## Karunya University

(Karunya Institute of Technology and Sciences)
(Declared as Deemed to be University under Sec. 3 of the UGC Act, 1956)

## End Semester Examination - April/May 2010

Subject Title: MECHANICS OF SOLIDS
Time: 3 hours
Subject Code: CE203
Maximum Marks: 100

## Answer ALL questions $\underline{\text { PART - A }(10 \times 1=10 \mathrm{MARKS})}$

1. State the difference between elastic limit and proportionality limits.
2. Define factor of safety.
3. What is a propped cantilever beam?
4. Define point of contra-flexure.
5. The variation of bending stresses along the neutral axis to the extreme fiber is $\qquad$ .
6. State the formula to find torsional stiffness.
7. The plane of maximum shear stress lies at $\qquad$ degrees to the plane of principal axes.
8. What does the radius of Mohr's circle represent?
9. State the limitation of Euler's formula.
10. The maximum deflection of a cantilever beam with uniformly distributed load over the entire span is
$\qquad$ -.

## $\underline{\text { PART - B }(5 \times 3=15 \text { MARKS })}$

11. A rod uniformly tapers from 15 mm to 45 mm over a length of 250 mm . Find the extension of the rod if it is subjected to an axial load of 5 kN . Take E=200GPa.
12. Prove the relation $F=\frac{d M}{d x}$, i.e. the variation of bending moment is equal to the area under the shear force diagram.
13. A close coiled helical spring is designed to have a load of 200 N and the mean diameter is 10 times the wire diameter. Find the dimensions of the spring if the maximum shear stress is limited to 80MPa.
14. Find the maximum shear stress for the state of stress consisting of two mutually perpendicular stresses 40 MPa and 30 MPa .
15. Determine the ratio of strength of a solid steel column of internal diameter equal to $3 / 4$ of its external diameter. Both columns have the same cross sectional area, length and end conditions.

## PART - C ( $5 \times 15=75$ MARKS $)$

16. A steel bar is placed between two copper bars each having same area and length as the steel bar at $20^{\circ} \mathrm{C}$. At this stage they are rigidly connected together at both ends. When the temperature is raised to $320^{\circ} \mathrm{C}$ the length of the bar increases by 1.5 mm . Find the original length and final stresses in the bar. Take $\mathrm{E}_{\text {steel }}=200 \mathrm{GPa}, \mathrm{E}_{\text {copper }}=100 \mathrm{GPa}, \alpha_{\text {steel }}=0.000012$ per $^{\circ} \mathrm{C}$ and $\alpha_{\text {copper }}=0.0000175 \operatorname{per}^{\circ} \mathrm{C}$.
(OR)
17. The fixed-end bar ABCD consists of three prismatic segments, as shown in the figure. The end segments have cross-sectional area $A_{1}=840 \mathrm{~mm}^{2}$ and length $\mathrm{L}_{1}=200 \mathrm{~mm}$. The middle segment has cross-sectional area $A_{2}=260 \mathrm{~mm}^{2}$ and length $L_{2}=250 \mathrm{~mm}$. Loads $\mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{C}}$ are equal to 25.5 kN and 17.0 kN , respectively. (a) Determine the reactions at the fixed supports. (b) Determine the compressive axial force in the middle segment of the bar.

18. A simply supported beam of length 10 m carries point load of 5 kN and 6 kN at distances of 4 m and 6 m from the left end. A uniformly distributed load of $2 \mathrm{kN} / \mathrm{m}$ acts over the entire span. Draw the shear force and bending moment diagram. Find the maximum bending moment and point of contra-flexure if any.
(OR)
19. Draw the shear force and bending moment diagram of a cantilever beam with the following force system.

20. A hollow steel tube having external and internal diameter of 120 mm and 100 mm is simply supported over a span of 5 m . The tube carries point load of W at a distance of 2 m from one of the supports. Find W if the maximum bending stress is not to exceed 100MPa.
(OR)
21. A solid steel shaft is subjected to a torque of 45 kNm . If the angle of twist is $0.5^{\circ}$ per meter length of the shaft and the shear stress is not allowed to exceed 90MPa, find (a) the suitable diameter for the shaft, (b) maximum shear stress and angle of twist and (c) maximum shear strain. Take C=80GN/m².
22. Find the principal stresses and their location. Also find the maximum shear stress and its location

23. Find the principal stress and their location using Mohr's circle for the above problem.
24. A simply supported beam has its supports 8 m apart at A and B. It carries a uniformly distributed load of $6 \mathrm{kN} / \mathrm{m}$ between A and B starting from 1 m and ending at 5 m from A. The end B of the beam has an overhang of 1 m and at the free end a concentrated load of 8 kN is applied. Find the deflection of the free end and the maximum deflection between A and B. Take $\mathrm{E}=210 \mathrm{GPa}$ and $\mathrm{I}=20 \times 10^{6} \mathrm{~mm}^{4}$.
(OR)
25. Derive the equation to find Euler's critical load for a column with both ends fixed. Assume the length of the column to be ' $l$ ' and subjected to axial load ' P '.
