

## MATHEMATICS

1. If  $A = \{a, b, c\}$ ,  $B = \{b, c, d\}$  and  $C = \{a, d, c\}$ , then  $(A - B) \times (B \cap C) =$
- 1)  $\{(a, c), (a, d), (b, d)\}$                       2)  $\{(c, a), (d, a)\}$   
3)  $\{(a, b), (c, d)\}$                               4)  $\{(a, c), (a, d)\}$
2. The function  $f: X \rightarrow Y$  defined by  $f(x) = \sin x$  is one-one but not onto if  $X$  and  $Y$  are respectively equal to,
- 1)  $\left[\frac{-\pi}{2}, \frac{\pi}{2}\right]$  and  $[-1, 1]$                       2)  $\left[0, \frac{\pi}{2}\right]$  and  $[-1, 1]$   
3)  $[0, \pi]$  and  $[0, 1]$                               4)  $\mathbb{R}$  and  $\mathbb{R}$
3. If  $\log_4^2 + \log_4^4 + \log_4^{16} + \log_4^x = 6$ , then  $x =$
- 1) 32    2) 8  
3) 4    4) 64
4. If  $S_n = \frac{1}{6.11} + \frac{1}{11.16} + \frac{1}{16.21} + \dots$  to  $n$  terms, then  $6S_n =$
- 1)  $\frac{1}{(5n+6)}$     2)  $\frac{(2n-1)}{5n+6}$   
3)  $\frac{n}{(5n+6)}$     4)  $\frac{5n-4}{5n+6}$
5. The remainder obtained when  $(1)^2 + (2)^2 + (3)^2 + \dots + (100)^2$  is divided by  $10^2$  is
- 1) 14    2) 17  
3) 28    4) 27

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(Space for Rough Work)

6. If  $(p \wedge \sim r) \rightarrow (\sim p \vee q)$  is false, then the truth values of  $p, q$  and  $r$  are respectively
- |                   |                   |
|-------------------|-------------------|
| 1) $T, F$ and $T$ | 2) $F, T$ and $T$ |
| 3) $F, F$ and $T$ | 4) $T, F$ and $F$ |
7. If  $\alpha, \beta$  and  $\gamma$  are the roots of the equation  $x^3 - 8x + 8 = 0$ , then  $\sum \alpha^2$  and  $\sum \frac{1}{\alpha\beta}$  are respectively =
- |             |              |
|-------------|--------------|
| 1) 16 and 0 | 2) -16 and 0 |
| 3) 16 and 8 | 4) 0 and -16 |
8. The g.c.d. of 1080 and 675 is
- |        |        |
|--------|--------|
| 1) 125 | 2) 225 |
| 3) 135 | 4) 145 |
9. If  $a \mid (b+c)$  and  $a \mid (b-c)$  where  $a, b, c \in N$  then,
- |                                |                                |
|--------------------------------|--------------------------------|
| 1) $c^2 \equiv a^2 \pmod{b^2}$ | 2) $a^2 \equiv b^2 \pmod{c^2}$ |
| 3) $a^2 + c^2 = b^2$           | 4) $b^2 \equiv c^2 \pmod{a^2}$ |
10. If  $a, b$  and  $c \in N$  which one of the following is not true ?
- |   |   |
|---|---|
| 1) $a \mid b$ and $a \mid c \Rightarrow a \mid b+c$ | 2) $a \mid b+c \Rightarrow a \mid b$ and $a \mid c$   |
| 3) $a \mid b$ and $b \mid c \Rightarrow a \mid c$   | 4) $a \mid b$ and $a \mid c \Rightarrow a \mid 3b+2c$ |

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(Space for Rough Work)

11. If  $2A + 3B = \begin{bmatrix} 2 & -1 & 4 \\ 3 & 2 & 5 \end{bmatrix}$  and  $A + 2B = \begin{bmatrix} 5 & 0 & 3 \\ 1 & 6 & 2 \end{bmatrix}$ , then  $B =$

1)  $\begin{bmatrix} 8 & 1 & 2 \\ 1 & 10 & 1 \end{bmatrix}$

2)  $\begin{bmatrix} 8 & 1 & -2 \\ -1 & 10 & -1 \end{bmatrix}$

3)  $\begin{bmatrix} 8 & 1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$

4)  $\begin{bmatrix} 8 & -1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$

12. If  $O(A) = 2 \times 3$ ,  $O(B) = 3 \times 2$ , and  $O(C) = 3 \times 3$ , which one of the following is not defined?

1)  $C(A+B')$

2)  $C(A+B')$

3)  $BAC$

4)  $CB+A'$

13. If  $A = \begin{bmatrix} 1 & -3 \\ 2 & K \end{bmatrix}$  and  $A^2 - 4A + 10I = A$ , then  $K =$

1) 1 or 4

2) 4 and not 1

3) -4

4) 0

14. The value of  $\begin{vmatrix} x+y & y+z & z+x \\ x & y & z \\ x-y & y-z & z-x \end{vmatrix} =$

1) 0

2)  $(x+y+z)^3$

3)  $2(x+y+z)^3$

4)  $2(x+y+z)^2$

15. On the set  $Q$  of all rational numbers the operation  $*$  which is both associative and commutative is given by  $a * b =$

1)  $2a + 3b$

2)  $ab + 1$

3)  $a^2 + b^2$

4)  $a + b + ab$

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(Space for Rough Work)

16. In the group  $G = \{1, 5, 7, 11\}$  under multiplication modulo 12, the solution of  $7^{-1} \times \left( x \times_{12} 11 \right) = 5$  is  $x =$

- 1) 11  
2) 7  
3) 1  
4) 5

17. A subset of the additive group of real numbers which is not a sub group is

- 1)  $(\mathbb{Q}, +)$   
2)  $(\mathbb{N}, +)$   
3)  $(\mathbb{Z}, +)$   
4)  $(\{0\}, +)$

18. If  $\vec{p} = \hat{i} + \hat{j}$ ,  $\vec{q} = 4\hat{k} - \hat{j}$  and  $\vec{r} = \hat{i} + \hat{k}$ , then the unit vector in the direction of  $3\vec{p} + \vec{q} - 2\vec{r}$  is

- 1)  $\hat{i} + 2\hat{j} + 2\hat{k}$   
2)  $\frac{1}{3}(\hat{i} - 2\hat{j} + 2\hat{k})$   
3)  $\frac{1}{3}(\hat{i} - 2\hat{j} - 2\hat{k})$   
4)  $\frac{1}{3}(\hat{i} + 2\hat{j} + 2\hat{k})$

19. If  $\vec{a}$  and  $\vec{b}$  are the two vectors such that  $|\vec{a}| = 3\sqrt{3}$ ,  $|\vec{b}| = 4$  and  $|\vec{a} + \vec{b}| = \sqrt{7}$ , then the angle between  $\vec{a}$  and  $\vec{b}$  is

- 1)  $150^\circ$   
2)  $30^\circ$   
3)  $60^\circ$   
4)  $120^\circ$

20. If  $\vec{a}$  is vector perpendicular to both  $\vec{b}$  and  $\vec{c}$ , then

- 1)  $\vec{a} \cdot (\vec{b} \times \vec{c}) = 0$   
2)  $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{0}$   
3)  $\vec{a} \times (\vec{b} + \vec{c}) = \vec{0}$   
4)  $\vec{a} + (\vec{b} + \vec{c}) = \vec{0}$

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(Space for Rough Work)

21. If the area of the parallelogram with  $\vec{a}$  and  $\vec{b}$  as two adjacent sides is 15 sq. units, then the area of the parallelogram having  $3\vec{a} + 2\vec{b}$  and  $\vec{a} + 3\vec{b}$  as two adjacent sides in sq. units is
- 1) 45
  - 2) 75
  - 3) 105
  - 4) 120
22. The locus of the point which moves such that the ratio of its distances from two fixed points in the plane is always a constant  $K (< 1)$  is
- 1) circle
  - 2) straight line
  - 3) ellipse
  - 4) hyperbola
23. If the lines  $x + 3y - 9 = 0$ ,  $4x + by - 2 = 0$  and  $2x - y - 4 = 0$  are concurrent, then  $b =$
- 1) 0
  - 2) 1
  - 3) 5
  - 4) -5
24. The lines represented by  $ax^2 + 2hxy + by^2 = 0$  are perpendicular to each other if
- 1)  $h_s = 0$
  - 2)  $h^2 = ab$
  - 3)  $a + b = 0$
  - 4)  $h^2 = a + b$
25. The equation of the circle having  $x - y - 2 = 0$  and  $x - y + 2 = 0$  as two tangents and  $x + y = 0$  as a diameter is
- 1)  $x^2 + y^2 = 1$
  - 2)  $x^2 + y^2 = 2$
  - 3)  $x^2 + y^2 - 2x + 2y - 1 = 0$
  - 4)  $x^2 + y^2 + 2x - 2y + 1 = 0$

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(Space for Rough Work)

26. If the length of the tangent from any point on the circle  $(x - 3)^2 + (y + 2)^2 = 5r^2$  to the circle  $(x - 3)^2 + (y + 2)^2 = r^2$  is 16 units, then the area between the two circles in sq. units is
- 1)  $16 \pi$
  - 2)  $8 \pi$
  - 3)  $4 \pi$
  - 4)  $32 \pi$
27. The circles  $ax^2 + ay^2 + 2g_1x + 2f_1y + c_1 = 0$  and  $bx^2 + by^2 + 2g_2x + 2f_2y + c_2 = 0$  ( $a \neq 0$  and  $b \neq 0$ ) cut orthogonally if
- 1)  $g_1g_2 + f_1f_2 = c_1 + c_2$
  - 2)  $bg_1g_2 + af_1f_2 = bc_1 + ac_2$
  - 3)  $g_1g_2 + f_1f_2 = bc_1 + ac_2$
  - 4)  $g_1g_2 + f_1f_2 = ac_1 + bc_2$
28. The equation of the common tangent of the two touching circles,  $y^2 + x^2 - 6x - 12y + 37 = 0$  and  $x^2 + y^2 - 6y + 7 = 0$  is
- 1)  $x + y + 5 = 0$
  - 2)  $x + y - 5 = 0$
  - 3)  $x - y + 5 = 0$
  - 4)  $x - y - 5 = 0$
29. The equation of the parabola with vertex at  $(-1, 1)$  and focus  $(2, 1)$  is
- 1)  $y^2 - 2y - 12x + 13 = 0$
  - 2)  $y^2 - 2y + 12x + 11 = 0$
  - 3)  $x^2 + 2x - 12y + 13 = 0$
  - 4)  $y^2 - 2y - 12x - 11 = 0$
30. The equation of the line which is tangent to both the circle  $x^2 + y^2 = 5$  and the parabola  $y^2 = 40x$  is
- 1)  $2x + y + 5 = 0$
  - 2)  $2x - y - 5 = 0$
  - 3)  $2x - y + 5 = 0$
  - 4)  $2x - y \pm 5 = 0$

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(Space for Rough Work)

31.  $x = 4(1 + \cos \theta)$  and  $y = 3(1 + \sin \theta)$  are the parametric equations of

1)  $\frac{(x-4)^2}{16} + \frac{(y-3)^2}{9} = 1$

2)  $\frac{(x-4)^2}{16} - \frac{(y-3)^2}{9} = 1$

3)  $\frac{(x+4)^2}{16} + \frac{(y+3)^2}{9} = 1$

4)  $\frac{(x-3)^2}{9} + \frac{(y-4)^2}{16} = 1$

32. If the distance between the foci and the distance between the directrices of the hyperbola

$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  are in the ratio 3 : 2, then  $a : b$  is =

1) 2 : 1

2) 1 : 2

3)  $\sqrt{3} : \sqrt{2}$

4)  $\sqrt{2} : 1$

33. The ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  and the hyperbola  $\frac{x^2}{25} - \frac{y^2}{16} = 1$  have in common

1) centre and vertices only

2) centre, foci and vertices

3) centre, foci and directrices

4) centre only

34. If  $\sec \theta = m$  and  $\tan \theta = n$ , then  $\frac{1}{m} \left[ (m+n) + \frac{1}{(m+n)} \right] =$

1)  $mn$

2)  $2n$

3)  $2m$

4) 2

35. The value of  $\frac{\sin 85^\circ - \sin 15^\circ}{\cos 65^\circ} =$

1) 0

2) 1

3) -1

4) 2

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(Space for Rough Work)

36. From an aeroplane flying, vertically above a horizontal road, the angles of depression of two consecutive stones on the same side of the aeroplane are observed to be  $30^\circ$  and  $60^\circ$  respectively. The height at which the aeroplane is flying in km is

- 1) 2
- 2)  $\frac{2}{\sqrt{3}}$
- 3)  $\frac{\sqrt{3}}{2}$
- 4)  $\frac{4}{\sqrt{3}}$

37. If the angles of a triangle are in the ratio 3 : 4 : 5, then the sides are in the ratio

- 1) 3 : 4 : 5
- 2)  $2 : \sqrt{3} : \sqrt{3} + 1$
- 3)  $\sqrt{2} : \sqrt{6} : \sqrt{3} + 1$
- 4)  $2 : \sqrt{6} : \sqrt{3} + 1$

38. If  $\text{Cos}^{-1}x = \alpha$ , ( $0 < x < 1$ ) and  $\text{Sin}^{-1}(2x\sqrt{1-x^2}) + \text{Sec}^{-1}\left(\frac{1}{2x^2-1}\right) = \frac{2\pi}{3}$ ,

then  $\text{Tan}^{-1}(2x) =$

- 1)  $\frac{\pi}{2}$
- 2)  $\frac{\pi}{3}$
- 3)  $\frac{\pi}{4}$
- 4)  $\frac{\pi}{6}$

39. If  $a > b > 0$ , then the value of  $\text{Tan}^{-1}\left(\frac{a}{b}\right) + \text{Tan}^{-1}\left(\frac{a+b}{a-b}\right)$  depends on

- 1) neither  $a$  nor  $b$
- 2)  $a$  and not  $b$
- 3)  $b$  and not  $a$
- 4) both  $a$  and  $b$

40. Which one of the following equations has no solution ?

- 1)  $\sqrt{3} \text{Sin} \theta - \text{Cos} \theta = 2$
- 2)  $\text{Cos} \theta + \text{Sin} \theta = \sqrt{2}$
- 3)  $\text{Cosec} \theta \cdot \text{Sec} \theta = 1$
- 4)  $\text{Cosec} \theta - \text{Sec} \theta = \text{Cosec} \theta \cdot \text{Sec} \theta$

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(Space for Rough Work)



41. The complex number  $\frac{(-\sqrt{3} + 3i)(1-i)}{(3 + \sqrt{3}i)(i)(\sqrt{3} + \sqrt{3}i)}$  when represented in the Argand diagram lies

- 1) on the X-axis (Real axis)                      2) on the Y-axis (Imaginary axis)  
 3) in the first quadrant                            4) in the second quadrant

42. If  $2x = -1 + \sqrt{3}i$ , then the value of  $(1 - x^2 + x)^6 - (1 - x + x^2)^6 =$

- 1) 0    2) 64  
 3) -64    4) 32

43. The modulus and amplitude of  $(1 + i\sqrt{3})^8$  are respectively

- 1) 256 and  $\frac{8\pi}{3}$     2) 2 and  $\frac{2\pi}{3}$   
 3) 256 and  $\frac{2\pi}{3}$     4) 256 and  $\frac{\pi}{3}$

44. The value of  $\lim_{x \rightarrow 0} \frac{5^x - 5^{-x}}{2x} =$

- 1)  $2 \log 5$     2) 1  
 3) 0    4)  $\log 5$

45. Which one of the following is not true always?

- 1) If a function  $f(x)$  is continuous at  $x = a$ , then  $\lim_{x \rightarrow a} f(x)$  exists.  
 2) If  $f(x)$  and  $g(x)$  are differentiable at  $x = a$ , then  $f(x) + g(x)$  is also differentiable at  $x = a$ .  
 3) If  $f(x)$  is continuous at  $x = a$ , then it is differentiable at  $x = a$ .  
 4) If  $f(x)$  is not continuous at  $x = a$ , then it is not differentiable at  $x = a$ .

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(Space for Rough Work)

46. If  $y = 1 + \frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^3} + \dots$  to  $\infty$  with  $|x| > 1$  then  $\frac{dy}{dx} =$

1)  $\frac{-y^2}{x^2}$

2)  $\frac{y^2}{x^2}$

3)  $x^2 y^2$

4)  $\frac{x^2}{y^2}$

47. If  $f(x)$  and  $g(x)$  are two functions with  $g(x) = x - \frac{1}{x}$  and  $f \circ g(x) = x^3 - \frac{1}{x^3}$ , then  $f'(x) =$

1)  $3x^2 + \frac{3}{x^4}$

2)  $1 + \frac{1}{x^2}$

3)  $x^2 - \frac{1}{x^2}$

4)  $3x^2 - 3$

48. The derivative of  $a^{\sec x}$  w.r.t.  $a^{\tan x}$  ( $a > 0$ ) is

1)  $a^{\sec x - \tan x}$

2)  $\sin x a^{\sec x - \tan x}$

3)  $\sin x a^{\tan x - \sec x}$

4)  $\sec x a^{\sec x - \tan x}$

49. If  $\sin(x+y) + \cos(x+y) = \log(x+y)$ , then  $\frac{d^2y}{dx^2} =$

1) 1

2) -1

3) 0

4)  $\frac{-y}{x}$

50. If  $f(x)$  is a function such that  $f''(x) + f(x) = 0$  and  $g(x) = [f(x)]^2 + [f'(x)]^2$  and  $g(3) = 8$ , then  $g(8) =$

1) 8

2) 3

3) 0

4) 5

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(Space for Rough Work)

51. If the curve  $y = 2x^3 + ax^2 + bx + c$  passes through the origin and the tangents drawn to it at  $x = -1$  and  $x = 2$  are parallel to the X-axis, then the values of  $a$ ,  $b$  and  $c$  are respectively.

- 1) 3, -12 and 0
- 2) -3, 12 and 0
- 3) -3, -12 and 0
- 4) 12, -3 and 0

52. A circular sector of perimeter 60 metre with maximum area is to be constructed. The radius of the circular arc in metre must be

- 1) 10
- 2) 15
- 3) 5
- 4) 20

53. The tangent and the normal drawn to the curve  $y = x^2 - x + 4$  at  $P(1, 4)$  cut the X-axis at  $A$  and  $B$  respectively. If the length of the subtangent drawn to the curve at  $P$  is equal to the length of the subnormal, then the area of the triangle  $PAB$  in sq. units is.

- 1) 16
- 2) 8
- 3) 32
- 4) 4

54. 
$$\int \frac{(x^3 + 3x^2 + 3x + 1)}{(x + 1)^5} dx =$$

- 1)  $\text{Tan}^{-1}x + c$
- 2)  $\text{Log}(x + 1) + c$
- 3)  $\frac{1}{5} \text{Log}(x + 1) + c$
- 4)  $-\frac{1}{(x + 1)} + c$

55. 
$$\int \frac{\text{Cosec}x}{\text{Cos}^2\left(1 + \text{Log Tan} \frac{x}{2}\right)} dx =$$

- 1)  $-\text{Tan}\left[1 + \text{Log Tan} \frac{x}{2}\right] + c$
- 2)  $\text{Sec}^2\left[1 + \text{Log Tan} \frac{x}{2}\right] + c$
- 3)  $\text{Tan}\left[1 + \text{Log Tan} \frac{x}{2}\right] + c$
- 4)  $\text{Sin}^2\left[1 + \text{Log Tan} \frac{x}{2}\right] + c$

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(Space for Rough Work)

56.  $\int \frac{dx}{x\sqrt{x^6-16}} =$

1)  $\text{Sec}^{-1}\left(\frac{x^3}{4}\right) + c$

2)  $\frac{1}{12} \text{Sec}^{-1}\left(\frac{x^3}{4}\right) + c$

3)  $\text{Cosh}^{-1}\left(\frac{x^3}{4}\right) + c$

4)  $\frac{1}{3} \text{Sec}^{-1}\left(\frac{x^3}{4}\right) + c$

57. If  $I_1 = \int_0^{\pi/2} x \sin x \, dx$  and  $I_2 = \int_0^{\pi/2} x \cos x \, dx$ , then which one of the following is true ?

1)  $I_1 = I_2$

2)  $I_1 + I_2 = 0$

3)  $I_1 = \frac{\pi}{2} I_2$

4)  $I_1 + I_2 = \frac{\pi}{2}$

58. If  $f(x)$  is defined in  $[-2, 2]$  by  $f(x) = 4x^2 - 3x + 1$  and  $g(x) = \frac{f(-x) - f(x)}{(x^2 + 3)}$ , then

$\int_{-2}^2 g(x) \, dx =$

1) 24

2) 0

3) -48

4) 64

59. The area enclosed between the parabola  $y = x^2 - x + 2$  and the line  $y = x + 2$  in sq. units =

1)  $\frac{4}{3}$

2)  $\frac{2}{3}$

3)  $\frac{1}{3}$

4)  $\frac{8}{3}$

60. The solution of the differential equation  $e^{-x}(y+1) \, dy + (\cos^2 x - \sin 2x)y \, dx = 0$  subjected to the condition that  $y = 1$  when  $x = 0$  is

1)  $(y+1) + e^x \cos^2 x = 2$

2)  $y + \text{Log } y = e^x \cos^2 x$

3)  $\text{Log}(y+1) + e^x \cos^2 x = 1$

4)  $y + \text{Log } y + e^x \cos^2 x = 2$

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(Space for Rough Work)