### **Physics**

#### Time: 2 hours

The marking Scheme is (+3, -1) for question numbers 1 to 12, (+5, -1) for question numbers 13 to (+5, -2) for question numbers 21 to 32 and (+6, 0) for question numbers 33 to 40.

Given. R. = 10

 $R_2 = 2\Omega$ 









The time constants (in uS) for the circuits I, II, III are respectively

(0)

(A) 18, 8/9, 4 (C) 4, 8/9, 18 18, 4

(D)

Sol

- $\tau_1 = 8/9 \, \mu S$ τ= 18 uS
- $\tau_1 = 4 \mu S$
- 2. Two blocks A and B of masses 2m and vely, are cona massless and inextensible string. whole s is suspended by a massless spring as shown in the The magni of acceleration of A and B, immediately after the str. cut, are respedv
  - (A) g, g/2

(B) g/2, g

(C) g, g

 $a_A = g/2$ 

(D) g/2, g/2

Sol (B)



 $a_0 = g$ A point obj s places a distance of 20 cm from a thin plano-convex lens of focal

the plane surface is silvered. The image will form at

ngth 15 cm 60 cm le m left of AB

(B) 30 cm left of AB (D) 60 cm right of AB

f AB

- ⇒ v = -12 cm i.e. 12 cm left of AB

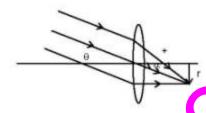


- 4. A biconvex lens of focal length f forms a circular image of sun of radius r in focal plane. Then
  - (A)  $\pi r^2 \propto f$

- (B)  $\pi r^2 \propto f^2$
- (C) if lower half part is covered by black sheet, then area of the image is equal to  $\pi r^2/2$
- (D) if f is doubled, intensity will increase
- Sol. (B)

 $r = f \tan \alpha$ 

Hence,  $\pi r^2 \propto f^2$ 



- Given a sample of Radium-226 having half-life of 4 days. Find the probability, a nucleus as the grates after 2 half lives.
  - (A) 1

(B) 1/2

(C) 1.5

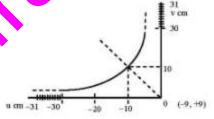
(D) 3/4

Sol. (B)

Disintegration of each nuclei is independent of any factor. Since your nuclei has same chance of disintegration.

 Graph of position of image vs position of point object from a convex lens is shown. Then, focal lengt of the lens is





Sol. (D)

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{v} \Rightarrow f = 5$$
 on

$$f = \frac{uv}{u+v}$$

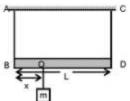
$$\frac{\Delta f}{f} = \frac{|\nabla f|}{|\nabla f|} + \frac{|\nabla f|}{|\nabla f|}$$

$$\Delta = 0.1$$

(for f = 5 cm)

The most appropriate answer is  $5.00 \pm 0.10$  cm

massless rod is suspended by two identical strings AB and CD of equal length. A block of mass m is suspended from point O such that BO is equal to 'x'. Further, it is observed that the frequency of 1st harmonic (fundamental frequency) in AB is equal to 2st harmonic frequency in CD. Then, length of BO is



(A) L/5

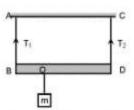
(B) 4L/5

(C) 3L/4

(D) L/4

$$T_2 = T_2/4$$

For rotational equilibrium,  $T_1x = T_2(L - x) \Rightarrow x = L/5$ 



A system of binary stars of masses m<sub>A</sub> and m<sub>B</sub> are moving in circular orbits of radii r<sub>A</sub> and r<sub>B</sub> respectively.
 T<sub>A</sub> and T<sub>B</sub> are the time periods of masses m<sub>A</sub> and m<sub>B</sub> respectively, then

$$(A) \quad \frac{T_A}{T_B} = \left(\frac{r_A}{r_B}\right)^{3/2}$$

(B) 
$$T_A > T_B$$
 (if  $r_A > r_B$ )

(D)  $T_A = T_B$ 

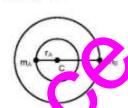
(C) 
$$T_A > T_B$$
 (if  $m_A > m_B$ )

Sol.

$$\frac{Gm_{A}m_{B}}{(r_{A}+r_{B})^{2}} = \frac{m_{A}r_{A}}{T_{A}^{2}} = \frac{m_{B}r_{B}}{T_{B}^{2}} = \frac{m_{B}r_{B}}{T_{B}^{2}}$$

$$\Rightarrow m_A r_A = m_B r_B$$

$$T_A = T_B$$



9. A solid sphere of mass M, radius R and having moment of iterticals an axis passing through the centre of mass as I, is recast into a disc of thickness t, whose moment of user about an axis passing through its edge and perpendicular to its plane remains I. Then, radius of the disc will be

$$(A)\frac{2R}{\sqrt{15}}$$

(B) 
$$R\sqrt{\frac{2}{15}}$$

(D) 
$$\frac{R}{4}$$
 [+3, -1]

SoL

$$\frac{2}{5}MR^2 = \frac{3}{2}Mr^2$$

$$r = \frac{2R}{\sqrt{15}}$$

10. A student performs an extiment for determination of  $g\left(=\frac{4\pi^2\ell}{T^2}\right)$ ,  $\ell\approx 1m$ , and he commits an error of  $\Delta\ell$ .

For T is a better time of n oscillations with the stop watch of least count ΔT and he commits a human error of a sec. For which of the following data, the measurement of g will be most accurate?

ΔΤ	n	Amplitude of oscillation
0.2 sec	10	5 mm
0.2 sec	20	5 mm
	0.2 sec	0.2 sec 10

Sol. (D)

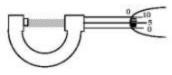
 The circular divisions of shown screw gauge are 50. It moves 0.5 mm on main scale in one rotation. The diameter of the ball is

(A) 2.25 mm

(B) 2.20 mm

(C) 1.20 mm

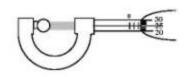
(D) 1.25 mm



Zero error =  $5 \times \frac{0.5}{50} = 0.05$  mm

Actual measurement

$$= 2 \times 0.5 \text{ mm} + 25 \times \frac{0.5}{50} - 0.05 \text{ mm}$$



12 Consider a cylindrical element as shown in the figure. Current flowing the through element is I and resistivity of material of the cylinder is ρ. Choose the correct option out the following.



- (A) Power loss in first half is four times the power loss in second half.
- (B) Voltage drop in first half is twice of voltage drop in second half.
- (C) Current density in both halves are equal.
- (D) Electric field in both halves is equal.

$$\frac{R_1}{R_2} = \frac{A_1}{A_2} = \frac{4}{1}$$

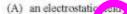
$$\frac{P_1}{P_2} = \frac{1^2 R_1}{1^2 R_2} = \frac{4}{1}$$

$$\frac{V_1}{V_2} = \frac{IR_1}{IR_2} = \frac{4}{1}$$

$$\frac{J_1}{J_2} = \frac{1}{4}$$

## More than One Choice may be correct .(+5, 1)

 In the given diagram, a line of force of particular force field is shown. Out of the following options, it can never that



(B) a magnetostatic field

(C) a gravitational fel of a mass at rest

(D) an induced electric field

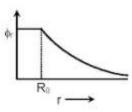


- Sol. (A), (C)
- 14. The electric potential (φ<sub>i</sub>) of a spherical symmetric system, kept at one is hown in the adjacent figure, and given as

$$\phi_1 = \frac{c_0}{4\pi \epsilon_0 r}$$

$$(r \ge R_0)$$

$$V_r = \frac{q}{4\pi \in_0 R_0} \quad (r \le R_0)$$



- Which of the following option(s) is/are correct?
- (A) For spherical region r ≤ R<sub>O</sub> total electrostatic energy stored is zero.
- (B) Within r = 2Ro, total charge is q.
- (C) There will be no charge anywhere except at r = R<sub>0</sub>.
- (D) Electric field is discontinuous at r = Ro.
- Sol. (A), (B), (C), (D)

The potential shown is for charged spherical conductor.

- A solid cylinder of mass m and radius r is rolling on a rough inclined plane of inclination θ. The coefficient of friction between the cylinder and incline is μ. Then
  - (A) frictional force is always μmg cos θ
- (B) friction is a dissipative force
- (C) by decreasing θ, frictional force decreases
- (D) friction opposes translation and supports rotation.

Sol. (C), (D)

Function x = A sin<sup>2</sup> ωt + B cos<sup>2</sup> ωt + C sin ωt cos ωt represents SHM

(B) if 
$$A = -B$$
;  $C = 2B$ , amplitude =  $B\sqrt{2}$ 

(C) if 
$$A = B$$
;  $C = 0$ 

Sol. (A), (B), (D)

$$x = \frac{A}{2}(1-\cos 2\omega t) + \frac{B}{2}(1+\cos 2\omega t) + \frac{C}{2}\sin 2\omega t$$

For 
$$A = 0$$
,  $B = 0$ 

$$x = \frac{C}{2} \sin 2\omega t$$

For 
$$A = -B$$
 and  $C = 2B$ 

$$x = B \cos 2\omega t + B \sin 2\omega t$$

Amplitude = 
$$B\sqrt{2}$$

$$x = A$$

Hence this is not correct option

For 
$$A = B$$
,  $C = 2B$ 

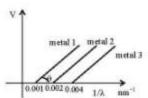
$$x = B + B \sin 2\omega t$$

It is also represents SHM.

- 17. In a dark room with ambiest temperature T<sub>0</sub>, a black body is kept at a temperature T. Keeping the temperature of the black to the temperature and the roof of the dark room. Assuming that there is no change in the ambient temperature of the room, which of the following states ent/ 150 recorrect?
  - (A) The quantity of diation absorbed by the black body in unit time will increase.
  - (B) Since missivity = absorptivity, hence the quantity of radiation emitted by black body in unit time will in page.
  - (C) Black be, radiates more energy in unit time in the visible spectrum.
  - The lected energy in unit time by the black body remains same.

Sol. (4), (B), (C), (D)

he graph between  $1/\lambda$  and stopping potential (V) of three metals having work functions  $\phi_1$ ,  $\phi_2$  and  $\phi_3$  in an experiment of photo-electric effect is plotted as shown in the figure. Which of the following statement(s) is/are correct? [Here  $\lambda$  is the wavelength of the incident ray].



- (A) Ratio of work functions φ<sub>1</sub>: φ<sub>2</sub>: φ<sub>2</sub> = 1:2:4
- (B) Ratio of work functions φ<sub>1</sub>: φ<sub>2</sub>: φ<sub>3</sub> = 4: 2: 1
- (C)  $\tan \theta$  is directly proportional to he/e, where h is Planck's constant and c is the speed of light.
- (D) The violet colour light can eject photoelectrons from metals 2 and 3.

$$\frac{hc}{\lambda} - \phi = eV$$

$$V = \frac{hc}{e\lambda} - \frac{\phi}{c}$$

plate 1: plate 2 plate 3  

$$\frac{\phi_1}{hc} = 0.001$$
  $\frac{\phi_2}{hc} = 0.002$   $\frac{\phi_3}{hc} = 0.004$ 

plate 3 
$$\frac{\phi_3}{h_0} = 0.004$$

$$\phi_1: \phi_2: \phi_3 = 1:2:4$$

For plate 2, threshold wavelength

$$\lambda = \frac{hc}{\phi_2} = \frac{hc}{0.002 \, hc} = \frac{1000}{2} = 500 \, \text{nm}$$

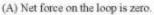
For plate 3, threshold wavelength

$$\lambda = \frac{hc}{\phi_a} = \frac{hc}{0.004hc} = \frac{1000}{4} = 250 \text{ nm}$$

Since violet colour light  $\lambda$  is 400 nm, so  $\lambda_{violet} < \lambda_{threshold}$  for plate 2

So, violet colour light will eject photo-electrons from plate 2 and not from

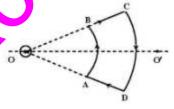
An infinite current carrying wire passes through point O and it 19 perpendicular to the plane containing a current carrying lo Al as shown in the figure. Choose the correct option (s).





(C) As seen from O, the loop rotates clockwi

(D) As seen from O, the loop rotates anticl



#### Sol (A), (C)

Magnetic force on wire BC would be p A uticalar to the plane of the loop along the outward direction and on wire DA the magnetic force would be a long the inward normal, so net force on the wire loop is zero and torque on the loop would be along the crockwise sense as seen from O.

A ball moves over fixe track is shown in the figure. From 20. A to B the ball as w hout slipping. Surface BC is frictionless KA, KB and KC are kinetic energies of the ball at A, B and C,  $\lambda$  specifically. Then (A)  $h_A \times h_C \longrightarrow K_C$ 



$$V_{\rm has} = V_{\rm has} \times K_{\rm d} > K_{\rm A}$$

$$(C_h_A = h_C, K_b = K_C$$

(D)  $h_A < h_C$ ;  $K_B > K_C$ 

$$V_A = mgh_A + K_A$$

$$E_B = K_B$$

$$E_c = mgh_2 + K_2$$

Using conservation of energy

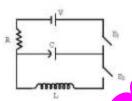
$$E_A = E_B = E_C$$

$$Mg(h_A - h_C) + (K_A - K_C) = 0$$

$$\Rightarrow h_A - h_C = \frac{K_C - K_A}{Mg}$$

### \*Comprehension-I

The capacitor of capacitance C can be charged (with the help of a resistance R) by a voltage source V, by closing switch  $S_1$  while keeping switch  $S_2$  open. The capacitor can be connected in series with an inductor 'L' by closing switch  $S_2$  and opening  $S_1$ .



- Initially, the capacitor was uncharged. Now, switch S<sub>1</sub> is closed and S<sub>2</sub> is kept open. If time constant of this circuit is τ, then
  - (A) after time interval τ, charge on the capacitor is CV/2
  - (B) after time interval 2τ, charge on the capacitor is CV(1-e<sup>-2</sup>)
  - (C) the work done by the voltage source will be half of the heat dissipated when the capacitor is fully charged.
  - (D) after time interval 2t, charge on the capacitor is CV(I-e-1)

$$Q = Q_0(1 - e^{-t/t})$$

 $Q = CV(1 - e^{-t/t})$  after time interval  $2\tau$ .

- After the capacitor gets fully charged, S<sub>1</sub> is opened and S<sub>2</sub> is closed that the inductor is connected in series
  with the capacitor. Then,
  - (A) at t = 0, energy stored in the circuit is pure in the t = 0, of magnetic energy
  - (B) at any time t > 0, current in the circuit in the time direction
  - (C) at t > 0, there is no exchange of the ben the inductor and capacitor
  - (D) at any time t > 0, instantantous cut tent true circuit may  $V\sqrt{\frac{C}{L}}$

$$q = Q_0 \cos \omega t$$

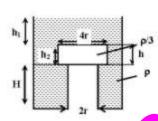
$$i = -\frac{dq}{dt} = Q_0 \omega \sin \theta$$

$$\Rightarrow i_{leas} \cdot C\omega = V \frac{C}{VL}$$

- If he total charge stored in the LC circuit is Q<sub>0</sub>, then for t ≥ 0.
  - (A) we charge on the capacitor is  $Q = Q_0 \cos\left(\frac{\pi}{2} + \frac{t}{\sqrt{LC}}\right)$
  - (B) the charge on the capacitor is  $Q = Q_0 \cos \left( \frac{\pi}{2} \frac{t}{\sqrt{LC}} \right)$
  - (C) the charge on the capacitor is  $Q = -LC \frac{d^2Q}{dt^2}$
  - (D) the charge on the capacitor is  $Q = -\frac{1}{\sqrt{LC}} \frac{d^2Q}{dt^2}$

### Comprehension-II

A wooden cylinder of diameter 4r, height h and density  $\rho/3$  is kept on a hole of diameter 2r of a tank, filled with water of density  $\rho$  as shown in the figure. The height of the base of cylinder from the base of tank is H.



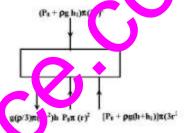
- 24. If level of liquid starts decreasing slowly when the level of liquid is at a height h<sub>1</sub> above the cylinder, the block just starts moving up. Then, value of h<sub>1</sub> is
  - (A) 2h/3

(B) 5h/4

(C) 5h/3

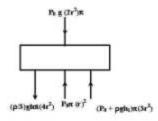
(D) 5h/2

Sol. (C) 
$$[P_0 + \rho g h_1] \pi (4r^2) + \frac{\rho}{3} \pi 4r^2 h g = [P_0 + \rho g (h_1 + h_2)] \pi (3r^2) + P_0 \pi r^2$$
 
$$h_1 = 5h/3$$



- 25. Let the cylinder is prevented from moving up, by applying a force any water level is further decreased. Then, height of water level (h<sub>2</sub> in figure) for which the cylinder remain original position without application of force is
  - (A) h/3
  - (C) 2h/3

- (B) 4h/9
- (D) h
- Sol. (B)  $P_0\pi(4r^2) + \frac{p}{3}\pi 4r^2hg = (P_0 + \mu h_2)\pi(\frac{r^2}{2}) + \frac{p}{6}\pi r^2$  $h_1 = 4h/9$



- 26. If height of vater revel is further decreased, then
  - (A cylinder) not move up and remains at its original position.
  - ( ) for . h/3, cylinder again starts moving up
  - (C) for h<sub>2</sub> = h/4, cylinder again starts moving up
  - (D) for h<sub>2</sub> = h/5 cylinder again starts moving up
- V ...
  - For h<sub>2</sub> < 4h/9 cylinder does not moves up
- 27. Two waves  $y_1 = A \cos(0.5 \pi x 100 \pi t)$

and  $y_2 = A \cos(0.46 \pi x - 92 \pi t)$  are travelling in a pipe placed along x-axis. Find the number of times intensity is maximum in time interval of 1 sec.

(A) 4

(B) 6

(C) 8

(D) 10

$$|\mathbf{f}_1 - \mathbf{f}_2| = 4 \text{ s}^{-1}$$

Find wave velocity of louder sound

(D) 96 m/s

$$v_1 = v_2 = 200 \text{ m/s}$$

29. Find the number of times  $y_1 + y_2 = 0$  at x = 0 in 1 sec

Sol. (D)

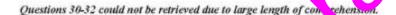
$$y_1 + y_2 = A \cos 100\pi t + A \cos 92\pi t = 0$$

$$\cos 100\pi t = -\cos 92\pi t$$

$$100\pi t = (2n+1)\pi - 92\pi t$$

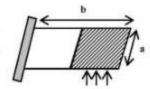
$$t = \frac{(2n+1)}{192}$$

$$\Delta t = t_{cr+1} - t_a = \frac{2}{192}$$



33. There is a rectangular plate of mass M kg of an ensions (x x b). The plate is held in horizontal position by striking it wall bar each of mass m per unit area per unit time. These are strictly in the shaded half region of the plate. The balls are colliding elastically on relocity v. What is v?

It is given n = 100, M = 3 kg, t = 0.0 kg/b = 2 m; a = 1m; g = 10 m/s².



Sol. Torque about hinge side

$$a \times \frac{b}{2}n(2 \text{ mv}) \times \frac{3b}{4} = \frac{b}{2}$$

$$2 \text{ Mg} \quad 2 \quad \text{M} \times 1$$

34. In an included vessel, 0.05 kg steam at 373 K and 0.45 kg of ice at 253 K are mixed. Then, find the final tupe, but of the mixture.

$$\Sigma \Delta Q = 0$$

Heat lost by steam to convert into 0°C water

$$H_L = 0.05 \times 540 + 0.05 \times 10 \times 1$$

$$=27+5=32$$
 kcal

Heat required by ice to change into 0°C water

$$H_g = 0.45 \times \frac{1}{2} \times 20 + 0.45 \times 80 = 4.5 + 36.00 = 40.5 \text{ kcal}$$

Thus, final temperature of mixture is 0°C.

In hydrogen-like atom (z = 11), nth line of Lyman series has wavelength λ equal to the de-Broglie's 35. wavelength of electron in the level from which it originated. What is the value of n?

Sol. 
$$\frac{1}{\lambda} = Rz^{2} \left( \frac{1}{n_{1}^{2}} - \frac{1}{n_{2}^{2}} \right)$$

$$\frac{1}{\lambda} = R(11)^{2} \left( \frac{1}{1} - \frac{1}{n^{2}} \right)$$

$$\lambda = \frac{h}{\rho} = \frac{h}{mv}$$

$$\lambda = \frac{hr}{mvr} = \frac{rh2\pi}{nh} = \frac{2\pi r}{n}.$$

$$\lambda = \frac{2\pi r}{n} = \frac{\pi(0.529 \times 10^{-10})n^{2}}{(n)(11)}$$

$$\therefore \frac{1}{\lambda} = \frac{11}{2\pi(0.529 \times 10^{-10})n} = \frac{11}{(2\pi)(0.529 \times 10^{-10})n} = 1.1 \times 10^{7} (11)^{2} \left( 1 - \frac{1}{n^{2}} \right)$$

$$= \frac{1}{(2\pi)(0.529 \times 10^{-10})(1.1 \times 10^{2})(11)} = n - \frac{1}{n}$$

$$n - \frac{1}{n} = 25$$

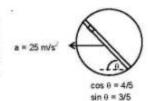
$$n^{2} - 1 = 25 n$$

$$n^{2} - 25 n - 1 = 0$$

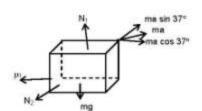
$$n = 25$$

Hence answer = 24

ter is ced horizontally. A A circular disc with a groove along its dia. 36. . q. T. co-efficient of friction block of mass 1 kg is placed as between the block and all surface of  $\infty$  in contact is  $\mu = 2/5$ . The disc has an acceleration of 2. m/s2. find he acceleration of the block with respect to disc.

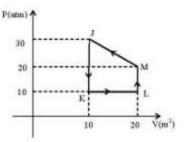


Sol. 
$$N_1 = mg$$
  
 $N_2 = m \ a \sin 37^\circ$   
 $a_{hd} = \frac{m \cos 37^\circ - \mu N_2 - \mu N_1}{m} = 10 \ m/s^2$ 



eat given to process is positive, match the following option of column I with the corresponding option of column II

Column I	Column II
(A) JK	(P) $\Delta W \ge 0$
(B) KL	$(Q) \Delta Q < 0$
(C) LM	(R) $\Delta W \leq 0$
(D) MJ	(S) $\Delta Q > 0$



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Column I		Column II
(A)	Nuclear fusion	(P) Converts some matter into energy
(B)	Nuclear fission	(Q) Generally possible for nuclei with low atomic umber
(C)	β-decay	(R) Generally possible for nuclei with higher aton ic number
(D)	Exothermic nuclear reaction	(S) Essentially proceeds by weak nuclear for

Sol. (A) 
$$\rightarrow$$
(P), (Q), (B)  $\rightarrow$ (P), (R), (C)  $\rightarrow$ (S), (P), (D)  $\rightarrow$ (P), (Q), (R)

# 39 Match the following Columns

	Column I	Column II
(A)	Dielectric ring uniformly charged	(P) The moment electrostatic field out of system
(B)	Dielectric ring uniformly charged rotating with angular velocity $\omega$	( Mag. Lac field
(C)	Constant current in ring i <sub>0</sub>	(R) induced electric field
(D)	$i = i_0 \cos \omega t$	(S) Magnetic moment

Sol. 
$$(A) \rightarrow (P)$$
,  $(B) \rightarrow (Q)$ ,  $(S)$ ,  $(C) \rightarrow (Q)$ ,  $(S)$ ,  $(S)$ ,  $(S)$ 

40. A simple telescope used the view distant objects has eyepiece and objective lens of focal lengths fe and fo, respectively. Then

Co umn 1	Column II	
(A) Intensity of the treceived by lens	(P) Radius of aperture (R)	
(B) Ang lar i agnitication	(Q) Dispersion of lens	
(C) Karoth of telescope	(R) focal length f <sub>0</sub> , f <sub>e</sub>	
(5) Sparpness of image	(S) spherical aberration	

Sol. 
$$(4) \rightarrow (1)$$
,  $(B) \rightarrow (R)$ ,  $(C) \rightarrow (R)$ ,  $(D) \rightarrow (P)$ ,  $(Q)$ ,  $(S)$