11) 1 kilogram = 2.204 pounds.
12) 1 gallon $=4.54609$ litres.
13) 1 hour $=60$ minutes $=3,600$ seconds ( 1 minute $=60$ seconds).
14) 1 degree $=12$ inches $=60$ miutes $=3,600$ seconds $\ldots .$. angular measurement.

## I) TEST OF DIVISIBILITY :

The rules for testing divisibility of a number by $2,3,4,5,6,7,8,9,10,11$, and 12 are given below:

| A number is <br> divisible by | if |
| :--- | :--- |
| 2 | The last digit is $0,2,4,6$ or 8 ( an even no.). <br> 3 <br> 4 <br> 5 <br> 6 <br> 8 |
| The sum of all its digit is divisible by 3. <br> The last two digit form a number divisible by 4 or are 00. <br> The last digit is 5 or 0. |  |
| 10 | It is divisible by both 2 and 3. <br> The last three digits form a number divisible by 8 or are 000. <br> The sum of all digits is divisible by 9. <br> The last digit is 0. |
| The difference between the sum of digits at odd and even places is either 0 or in |  |
| multiples of 11. |  |
| It is divisible by both 3 and 4. |  |

