

7.1

Amplitude Modulation

Statement for Q.1-3.

An AM signal is represented by

$$v_c(t) = (10 + 4 \sin 1000\pi t) \cos (2\pi \times 10^6 t) \text{ V}$$

1. The modulation index is

- (A) 10 (B) 4
(C) 0.4 (D) 2.5

2. The total signal power is

- (A) 108 W (B) 116 W
(C) 100 W (D) 132 W

3. The total side band power is

- (A) 8 W (B) 16 W
(C) 0 W (D) 32 W

4. A 1 kW carrier is to be modulated to a 80% level.

The total transmitted power would be

- (A) 2 kW (B) 1.32 kW
(C) 1.4 kW (D) None of the above

5. An AM broadcast station operates at its maximum allowed total output of 100 kW with 90% modulation.

The power in the intelligence part is

- (A) 28.8 kW (B) 71.2 kW
(C) 35.6 kW (D) None of the above

6. The aerial current of an AM transmitter is 16 A when unmodulated but increases to 18 A when modulated. The modulation index is

- (A) 0.73 (B) 0.63
(C) 0.89 (D) None of the above

7. A modulating signal is amplified by a 80% efficiency amplifier before being combined with a 10 kW carrier to generate an AM signal. The required DC input

power to the amplifier, for the system to operate at 100% modulation, would be

- (A) 5 kW (B) 8.46 kW
(C) 10 kW (D) 6.25 kW

8. A 2 MHz carrier is amplitude modulated by a 500 Hz modulating signal to a depth of 60%. If the unmodulated carrier power is 1 kW, the power of the modulated signal is

- (A) 1.83 kW (B) 1.36 kW
(C) 1.18 kW (D) 1.26 kW

9. An AM transmitter is coupled to an aerial. The input current is observed to be 5 A. With modulation the current value increases to 5.9 A. The depth of modulation is

- (A) 83.4 % (B) 88.6 %
(C) 78.2 % (D) 74.3 %

10. A carrier is amplitude modulate to 100 % by a polar rectangular signal as shown in fig. P7.1.10. The percentage increase in signal power is

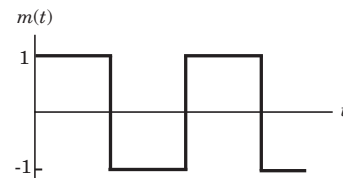


Fig. P7.1.10

- (A) 83.3 % (B) 100 %
(C) 50 % (D) None of the above

11. A carrier is amplitude modulated by two sinusoidal signals of different frequencies with individual modulation depths of 0.3 and 0.4. The power in side band would be

- (A) 12 % (B) 9 %
 (C) 11.1 % (D) 10 %

12. In 50 % modulated AM signal, the carrier is suppressed before transmission. The saving in transmitted power would be

- (A) 88.9 % (B) 11.1 %
 (C) 72 % (D) 18 %

13. A 20 kW carrier is sinusoidally modulated by two carriers corresponding to a modulation index of 30 % and 40 % respectively. The total radiated power is

- (A) 25 kW (B) 22.5 kW
 (C) 30 kW (D) 35 kW

14. In a broadcast transmitter, the RF output is represented as

$$x_c(t) = 100[1 + 0.9 \cos 5000t + 0.3 \sin 9000t] \cos(6 \times 10^6 t) \text{ V.}$$

The sidebands frequencies are

- (A) 5.991, 5.995, 6.005, 6.009 MHz
 (B) 953.5, 954.1, 955.7, 956.4 kHz
 (C) 5, 9 kHz
 (D) 795.8, 432.4 Hz

15. A diode detector has a load of 1 k Ω shunted by a 10000 pF capacitor. The diode has a forward resistance of 1 Ω . The maximum permissible depth of modulation, so as to avoid diagonal clipping, with modulating signal frequency of 10 kHz will be

- (A) 0.847 (B) 0.628
 (C) 0.734 (D) None of the above

16. A non-linear device with a transfer characteristic given by $i = (10 + 2v_i + 0.2v_i^2)$ mA is supplied with a carrier of 1 V amplitude and a sinusoidal signal of 0.5 V amplitude in series. If at the output the frequency component of AM signal is considered, the depth of modulation is

- (A) 18 % (B) 10 %
 (C) 20 % (D) 33.33 %

17. A message signal is periodic with period T , as shown in fig. P7.1.17. This message signal is applied to an AM modulator with modulation index $\beta = 0.4$. The modulation efficiency would be

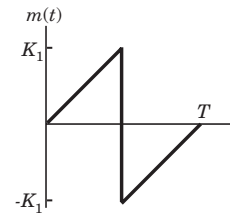


Fig. P7.1.17

- (A) 51 % (B) 11.8 %
 (C) 5.1 % (D) None of the above

Statement for Q.18-21:

The fig. P1.7.18-21 shows the positive portion of the envelope of the output of an AM modulator. The message signal is a waveform having zero DC value.

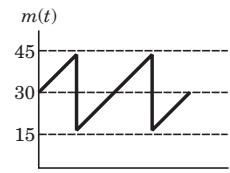


Fig. P7.1.18-21

- 18.** The modulation index is
 (A) 0.5 (B) 0.6
 (C) 0.4 (D) 0.8

- 19.** The modulation efficiency is
 (A) 8.3% (B) 14.28%
 (C) 7.69% (D) None of the above

- 20.** The carrier power is
 (A) 60 W (B) 450 W
 (C) 30 W (D) 900 W

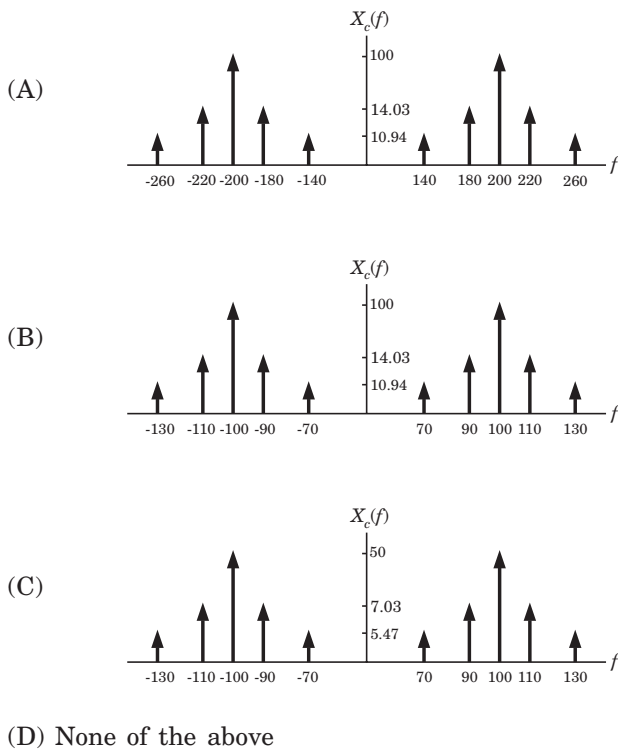
- 21.** The power in sidebands is
 (A) 85 W (B) 42.5 W
 (C) 56 W (D) 37.5 W

Statement for Q.22-23:

An AM modulator operates with the message signal $m(t) = 9 \cos 20\pi t + 7 \cos 60\pi t$. The unmodulated carrier is given by $100 \cos 200\pi t$, and the system operates with an index of 0.5.

- 22.** The power in normalized message signal $m_n(t)$ would be
 (A) 0.693 (B) 0.542
 (C) 0.254 (D) None of the above

- 23.** The double-sided spectrum of $x_c(t)$ would be



- 24.** An AM modulator has output

$$x_c(t) = 40 \cos 400\pi t + 4 \cos 360\pi t + 4 \cos 440\pi t$$
 The modulation efficiency is
 (A) 0.01 (B) 0.02
 (C) 0.03 (D) 0.04
- 25.** An AM modulator has output

$$x_c(t) = A \cos 400\pi t + B \cos 380\pi t + B \cos 420\pi t$$
 The carrier power is 100 W and the efficiency is 40 %. The value of A and B are
 (A) 14.14 , 8.16 (B) 50 , 10
 (C) 22.36 , 13.46 (D) None of the above

Statement for Q.26-27:

Consider the system shown in fig. P7.1.26-27. The average value of $m(t)$ is zero and maximum value of $|m(t)|$ is M . The square-law device is defined by $y(t) = 4x(t) + 10x^2(t)$

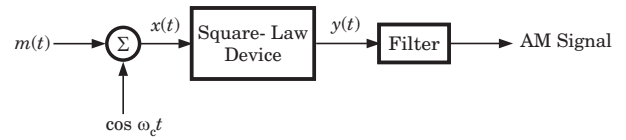


Fig. P7.1.26-27

- 26.** The value of M , required to produce modulation index of 0.8, is
 (A) 0.32 (B) 0.26
 (C) 0.52 (D) 0.16
- 27.** Let W be the BW of message signal $m(t)$. AM signal would be recovered if.
 (A) $f_c > W$ (B) $f_c > 2W$
 (C) $f_c > 3W$ (D) $f_c > 4W$
- 28.** A super heterodyne receiver is designed to receive transmitted signals between 5 and 10 MHz. High-side tuning is to be used. The tuning range of the local oscillator for IF frequency 500 kHz would be
 (A) 4.5 MHz– 9.5 MHz
 (B) 5.5 MHz – 10.5 MHz
 (C) 4.5 MHz – 10.5 MHz
 (D) None of the above
- 29.** A super heterodyne receiver uses an IF frequency of 455 kHz. The receiver is tuned to a transmitter having a carrier frequency of 2400 kHz. High-side tuning is to be used. The image frequency will be
 (A) 2855 kHz (B) 3310 kHz
 (C) 1945 kHz (D) 1490 kHz
- 30.** A super heterodyne receiver is to operate in the frequency range of 550 kHz – 1650 kHz, with the intermediate frequency of 450 kHz. The receiver is tuned to 700 kHz. The capacitance ratio $R = C_{max}/C_{min}$ of the local oscillator would be
 (A) 4.41 (B) 2.1
 (C) 3 (D) 9

- 31.** Consider a system shown in fig. P7.1.31. Let $X(f)$ and $Y(f)$ denote the Fourier transform of $x(t)$ and $y(t)$ respectively. The positive frequencies where $Y(f)$ has spectral peak are

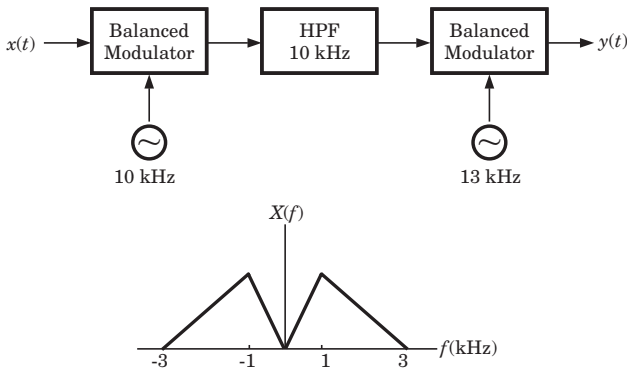


Fig. P7.1.31b

- (A) 1 kHz and 24 kHz
- (B) 2 kHz and 24 kHz
- (C) 1 kHz and 14 kHz
- (D) 2 kHz and 14 kHz

32. In fig. P7.1.32, $m(t) = \frac{2 \sin 2\pi t}{t}$, $s(t) = \cos 200\pi t$ and $n(t) = \frac{\sin 199\pi t}{t}$. The output $y(t)$ is

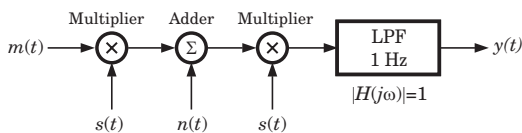


Fig. P7.1.32

- (A) $\frac{\sin 2\pi t}{2t}$
- (B) $\frac{\sin 2\pi t}{2t} + \frac{\sin \pi t}{t} \cos 3\pi t$
- (C) $\frac{\sin 2\pi t}{2t} + \frac{\sin 0.5\pi t}{t} \cos 1.5\pi t$
- (D) $\frac{\sin 2\pi t}{2t} + \frac{\sin \pi t}{t} \cos 0.75\pi t$

33. In the circuit shown in fig P7.1.33 between the terminal 1 and 2 an a.c. voltage source of frequency 400 Hz is connected. Another a.c. voltage of 1.0 MHz is connected between 3 and 4. The output between 5 and 6 contains components at

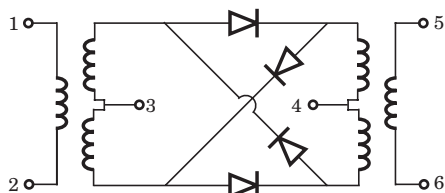


Fig. P7.1.33

- (A) 400 Hz, 1 MHz, 1000.4 kHz, 999.6 kHz
- (B) 1 MHz, 1000.4 kHz, 999.6 kHz

- (C) 400 Hz, 1000.4 kHz, 999.6 kHz
- (D) 1000.4 kHz, 999.6 kHz

34. 12 signals each band-limited to 5 kHz are to be transmitted over a single channel by frequency division multiplexing. If AM-SSB modulation guard band of 1 kHz is used, then the band width of the multiplexed signal will be

- (A) 131 kHz
- (B) 81 kHz
- (C) 121 kHz
- (D) 71 kHz

35. Let $x(t)$ be a signal band-limited to 1 kHz. Amplitude modulation is performed to produce signal $g(t) = x(t) \sin 2000\pi t$. A proposed demodulation technique is illustrated in fig. P7.1.35. The ideal low pass filter has cutoff frequency 1 kHz and pass band gain 2. The $y(t)$ would be

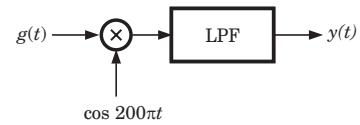


Fig. P7.1.35

- (A) $2y(t)$
- (B) $y(t)$
- (C) $\frac{y(t)}{2}$
- (D) 0

36. Suppose we wish to transmit the signal $x(t) = \sin 200\pi t + 2 \sin 400\pi t$ using a modulation that create the signal $g(t) = x(t) \sin 400\pi t$. If the product $g(t) \sin 400\pi t$ is passed through an ideal LPF with cutoff frequency 400π and pass band gain of 2, the signal obtained at the output of the LPF is

- (A) $\sin 200\pi t$
- (B) $\frac{1}{2} \sin 200\pi t$
- (C) $2 \sin 200\pi t$
- (D) 0

37. In a AM signal the received signal power is 10^{-10} W with a maximum modulating signal of 5 kHz. The noise spectral density at the receiver input is 10^{-18} W/Hz. If the noise power is restricted to the message signal bandwidth only, the signals-to-noise ratio at the input to the receiver is

- (A) 43 dB
- (B) 66 dB
- (C) 56 dB
- (D) 33 dB

Solutions

1. (C) $v_c(t) = 10[1 + 0.4 \sin(1000\pi t) \cos(2\pi \times 10^6 t)]$ V

$$\beta = 0.4$$

2. (A) $P_t = P_c \left(1 + \frac{\beta^2}{2}\right)$, $P_c = (10)^2 = 100$, $\beta = 0.4$

$$P_t = 100 \left(1 + \frac{(0.4)^2}{2}\right) = 108 \text{ W}$$

3. (A) $P_t = 108$, $P_c = 100$, $P_{sb} = 108 - 100 = 8$ W

4. (B) $P_t = P_c \left(1 + \frac{\beta^2}{2}\right) = 1000 \left(1 + \frac{(0.8)^2}{2}\right) = 1.32$ kW

5. (A) $P_t = P_c \left(1 + \frac{\beta^2}{2}\right)$

$$\Rightarrow 100 \times 10^3 = P_c \left(1 + \frac{(0.9)^2}{2}\right)$$

$$\Rightarrow P_c = 712 \text{ kW}$$

$$P_i = (P_t - P_c) = (100 - 712) = 28.8 \text{ kW}$$

6. (A) $I_t = I_c \left(1 + \frac{\beta^2}{2}\right)^{\frac{1}{2}}$

$$\Rightarrow 18 = 16 \left(1 + \frac{\beta^2}{2}\right)^{\frac{1}{2}} \Rightarrow \beta = 0.73$$

7. (D) $P_t = 10 \text{ k} \left(1 + \frac{1}{2}\right)$, $P_t = 15$ kW,

$$P_i = 15 - 10 = 5 \text{ kW}$$

$$\text{The DC input power} = \frac{5}{0.8} = 6.25 \text{ kW}$$

8. (C) $P_c = 1$ kW, $\beta = 60\%$ = 0.6

$$P_t = P_c \left(1 + \frac{\beta^2}{2}\right) = 1 \left(1 + \frac{(0.6)^2}{2}\right) = 1.18 \text{ kW}$$

9. (B) $I_t = I_c \left(1 + \frac{\beta^2}{2}\right)^{\frac{1}{2}}$,

$$\Rightarrow 5.9 = 5 \left(1 + \frac{\beta^2}{2}\right)^{\frac{1}{2}} \Rightarrow \beta = 0.886, \text{ depth} = 88.6\%$$

10. (B) $\beta = 1.0$ or 100%

The modulating signal $m(t)$ assumes any of the two values +1, or -1, with $m(t)$ being a polar rectangular signal so

$$\beta^2 m^2(t) = 1, P_t = P_c [1 + \beta^2 m^2(t)] = 2P_c$$

$$\% \text{ increase} = 100\%$$

11. (C) Let P_c be the carrier power.

$$\text{Total side band power} = \beta^2 \overline{x^2(t)} P_c$$

$$\text{where } \beta x(t) = 0.3 \cos \omega_1 t + 0.4 \cos \omega_2 t$$

$$\beta^2 \overline{x^2(t)} = (0.3 \cos \omega_1 t + 0.4 \cos \omega_2 t)^2$$

$$= \frac{1}{2} ((0.3)^2 + (0.4)^2) = 0.125$$

$$2P_{sb} = 0.125P_c$$

$$P_t = P_c + 0.125P_c = 1.125P_c$$

$$\% \text{ side-band power} = \frac{0.125P_c}{1.125P_c} = 11.1\%$$

12. (A) $\beta = \frac{50}{100} = 0.5$

$$P_t = P_c \left(1 + \frac{\beta^2}{2}\right) = P_c \left(1 + \frac{(0.5)^2}{2}\right)$$

$$P_t = 1.125P_c$$

Saving will be P_c if carrier is suppressed.

$$\text{Saving} = \frac{P_c}{1.125P_c} = 89.9\%$$

13. (B) $P_t = P_c \left(1 + \frac{\beta_1^2}{2} + \frac{\beta_2^2}{2}\right)$, $\beta_1 = 0.3$, $\beta_2 = 0.4$

$$P_t = 20 \left(1 + \frac{0.09}{2} + \frac{0.16}{2}\right) = 22.5 \text{ kW}$$

14. (B) Side band frequencies are,

$$(6 \times 10^6 \pm 5000) \text{ rad and } (6 \times 10^6 \pm 9000) \text{ rad}$$

$$\omega_{sb} = 5.995, 6.005, 5.991 \text{ and } 6.009 \text{ MHz}$$

$$f_{sb} = \frac{\omega_{sb}}{2\pi} = 953.5, 955.7, 954.1, 956.4 \text{ kHz}$$

15. (A) $f_m = 10$ kHz, $R = 1000 \Omega$, $C = 10000$ pF

$$\text{Hence } 2\pi f_m RC = 2\pi \times 10^4 \times 10^3 \times 10^{-8} = 0.628$$

$$\beta_{\max} = (1 + (0.628)^2)^{\frac{1}{2}} = 0.847$$

16. (C) $v_i(t) = \cos \omega_c t + 0.5 \cos \omega_m t$

$$i = 10 + 2(\cos \omega_c t + 0.5 \cos \omega_m t) + 0.2(\cos \omega_c t + 0.5 \cos \omega_m t)^2$$

The AM signal

$$= 2 \cos \omega_c t + 0.2 \cos \omega_c t \cos \omega_m t = (2 + 0.2 \cos \omega_m t) \cos \omega_c t$$

$$\beta = \frac{0.2}{2} = \frac{1}{10} = 10\%$$

17. (C) The normalized message signal is

$$m(t) = \frac{2}{T} t, \quad 0 < t \leq \frac{T}{2}$$

$$\overline{m^2(t)} = \frac{2}{T} \int_0^{T/2} \left(\frac{2}{T} t\right)^2 dt = \frac{1}{3}$$

$$E_{eff} = \frac{\beta^2 \overline{m^2(t)}}{1 + \beta^2 \overline{m^2(t)}} = \frac{(0.4)^2 \frac{1}{3}}{1 + (0.4)^2 \frac{1}{3}} = 5.1\%$$

18. (A) $A_c(1 + \beta) = 45$, $A_c(1 - \beta) = 15$

$$\frac{1 + \beta}{1 - \beta} = 3 \Rightarrow \beta = 0.5$$

19. (C) Normalized message

$$m_n(t) = \frac{2}{T} t, \quad 0 \leq t \leq \frac{T}{2}$$

$$\overline{m_n^2(t)} = \frac{2}{T} \int_0^{T/2} \left(\frac{2}{T} t\right)^2 dt = \frac{1}{3}$$

$$E_{eff} = \frac{(0.5)^2 \frac{1}{3}}{1 + (0.5)^2 \frac{1}{3}} = 7.69\%$$

20. (B) $A_c(1 + 0.5) = 45 \Rightarrow A_c = 30$,

carrier power is $P_c = \frac{1}{2} A_c^2 = 450$ W

$$21. (D) E_{eff} = \frac{P_{sb}}{P_c + P_{sb}} = 0.0769$$

$$P_{sb} = \frac{0.0769}{1 - 0.0769 P_c} = \frac{0.0769}{0.9231} \times 450 = 37.5$$
 W

22. (C) The maximum value of $m(t) = 16$

$$m_n(t) = \frac{1}{16} (9 \cos 20\pi t + 7 \cos 60\pi t)$$

$$\overline{m_n^2(t)} = \left(\frac{1}{16}\right)^2 \left(\frac{9^2}{2} + \frac{7^2}{2}\right) = 0.254$$
 W

23. (B)

$$\begin{aligned} x_c(t) &= 100 \left(1 + \frac{1}{16} \frac{1}{2} (9 \cos 20\pi t + 7 \cos 60\pi t)\right) \cos 200\pi t \\ &= 10.94 \cos(140\pi t) + 14.06 \cos(180\pi t) + 100 \cos(200\pi t) \\ &\quad + 14.06 \cos(220\pi t) + 10.94 \cos(260\pi t) \\ &= 5.47(e^{j(140\pi t)} + e^{-j(140\pi t)}) + 7.03(e^{j(180\pi t)} + e^{-j(180\pi t)}) \\ &\quad + 50(e^{j(200\pi t)} + e^{-j(200\pi t)}) + 7.03(e^{j(220\pi t)} + e^{-j(220\pi t)}) \end{aligned}$$

$$+ 5.47(e^{j(260\pi t)} + e^{-j(260\pi t)})$$

Hence (B) is correct option.

24. (B) $x_c(t)$ can be written as

$$x_c(t) = (40 + 8 \cos 40\pi t) \cos 400\pi t$$

$$\text{modulation index } \beta = \frac{8}{40} = 0.2$$

$$P_c = \frac{1}{2} (40)^2 = 800$$
 W

The components at 180 Hz and 220 Hz are side band

$$P_{sb} = \frac{1}{2} (4)^2 + \frac{1}{2} (4)^2 = 16$$
 W

$$E_{eff} = \frac{P_{sb}}{P_c + P_{sb}} = \frac{16}{800 + 16}$$

25. (A) Carrier power $P_c = \frac{A^2}{2} = 100$ W, $A = 14.14$

$$E_{eff} = \frac{P_{sb}}{P_c + P_{sb}} = \frac{40}{100} \Rightarrow \frac{P_{sb}}{100 + P_{sb}} = 0.4$$

$$P_{sb} = 66.67$$
 W

$$P_{sb} = \frac{1}{2} B^2 + \frac{1}{2} B^2 = 66.67 \Rightarrow B = 8.161$$

$$\begin{aligned} 26. (D) y(t) &= 4(m(t) + \cos \omega_c t) + 10(m(t) + \cos \omega_c t)^2 \\ &= 4m(t) + 4 \cos \omega_c t + 10m^2(t) + 20m(t) \cos \omega_c t + 5 + 5 \cos 2\omega_c t \\ y(t) &= 5 + 4m(t) + 10m^2(t) + 4(1 + 5m(t)) \cos \omega_c t + 5 \cos 2\omega_c t \end{aligned}$$

The AM signal is,

$$x_c(t) = 4[1 + 5m(t)] \cos \omega_c t$$

$$m(t) = Mm_n(t)$$

$$x_c(t) = 4[1 + 5Mm_n(t)] \cos \omega_c t$$

$$5M = 0.8, M = 0.16$$

27. (C) The filter characteristic is shown in fig. S7.1.17

$$f_c - W > 2W \Rightarrow f_c > 3W, f_c + W < 2f_c \Rightarrow f_c > W$$

Therefore $f_c > 3W$.

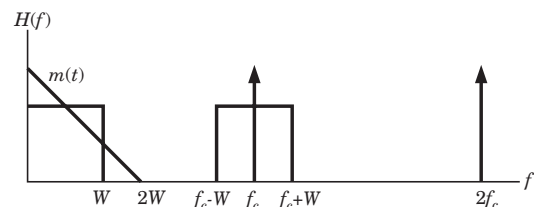


Fig. S7.1.27

28. (B) Since High-side tuning is used, $f_{LO} = f_m + f_{IF}$

$$f_{IF} = 500$$
 kHz,

$$f_{LOL} = 5 + 0.5 = 5.5$$
 MHz, $f_{LOU} = 10 + 0.5 = 10.5$ MHz

29. (B) $f_{image} = f_L + 2 f_{IF} = 2400 + 2 \times 455 = 3310$ kHz

30. (A) $f_{\max} = 1650 + 450 = 2100 \text{ kHz}$

$f_{\min} = 550 + 450 = 1000 \text{ kHz}$

$$f = \frac{1}{2\pi\sqrt{LC}}$$

When frequency is minimum, capacitance will be maximum

$$R = \frac{C_{\max}}{C_{\min}} = \frac{f_{\min}^2}{f_{\max}^2} = (2.1)^2 \Rightarrow R = 4.41$$

31. (B) Since $X(f)$ has spectral peak at 1 kHz so at the output of first modulator spectral peak will be at $(10\text{k} + 1\text{k}) \text{ Hz}$ and $(10\text{k} - 1\text{k}) \text{ Hz}$. After passing the HPF frequency component of 11 kHz will remain. The output of 2nd modulator will be $(13\text{k} \pm 11\text{k}) \text{ Hz}$. So $Y(f)$ has spectral peak at 2 k and 24 kHz.

32. (C) $m(t)s(t) = y_1(t) = \frac{2 \sin(2\pi t) \cos(200\pi t)}{t}$

$$= \frac{\sin(202\pi t) - \sin(198\pi t)}{t}$$

$$y_1(t) + n(t) = y_2(t) = \frac{\sin 202\pi t - \sin 198\pi t}{t} + \frac{\sin 198\pi t}{t}$$

$$y_2(t) s(t) = y(t) = \frac{[\sin 202\pi t - \sin 198\pi t + \sin 199\pi t] \cos 200\pi t}{t}$$

$$= \frac{1}{2t} [\sin(402\pi t) + \sin(2\pi t) - \{\sin(398\pi t) - \sin(2\pi t)\}]$$

$$+ \sin(399\pi t) - \sin(\pi t)]$$

After filtering

$$y(t) = \frac{\sin(2\pi t) + \sin(2\pi t) - \sin(\pi t)}{2t}$$

$$= \frac{\sin(2\pi t) + 2 \sin(0.5t) \cos(1.5\pi t)}{2t}$$

$$= \frac{\sin 2\pi t}{2t} + \frac{\sin 0.5\pi t}{t} \cos 1.5\pi t$$

33. (D) The given circuit is a ring modulator. The output is DSB-SC signal. So it will contain $m(t) \cos(n\omega_c t)$ where $n = 1, 2, 3, \dots$

Therefore there will be only $(1 \text{ MHz} \pm 400 \text{ Hz})$ frequency component.

34. (D) The total signal bandwidth $= 5 \times 12 = 60 \text{ kHz}$

There would be 11 guard band between 12 signal. So guard band width $= 11 \text{ kHz}$

Total band width $= 60 + 11 = 71 \text{ kHz}$

35. (D) $x_1(t) = g(t) \cos(2000\pi t)$

$$= x(t) \sin(2000\pi t) \cos(2000\pi t) = \frac{1}{2} x(t) \sin(4000\pi t)$$

$$X_1(j\omega) = \frac{1}{4j} X(j(\omega - 4000\pi)) - X(j(\omega + 4000\pi))$$

This implies that $X_1(j\omega)$ is zero for $|\omega| \leq 2000\pi$ because $\omega < 2\pi f_m = 2\pi 1000$. When $x_1(t)$ is passed through a LPF with cutoff frequency 2000π , the output will be zero.

36. (A) $y(t) = g(t) \sin(400\pi t) = x(t) \sin^2(400\pi t)$

$$= (\sin(200\pi t) + 2 \sin(400\pi t)) \frac{(1 - \cos(800\pi t))}{2}$$

$$= \frac{1}{2} [\sin(200\pi t) - \sin(200\pi t) \cos(800\pi t)$$

$$+ 2 \sin(400\pi t) - \sin(400\pi t) \cos(800\pi t)]$$

$$= \frac{1}{2} \sin(200\pi t) - \frac{1}{4} [\sin(1000\pi t) - \sin(600\pi t)]$$

$$+ \sin(400\pi t) - \frac{1}{4} [\sin(1200\pi t) - \sin(400\pi t)]$$

If this signal is passed through LPF with frequency 400π and gain 2, the output will be $\sin(200\pi t)$.

37. (A) Message signal BW $f_m = 5 \text{ kHz}$

Noise power density $= 10^{-18} \text{ W/Hz}$.

Total noise power $= 10^{-18} \times 5\text{k} = 5 \times 10^{-15} \text{ W}$

Input signal-to-noise ratio

$$\text{SNR}_i = \frac{10^{-10}}{5 \times 10^{-15}} = 2 \times 10^4$$

$$\text{SNR}_i = 10 \log_{10} 2 \times 10^4 = 43 \text{ dB}$$
