

Code: DE15
Time: 3 Hours

Subject: CONTROL ENGINEERING
Max. Marks: 100

DECEMBER 2007

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q. 1. must be written in the space provided for it in the answer book supplied and nowhere else.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Q.1 Choose the correct or best alternative in the following: (2x10)

- a. The transfer function of the system is given by $G(s) = \frac{1}{s(s+1)}$ then the impulse response function is
- (A) $e^{-t} + U(t), t \geq 0$ (B) $-e^{-t} + U(t), t \geq 0$
 (C) $-e^{-t} - U(t), t \geq 0$ (D) $e^{-t} - U(t), t \geq 0$
- b. The open-loop transfer function of a feedback control system is given as $G(s)H(s) = \frac{100}{s^2 + 10s + 100}$. The gain margin of the system in decibels is
- (A) 0. (B) 10.
 (C) 20. (D) infinite.
- c. The steady-state error coefficients for a system are given by $k_p = \infty, k_v = \infty$ and $k_a = \text{finite constant}$. The system is a
- (A) Type 0 system. (B) Type one system.
 (C) Type two system. (D) Type three system.
- d. A closed loop system with unity feedback has open-loop transfer function given as $G(s) = \frac{4s^2 + 3s + 4}{s^5 + 3s^4}$. The system may have the characteristic equation having
- (A) all roots in the left half of s-plane.
 (B) all roots in the right half of s-plane.
 (C) some roots in the right half and some roots in the left half of s-plane.
 (D) all roots on the imaginary axis.
- e. Transfer function representation of a system assumes that
- (A) system inputs are unit-step type.
 (B) all initial conditions are zero.
 (C) system is stable.
 (D) system output is exponential.
- f. A system transfer function $G(s) = \frac{K}{(s+a)}$ can be represented in the Bode-plot for the values of $\omega \gg a$ by a straight line of slope
- (A) -6 dB/octave. (B) 12 dB/decade.
 (C) -30 dB/decade. (D) -20 dB/decade.
- g. A transfer function is called minimum phase if
- (A) it has all its poles and zeros in the left half of s-plane.
 (B) it has all its poles in the left half of s-plane.
 (C) it has all its poles in the left half of s-plane and zeros in the right half of s-plane.
 (D) it has all its poles and zeros in the right half of s-plane.
- h. The transfer function of a first order system is $G(s) = \frac{10}{1+2s}$. The time constant of the system is

- (A) 10 seconds. (B) $\frac{1}{10}$ second.
 (C) 2 seconds. (D) $\frac{1}{2}$ second.

i. The unit-step response of a system starting from rest is given by $C(t) = 1 - e^{-2t}$ for $t \geq 0$. The transfer function of the system is

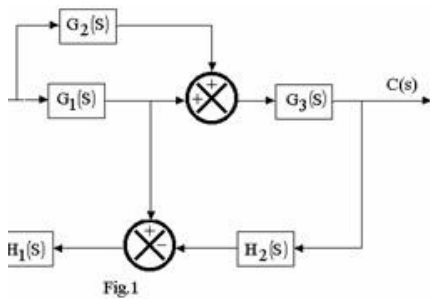
- (A) $\frac{1}{1+2s}$ (B) $\frac{2}{s+2}$
 (C) $\frac{2}{1+s}$ (D) $\frac{2s}{1+2s}$

j. The open-loop transfer function of a unity-feedback control system is given by $G(s) = \frac{1}{(s+1)(s+2)}$. The phase margin of the system is

- (A) ∞° (B) 180°
 (C) 90° (D) 45°

**Answer any FIVE Questions out of EIGHT Questions.
 Each question carries 16 marks.**

Q.2 a. Obtain the signal flow graph for the block diagram shown in Fig.1. Find the transfer function $C(s)/R(s)$ using Mason's Gain Formula. (12)



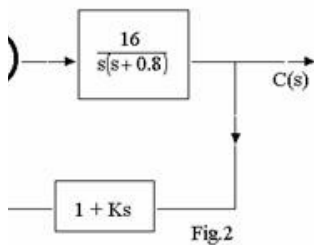
b. Discuss the effect of feedback on stability. (4)

Q.3 The open-loop transfer function of a unity feedback control system is given as $G(s) = \frac{K(s+5)(s+40)}{s^3(s+200)(s+1000)}$.

a. Using the Routh-Hurwitz criterion, determine the stability of the closed-loop system as a function of K . (10)

b. How do you determine the value of K that will cause sustained constant-amplitude oscillations in the system and the corresponding frequency of oscillation? (6)

Q.4 The block diagram of a feedback control system is given in Fig.2.



Determine the values of K such that the damping ratio ξ is 0.5. Then obtain the rise time t_r , peak time t_p , the maximum overshoot M_p and settling time t_s from the unit-step response. (16)

- Q.5** a. Determine the step, ramp and parabolic error constants of the unity-feedback control system having open-loop transfer function given as $G(s) = \frac{K}{(1+s)(1+10s)(1+20s)}$. Also determine the steady-state errors for a unit-step input, a unit ramp and a unit parabolic input $\frac{t^2}{2}U(t)$. **(10)**

- b. What is the effect of feedback on sensitivity in control system? **(6)**

- Q.6** a. Consider the unity-feedback control system whose open-loop transfer function is $G(s) = \frac{as+1}{s^2}$. Determine the value of 'a' so that the phase-margin of the system is 45° . **(8)**

- b. What do you mean by the terms

- (i) gain margin (ii) phase-margin

for a control system. How do you determine them from the Bode plot? **(8)**

- Q.7** a. State and explain Nyquist stability criterion. Distinguish between Encircled and Enclosed. **(8)**

- b. Draw the Nyquist plot for a unity feedback control system, whose open loop transfer function is given as:

$$G(s)H(s) = \frac{K}{s(s+1)}$$

comment upon the stability of system. **(8)**

- Q.8** Write short notes on any **TWO** of the following:

(i) Phase lead compensation.

(ii) LVDT.

(iii) D.C. servo-motor. **(16)**

- Q.9** a. Find the angles of the asymptotes and the intersection of the asymptotes of the root loci of the following characteristic equation of a control system when K varies from 0 to ∞ .

$$s^4 + 4s^3 + 5s^2 + (K+10)s + K = 0 \quad \mathbf{(8)}$$

- b. Explain the terms conditionally stable and marginally stable control systems. **(8)**