## **Diplete – Et / CS (OLD SCHEME)**

Code: DE01 / DC01 Time: 3 Hours

## **DECEMBER 2010**

Subject: MATHEMATICS - I Max. Marks: 100

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after half an hour of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

## Q.1 Choose the correct or the best alternative in the following:

(2x10)

a. The equation whose roots are double the roots of  $x^2 - bx + c = 0$  is

| $(A) 4x^2 - 2bx + c = 0$ | $(B)  x^2 - 2bx + 4c = 0$       |
|--------------------------|---------------------------------|
| (C) $x^2 - 2bx + 2c = 0$ | <b>(D)</b> $x^2 - 4bx + 2c = 0$ |

b.  $\lim_{x \to 0} \frac{\tan x - \sin x}{x^3}$  is

| ( <b>A</b> ) 0    | <b>(B)</b> 1             |
|-------------------|--------------------------|
| (C) $\frac{1}{2}$ | <b>(D)</b> $\frac{1}{4}$ |

c. If A(2, 1), B(4, 5) and C(K, -1) lie on a straight line, then value of k is

| ( <b>A</b> ) 1 | <b>(B)</b> 2   |
|----------------|----------------|
| (C) 3          | ( <b>D</b> ) 0 |

d. The equation of the straight line with slope 3 and x-intercept 2 is

(A) 
$$y=3x+2$$
 (B)  $y=3x-2$   
(C)  $y=3x+6$  (D)  $y=3x-6$ 

e. If  $y = \log(\sec x + \tan x)$ , the value of  $\frac{dy}{dx}$  is

| (A) $\frac{1}{\sec x + \tan x}$ | ( <b>B</b> ) $\sec x + \tan x$ |
|---------------------------------|--------------------------------|
| (C) sec x                       | ( <b>D</b> ) tan x             |

f. The value of  $\int_0^{\frac{\pi}{2}} \frac{dx}{1+\tan x}$  is

(A) 0 (B) 
$$\pi$$
  
(C)  $\frac{\pi}{2}$  (D)  $\frac{\pi}{4}$ 

g. The area bounded by  $y = \sin x$ , the x – axis between x = 0 and  $x = \pi$  is

| ( <b>A</b> ) 1 | <b>(B)</b> 2 |
|----------------|--------------|
| ( <b>C</b> ) 3 | <b>(D)</b> 4 |

h. The solution of the differential equation  $\frac{dy}{dx} + \frac{y}{x} = 0$  is

| $(\mathbf{A}) \mathbf{x} + \mathbf{y} = \mathbf{c}$ | $(\mathbf{B}) \ \mathbf{x}^2 + \mathbf{y}^2 = \mathbf{c}$ |
|---|---|
| $(\mathbf{C}) \mathbf{x} \mathbf{y} = \mathbf{c}$   | ( <b>D</b> ) $\frac{\mathbf{x}}{\mathbf{v}} = \mathbf{c}$ |

i. The value of  $\tan^{-1}\left[\sqrt{\frac{1-\cos x}{1+\cos x}}\right]$  is

(A) x (B) 
$$\frac{x}{2}$$

(C) 
$$\frac{x}{4}$$
 (D) 0

The value of  $\frac{\sin 5A - \sin 3A}{\cos 5A + \cos 3A}$  is j. (A) tan 5A **(B)** tan 3A (C) tan 2A (D) tan A

## Answer any FIVE Questions out of EIGHT Questions. Each question carries 16 marks.

- a. The sum of an infinite number of terms of a G.P. is 9 and sum of the Q.2 squares of these terms is  $\frac{81}{5}$ . Find the G.P. (8)
  - If the r<sup>th</sup> term to the expansion of  $(1 + x)^{20}$  has its coefficient equal to that b. of  $(r+4)^{\text{th}}$  term. Find r. (8)
- If  $A + B + C = \pi$ , show that  $\tan 2A + \tan 2B + \tan 2C = \tan 2A$ .tan 2B.tan **Q.3** a. 2C(8)

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- b. If a, b, c be the sides opposite to the angles A, B, C for a triangle ABC, show that  $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$ . (8)
- Q.4 a. Find the equation of a straight line when the length of perpendicular on it from the origin is given as 'p' and the inclination of this perpendicular to x-axis is given as  $\alpha$ . (8)

b. Find the angle between the straight lines 
$$y - \sqrt{3x - 5} = 0$$
 and  $\sqrt{3}y - x + 6 = 0$ . (8)

- **Q.5** a. Find the equation of the circle circumscribing the triangle formed by the lines x + y = 2, x y = 0 and 3x 4y = 6. (8)
  - b. Find the focus, vertex, latus rectum and directrix of the parabola  $(y+3)^2 = 2(x+2)$   $(4 \times 2 = 8)$

**Q.6** a. If 
$$\sin y = x \sin (a+y)$$
, show that  $\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin a}$  (8)

- b. Show that the sum of the intercepts on axes of any tangent to the curve  $\sqrt{x} + \sqrt{y} = \sqrt{a}$  is constant. (8)
- Q.7 a. Find the local maximum and minimum values of the function f(x) = (x-1) (x-2) (x-3) (4+4)

b. Evaluate 
$$\int \sqrt{\left(\frac{2+x}{2-x}\right)} dx$$
 (8)

**Q.8** a. Find the area bounded by the axis of x and the curve  $y = 1 - x^2$  (8)

b. Evaluate 
$$\int_{0}^{\pi/4} \log(1 + \tan x) dx$$
 (8)

Q.9 Solve any <u>TWO</u> of the following differential equations:-

(i) 
$$\sec^2 x \tan y dx + \sec^2 y \tan x dy = 0$$
  
(ii)  $x \frac{dy}{dx} + y = \log x$   
(iii)  $x dy - y dx = \sqrt{x^2 + y^2} dx$  (8+8)