

## ALCCS

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Code: CS41

Subject: NUMERICAL &amp; SCIENTIFIC COMPUTING

Time: 3 Hours

Max. Marks: 100

**MARCH 2010**

NOTE:

- Question 1 is compulsory and carries 28 marks. Answer any FOUR questions from the rest. Marks are indicated against each question.
  - Parts of a question should be answered at the same place.
  - All calculations should be up to three places of decimals.
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**Q.1** a. Find the number of terms of the exponential series such that their sum gives the value of  $e^x$  correct to six decimal places at  $x = 1$ .

b. Find a root of the equation  $xe^x = \cos x$ , by the secant method upto two iterations.

c. Factorize the matrix  $\begin{pmatrix} 3 & 2 & 7 \\ 2 & 3 & 1 \\ 3 & 4 & 1 \end{pmatrix}$  using LU decomposition.

d. Given the matrix  $A = I + L + U$ , where  $A = \begin{bmatrix} 1 & 2 & -2 \\ 1 & 1 & 1 \\ 2 & 2 & 1 \end{bmatrix}$ , L and U are the lower and upper triangular matrices respectively, decide whether Jacobi method converges to the solution of  $Ax = b$ .

e. Evaluate  $\int_{-1}^1 \frac{dx}{1+x^2}$  using Gauss formula for  $n = 2$ .

f. Solve

$$\frac{dy}{dx} = y - \frac{2x}{y}; y(0) = 1 \text{ at } x = 0.1 \text{ using Euler method.}$$

g. Show that  $\Delta^3 y_2 = \nabla^3 y_5$ . (7 × 4)

**Q.2** a. Find a real root of  $2x - \log_{10} x = 7$  correct to four decimal places using Newton's Method.

b. One entry in the following table is incorrect and  $y$  is a cubic polynomial in  $x$ . Use the difference table to locate and correct the error: (9+9)

x	0	1	2	3	4	5	6	7
y	25	21	18	18	27	45	76	123

**Q.3** a. Solve by Gauss-Seidel method, the following system of equations:

$$x + y + z = 9$$

$$2x - 3y + 4z = 13$$

$$3x + 4y + 5z = 40$$

b. Solve by Relaxation method, the system of equations:

$$10x_1 - 2x_2 - 2x_3 = 6;$$

$$-x_1 + 10x_2 - 2x_3 = 7;$$

$$-x_1 - x_2 + 10x_3 = 8.$$

(9+9)

**Q.4** a. Using Jacobi's method, find all the eigenvalues and the eigenvectors of the matrix

$$A = \begin{pmatrix} 1 & \sqrt{2} & 2 \\ \sqrt{2} & 3 & \sqrt{2} \\ 2 & \sqrt{2} & 1 \end{pmatrix}$$

b. Using inverse interpolation, find the real root of the equation  $x^3 + x - 3 = 0$  which is close to 1.2. (9+9)

**Q.5** a. The following table gives the distance in nautical miles of the visible horizon for the given heights in feet above the earth's surface :

x = height	100	150	200	250	300	350	400
y = distance	10.63	13.03	15.04	16.81	18.42	19.90	21.27

Find the value of y when x = 218 ft and x = 410 ft.

b. From the given data, find the maximum value of y:

(9+9)

x	-1	1	2	3
y	-21	15	12	3

**Q.6** a. Use Romberg's method to compute  $\int_0^1 \frac{dx}{1+x^2}$  correct to four decimal places.

b. Determine f(x) as a polynomial in x for the following data:

(9+9)

x	-4	-1	0	2	5
y	1245	33	5	9	1335

**Q.7** a. Using Runge-Kutta method of fourth order, solve for y(0.1), y(0.2) given that  $\frac{dy}{dx} = xy + y^2, y(0) = 1$ .

b. Using Taylor's series method, solve  $\frac{dy}{dx} = x^2 - y, y(0) = 1$  at x = 0.1, 0.2. (12+6)