

- N.B.:** (1) Question No. 1 is **compulsory**.  
 (2) Attempt **five** questions in **all**.  
 (3) **All** parts of the **same** questions must be written in **continuation**.  
 (4) Assume suitable **data**, if **required** and state them **clearly**.

1. Answer any **four** of the following :—

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(a) Find the ROC of the given signal  
 $x(t) = 3e^{-2t} u(t) - 2e^{-t} u(t)$ .

(b) Determine the direct form - I realisation for the following transfer function  
 $H(z) = 1 - 0.7z^{-1} + 0.4z^{-2}$

(c) A linear-time invariant (LTI) system is characterized by the following difference equation :

$$y(n) = a y(n-1) + b x(n) \text{ for } 0 < a < 1$$

Find the magnitude and phase of the frequency response  $H(e^{j\omega})$  of the system.

(d) Determine the signal energy and signal power for the following signals :

(i)  $x(t) = e^{-3t}$

(ii)  $x(t) = e^{-3t}$

(e) State and explain convolution property of Z-transform.

2. (a) Consider the analog signal  $x_a(t) = 5 \sin 200\pi t$

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(i) Determine the minimum required sampling rate to avoid sampling.

(ii) Suppose that the signal is sampled at the rate  $F_s = 100$  Hz. What is the discrete time signal obtained after sampling ?

(iii) Suppose that the signal is sampled at the rate  $F_s = 300$  Hz, what is the discrete time signal obtained after sampling .

(b) Impulse response of a discrete-time LTI system is expressed as under :

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$$h(n) = \{1, 2, 3\}$$

Find the i/p sequence  $x(n)$  for output response which is given by —

$$y(n) = \{1, 1, 2, -1, 3\}.$$

3. (a) Compute the response of the system  $y(n) = 0.7y(n-1) - 0.12y(n-2) + x(n-1) + x(n-2)$  to input  $x(n) = nu(n)$ . Is the system stable? 10
- (b) Obtain the Fourier transform of a rectangular pulse of duration 2 seconds and having a magnitude of 10 volts. 10
4. (a) Find the Fourier series for the function  $x(t)$  defined by 10

$$x(t) = \begin{cases} 0 & -\frac{T}{2} < t < 0 \\ A \sin w_0 t & 0 < t < \frac{T}{2} \end{cases}$$

and  $x(t + T) = x(t)$ ,  $w_0 = \frac{2\pi}{T}$ .

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