## Mathematics

## Class X

## Board Paper - 2011

Time: $\mathbf{2 1} / \mathbf{2}$ hour
Total Marks: 80

1. Answer to this paper must be written on the paper provided separately.
2. You will NOT be allowed to write during the first 15 minutes. This time is to be spent in reading the question paper.
3. The time given at the head of this paper is the time allowed for writing the answers.
4. This question paper is divided into two Sections. Attempt all questions from Section $A$ and any four questions from Section B.
5. Intended marks for questions or parts of questions are given in brackets along the questions.
6. All working, including rough work, must be clearly shown and should be done on the same sheet as the rest of the answer. Omission of essential working will result in loss of marks.
7. Mathematical tables are provided.

## Section - A (40 Marks)

## Q.1.

(a) Find the value of ' $k$ ' if ( $x-2$ ) is a factor of $x^{3}+2 x^{2}-k x+10$.

Hence determine whether $(x+5)$ is also a factor.
(b) If $A=\left[\begin{array}{cc}3 & 5 \\ 4 & -2\end{array}\right]$ and $B=\left[\begin{array}{l}2 \\ 4\end{array}\right]$, is the product $A B$ possible? Give a reason. If yes, find $A B$.
(c) Mr. Kumar borrowed ₹ 15000 for two years. The rates of interest for two successive years are $8 \%$ and $10 \%$ respectively. If he repays $₹ 6200$ at the end of first year, find the outstanding amount at the end of second year.

## Q. 2.

(a) From a pack of 52 playing cards all cards whose numbers are multiples of 3 are removed. A card is now drawn at random.
(i) a face card (King, Jack or Queen)
(ii) an even numbered red card
(b) Solve the following equation:
$x-\frac{18}{x}=6$. Give your answer correct to two significant figures.
(c) In the given figure $O$ is the centre of the circle. Tangents $A$ and $B$ meet at $C$. If $\angle A C O=30^{\circ}$, find
(i) $\angle \mathrm{BCO}$
(ii) $\angle A O B$
(iii) $\angle A P B$


## Q.3.

(a) Ahmed has a recurring deposit account in a bank. He deposits ₹ 2,500 per month for 2 years. If he gets $₹ 66,250$ at the time of maturity, find
(i) The interest paid by the bank
(ii) The rate of interest
(b) Calculate the area of the shaded region, if the diameter of the semi circle is equal to 14 cm .

$$
\begin{equation*}
\text { Take } \pi=\frac{22}{7} \tag{3}
\end{equation*}
$$


(c) $A B C$ is a triangle and $G(4,3)$ is the centroid of the triangle.If $A=(1,3), B$ $=(4, b)$ and $C=(a, 1)$, find ' $a$ ' and ' $b$ '. Find length of side $B C$.
[4]
Q.4.
(a) Solve the following inequation and represent the solution set on the number line $2 x-5 \leq 5 x+4<11$, where $x \in I$
(b) Evaluate without using trigonometric tables.

$$
\begin{equation*}
2\left(\frac{\tan 35^{\circ}}{\cot 55^{\circ}}\right)^{2}+\left(\frac{\cot 55^{\circ}}{\tan 35^{\circ}}\right)-3\left(\frac{\sec 40^{\circ}}{\operatorname{cosec} 50^{\circ}}\right) \tag{3}
\end{equation*}
$$

(c) A Mathematics aptitude test of 50 students was recorded as follows:

| Matks | $50-$ <br> 60 | $60-$ <br> 70 | $70-$ <br> 80 | $80-$ <br> 90 | $90-$ <br> 100 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. of <br> Students | 4 | 8 | 14 | 19 | 5 |

Draw a histogram from the above data using a graph paper and locate the mode.
[4]

## Section - B (40 marks)

Q.5.
(a) A manufacturer sells a washing machine to a wholesaler for $₹ 15000$. The wholesaler sells it to a trader at a profit of $₹ 1200$ and the trader in turns sells it to a consumer at a profit of $₹ 1800$. If the rate of VAT is $8 \%$ find:
(i) The amount of VAT received by the state government on the sale of this machine from the manufacturer and the wholesaler.
(ii) The amount that the consumer pays for the machine.
(b) A solid cone of radius 5 cm and height 8 cm is melted and made into small spheres of radius 0.5 cm . Find the number of spheres formed. [3]
(c) $A B C D$ is a parallelogram where $A(x, y), B(5,8), C(4,7)$ and $D(2,-4)$. Find
(i) Coordinates of $A$
(ii) Equation of diagonal BD

## Q.6.

(a) Use a graph paper to answer the following questions (Take $1 \mathrm{~cm}=1$ unit on both axes)
(i) Plot $A(4,4), B(4,-6)$ and $C(8,0)$, the vertices of a triangle $A B C$.
(ii) Reflect $A B C$ on the $y$-axis and name it $A^{\prime} B^{\prime} C^{\prime}$.
(iii) Write the coordinates of the images $\mathrm{A}^{\prime}, \mathrm{B}^{\prime}$ and $\mathrm{C}^{\prime}$.
(iv) Give a geometrical name for the figure $A A^{\prime} C^{\prime} B^{\prime} B C$.
(v) Identify the line of symmetry of $A A^{\prime} C^{\prime} B C^{\prime}$.
[4]
(b) Mr. Choudhury opened a Saving's Bank Account at State Bank of India on $1^{\text {st }}$ April 2007. The entries of one year as shown in his pass book are given below.

| Date | Particulars | Withdrawals (in | Deposits (in | Balnce (in Rs.) |
| :--- | :--- | :--- | :--- | :--- |


|  |  | Rs. $)$ | Rs. $)$ |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{I}^{\text {st }}$ April 2007 | By Cash | - | 8550.00 | 8550.00 |
| $12^{\text {th }}-$ <br> 2007 | To Seril | 1200,00 | - | 7350.00 |
| $24^{\text {th }}$ April 2007 | By Cash | - | 4550.00 | 11900.00 |
| $8^{\text {th }}$ July 2007 | By Cheque | - | 1500.00 | 13400.00 |
| $10^{\text {th }}$ <br> 2007 | Bept. | To Cheque | 2500.00 | 3500.00 |
| $17^{\text {th }}$ <br> 2007 | - | 16900.00 |  |  |
| $11^{\text {th }}$ Oct. 2007 | By Cash | - | 800.00 | 15200.00 |
| $6^{\text {th }}$ Jan. 2008 | To Self | 2000.00 | - | 13200.00 |
| $9^{\text {th }}$ March 2008 | By Cheque | - | 950.00 | 14150.00 |

If the bank pays interest at the rate of $5 \%$ per annum, find the interest paid on $1^{\text {st }}$ April. 2008. Give your answer correct to the nearest rupee.
[6]

## Q. 7.

(a) Using componendo and dividendo, find the value of $x$

$$
\begin{equation*}
\frac{\sqrt{3 x+4}+\sqrt{3 x-5}}{\sqrt{3 x+4}-\sqrt{3 x-5}}=9 \tag{3}
\end{equation*}
$$

(b) If $A=\left[\begin{array}{ll}2 & 5 \\ 1 & 3\end{array}\right], B=\left[\begin{array}{cc}4 & -2 \\ -1 & 3\end{array}\right]$ and $I$ is the identity matrix of the same order and $A^{t}$ is the transpose of matrix $A$, find $A^{t} \cdot B+B I$.
[3]
(c) In the adjoining figure $A B C$ is a right
angled triangle with $\angle \mathrm{BAC}=90^{\circ}$.
(i) Prove $\triangle \mathrm{ADB} \sim \Delta \mathrm{CDA}$.
(ii) If $\mathrm{BD}=18 \mathrm{~cm} \mathrm{CD}=8 \mathrm{~cm}$ Find $A D$.
[4]
(iii) Find the ratio of the area of $\triangle \mathrm{ADB}$ is to area of $\triangle \mathrm{CDA}$.


## Q.8.

(a) (i) Using step - deviation method, calculate the mean marks of the following distribution.
(ii) State the modal class.

| Class interval | $50-$ <br> 55 | $55-$ <br> 60 | $60-$ <br> 65 | $65-$ <br> 70 | $70-$ <br> 75 | $75-$ <br> 80 | $80-$ <br> 85 | $85-$ <br> 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 5 | 20 | 10 | 10 | 9 | 6 | 12 | 8 |

(b) Marks obtained by 200 students in an examination are given below:

Draw an ogive for the given distribution taking $2 \mathrm{~cm}=10$ marks on one axis and $2 \mathrm{~cm}=20$ students on the other axis. Using the graph, determine
(i) The median marks.
(ii) The number of students who failed if minimum marks required to pass is 40 .
(iii) If scoring 85 and more marks is considered as grade one, find the number of students who secured grade one in the examination.
Q.9.
(a) Mr. Parekh invested Rs. 52,000 on Rs. 100 shares at a discount of Rs. 20 paying $8 \%$ dividend. At the end of one year he sells the shares at a premium of Rs. 20. find
(i) The annual dividend.
(ii) The profit earned including his dividend.
[3]
(b) Draw a circle of radius 3.5 cm . Marks a point P outside the circle at a distance of 6 cm from the centre. Construct two tangents from $P$ to the given circle. Measure and write down the length of one tangent.
[3]
(c) Prove that $(\operatorname{cosec} A-\operatorname{Sin} A)(\sec A-\cos A) \sec ^{2} A=\tan A$.
[4]

## Q. 10.

(a) 6 is the mean proportion between two numbers $x$ and $y$ and 48 is the third proportional of $x$ and $y$. Find the numbers.
(b) In what period of time will $₹ 12,000$ yield $₹ 3972$ as compound interest at $10 \%$ per annum, if compounded on an yearly basis?
(c) A man observes the angle of elevation of the top of a building to be $30^{\circ}$. He walks towards it in a horizontal line through its base. On covering 60 m the angle of elevation changes to $60^{\circ}$. Find the height of the building correct to the nearest metre.
Q. 11.
(a) $A B C$ is a triangle with $A B=10 \mathrm{~cm}, B C=8 \mathrm{~cm}$ and $A C=6 \mathrm{~cm}$ (not drawn to scale). Three circles are drawn touching each other with the vertices as their centres. Find the radii of the three circles.
[3]

(b) Rs. 480 is divided equally among ' $x$ ' children. If the numbers of children were 20 more then each would have got Rs. 12 less. Find ' $x$ '.
[3]
(c) Given equation of line $L$, is $y=4$.
(i) Write the slope of line $L_{2}$, if $L_{2}$, is the bisector of angle 0 .
(ii) Write the co-ordinates of point $P$.
(iii) Find the equation of $L_{2}$.
[4]


## TOPPER <br> ICSE X| Mathematics

LEARNING
Board Paper

