AIEEE-2011 (Set -Q)

13.

IMPORTANT INSTRUCTIONS

- 1. Immediately fill in the particulars on this page of the Test Booklet with Blue/Black Ball Point Pen. Use of Pencil is strictly prohibited. 2. The Answer Sheet is kept inside the Test Booklet. When you are directed to open the Test Booklet, take
- 3. The test is of **3 hours** duration. The Test Booklet consists of 90 questions. The maximum marks are 360. 4.
- There are three parts in the question paper A, B, C consisting of Physics, Mathematics, Chemistry having 5. 30 questions in each part of equal weight age. Each question is allotted 4(four) marks for each correct

out the Answer Sheet and fill in the particulars carefully.

- response. Candidates will be awarded marks as stated above in instruction No. 5 for correct response of each 6. question ¼ (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
- 7. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above. Use Blue/Black Ball Point Pen only for writing particulars/marking responses on Side-1 and Side-2 of the 8.
- Answer Sheet. Use of pencil is strictly prohibited. 9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc., except the Admit Card inside the examination hall/room.
- 10. Rough work is to be done on the space provided for this purpose in the Test Booklet only. This space is given at the bottom of each page and in 3 pages (Pages 21 - 23) at the end of the booklet.
- 11. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the
- Room/Hall, However, the candidates are allowed to take away this Test Booklet with them. 12. The CODE for this Booklet is Q. Make sure that the CODE printed on **Side-2** of the Answer Sheet is the
 - same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to

the Invigilator for replacement of both the Test Booklet and the Answer Sheet.

Do not fold or make any stray marks on the Answer Sheet.

4.

5.

6.

8.

(1) $V \propto X^{-1}$

This represents a

PART A: PHYSICS

The transverse displacement y(x,t) of a wave on a string is given by $y(x,t) = e^{-(ax^2+bt^2+2\sqrt{ab}\,xt)}$ 1.

(1) wave moving in – x direction with speed
$$\sqrt{\frac{b}{a}}$$
 (2) standing wave of frequency \sqrt{b}

(3) standing wave of frequency
$$\frac{1}{\sqrt{b}}$$
 (4) wave moving in + x direction with $\sqrt{\frac{a}{b}}$

2. A screw gauge gives the following reading when used to measure the diameter of a wire. Main scale reading: 0 mm

Circular scale reading: 52 divisions

Given that 1 mm on main scale corresponds to 100 divisions of the circular scale. The diameter of wire from the above date is: (4) 0.52 cm (1) 0.052 cm (2) 0.026 cm (3) 0.005 cm

mass m, if the string does not slip on the pulley, is
(1) g
(2)
$$\frac{2}{3}$$
g
(3) $\frac{9}{3}$

(1)
$$0.2\pi \text{ mJ}$$
 (2) $2\pi \text{ mJ}$ (3) $0.4 \pi \text{ mJ}$ (4) $4\pi \text{ mJ}$

x-axis. Their mean position is separated by distance
$$X_0(X_0 > A)$$
. If the maximum separation between them is $(X_0 + A)$, the phase difference between their motion is :

(2) $\frac{\pi}{4}$

line joining them where the gravitational field is zero is:

(1)
$$-\frac{4Gm}{}$$
 (2) $-\frac{6Gm}{}$ (3) $-\frac{9Gm}{}$ (4) zero

(1)
$$-\frac{4Gm}{r}$$
 (2) $-\frac{6Gm}{r}$ (3) $-\frac{9Gm}{r}$ (4) zero

Two identical charged spheres suspended from a common point by two massless strings of length I are initially a distance d(d << 1) apart because of their mutual repulsion. The charge begins to leak from

both the spheres at a constant rate. As a result the charges approach each other with a velocity v. Then as a function of distance x between them,

(1)
$$v \propto x^{-1}$$
 (2) $v \propto x^{1/2}$ (3) $v \propto x$ (4) $v \propto x^{-1/2}$

(3) $v \propto x$

(3) $\frac{\pi}{6}$

(4) $\frac{\pi}{2}$

magnitude of the induced emf in the wire of aerial is: (1) 0.75 mV (2) 0.50 mV (3) 0.15 mV (4) 1 mV 10. An object, moving with a speed of 6.25 m/s, is decelerated at a rate given by : $\frac{dV}{dt} = -2.5\sqrt{V}$

9.

13.

A boat is moving due east in a region where the earth's magnetic field is 5.0×10⁻⁵NA⁻¹m⁻¹ due north and

horizontal. The boat carries a vertical aerial 2m long. If the speed of the boat is 1.50 ms⁻¹, the

11. A fully charged capacitor C with initial charge q_0 is connected to a coil of self inductance L at t = 0. The time at which the energy is stored equally between the electric and the magnetic field is :

(1)
$$\frac{\pi}{4}\sqrt{\text{LC}}$$
 (2) $2\pi\sqrt{\text{LC}}$ (3) $\sqrt{\text{LC}}$ (4) $\pi\sqrt{\text{LC}}$

Let the x – z plane be the boundary between two transparent media. Medium 1 in $z \ge 0$ has a refractive 12. index of $\sqrt{2}$ and medium 2 with z < 0 has a refractive index of $\sqrt{3}$. A ray of light in medium 1 given by

index of
$$\sqrt{2}$$
 and medium 2 with $z < 0$ has a refractive index of $\sqrt{3}$. A ray of light in medium 1 given by the vector $\vec{A} = 6\sqrt{3}\,\hat{i} + 8\sqrt{3}\,\hat{j} - 10\,\hat{k}$ is incident on the plane of separation. The angle of refraction in medium 2 is

 $(3) 75^{\circ}$ $(2) 60^{\circ}$ $(4) 30^{\circ}$ (1) 45° A current I flows in an infinitely long wire with cross section in the form of a semicircular ring of radius R. The magnitude of the magnetic induction along its axis is

The magnitude of the magnetic induction along its axis is
$$(1) \frac{\mu_0 I}{2\pi^2 R} \qquad \qquad (2) \frac{\mu_0 I}{2\pi R} \qquad \qquad (3) \frac{\mu_0 I}{4\pi^2 R} \qquad \qquad (4) \frac{\mu_0 I}{\pi^2 R}$$

14. A thermally insulated vessel contains an ideal gas of molecular mass M and ratio of specific heats γ. It is moving with speed υ and is suddenly brought to rest. Assuming no heat is lost to the surroundings, its

moving with speed
$$\upsilon$$
 and is suddenly brought to rest. Assuming no heat is lost to the surroundings, its temperature increases by :

(1) $\frac{(\gamma-1)}{2\nu R} M\upsilon^2 K$

(2) $\frac{\gamma M\upsilon^2}{2R} K$

(3) $\frac{(\gamma-1)}{2R} M\upsilon^2 K$

(4) $\frac{(\gamma-1)}{2(\gamma+1)R} M\upsilon^2 K$

15. A mass M, attached to a horizontal spring, executes S.H.M. with amplitude A₁. When the mass M passes through its mean position then a smaller mass m is placed over it and both of them move together with

amplitude A₂. The ratio of
$$\left(\frac{A_1}{A_2}\right)$$
 is:

(1) $\frac{M+m}{M}$ (2) $\left(\frac{M}{M+m}\right)^{1/2}$ (3) $\left(\frac{M+m}{M}\right)^{1/2}$ (4) $\frac{M}{M+m}$

Water is flowing continuously from a tap having an internal diameter 8×10⁻³ m. The water velocity as it 16. leaves the tap is 0.4 ms⁻¹. The diameter of the water stream at a distance 2×10⁻¹m below the lap is

close to: (3) 3.6×10^{-3} m (2) 9.6×10^{-3} m (1) 7.5×10^{-3} m (4) 5.0×10^{-3} m

18.

19.

20.

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23.

choose the one that best describes the two statements. Statement-1: Sky wave signals are used for long distance radio communication. These signals are in general, less stable than ground wave signals. **Statement-2**: The state of ionosphere varies from hour to hour, day to day and season to season.

This question has Statement – 1 and Statement – 2. Of the four choices given after the statements,

(1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1. (2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1. (3) Statement-1 is false, Statement-2 is true.

(4) Statement-1 is true, Statement-2 is false. Three perfect gases at absolute temperatures T₁, T₂ and T₃ are mixed. The masses of molecules are m₁,

final temperature of the mixture is:

(1) more than 3 but less than 6

(3) more than 9

(1) $1.7 \times 10^5 \Omega$

Direction:

 $(1) \ \frac{n_1T_1+n_2T_2+n_3T_3}{n_1+n_2+n_3} \quad (2) \ \frac{n_1T_1+n_2T_2^2+n_3T_3^2}{n_1T_1+n_2T_2+n_3T_3} \quad (3) \ \frac{n_1^2T_1^2+n_2^2T_2^2+n_3^2T_3^2}{n_1T_1+n_2T_2+n_3T_3} \quad (4) \ \frac{(T_1+T_2+T_3)}{3}$

m₂ and m₃ and the number of molecules are n₁, n₂ and n₃ respectively. Assuming no loss of energy, the

pulley before its direction of motion if reversed, is :

after the switch has been closed. $(log_{10} 2.5 = 0.4)$

(2) $2.7 \times 10^6 \Omega$

If a wire is stretched to make it 0.1% longer, its resistance will:

(4) less than 3

A pulley of radius 2 m is rotated about its axis by a force $F = (20t - 5t^2)$ Newton (where t is measured in

seconds) applied tangentially. If the moment of inertia of the pulley about its axis of rotation made by the

(2) more than 6 but less than 9 A resistor 'R' and 2µF capacitor in series is connected through a switch to 200 V direct supply. Across

the capacitor is a neon bulb that lights up at 120 V. Calculate the value of R to make the bulb light up 5 s (3) $3.3 \times 10^7 \Omega$ (4) $1.3 \times 10^4 \Omega$

A Carnot engine operating between temperatures T_1 and T_2 has efficiency $\frac{1}{6}$. When T_2 is lowered by 62 K, its efficiency increases to $\frac{1}{3}$. Then T₁ and T₂ are, respectively : (1) 372 K and 330 K (2) 330 K and 268 K (3) 310 K and 248 K (4) 372 K and 310 K

(1) increase by 0.2% (2) decrease by 0.2% (3) decrease by 0.05% (4) increases by 0.05%

The question has a paragraph followed by two statements, Statement -1 and statement -2. Of the given four alternatives after the statements, choose the one that describes the statements. A thin air film is formed by putting the convex surface of a plane - convex lens over a plane glass plate. With monochromatic light, this film gives an interference pattern due to light reflected from the top (convex) surface and the bottom (glass plate) surface of the film. Statement-1: When light reflects from the air-glass plate interface, the reflected wave suffers a phase change of π .

Statement-2: The centre of the interference pattern is dark. (1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1. (2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1. (3) Statement-1 is false, Statement-2 is true. (4) Statement-1 is true, Statement-2 is false.

seen in the mirror of the first one is:

24.

25.

26.

27.

28.

29.

30.

(1) $\frac{1}{15}$ m/s Energy required for the electron excitation in Li⁺⁺ from the first to the third Bohr orbit is (1) 36.3 eV

(1) −6aε_or

(1) $\pi \frac{V^4}{Q^2}$

(1) 8.4 kJ

(1) 14 min

(2) 108.8 eV

(2) $-24\pi a \epsilon_0 r$

fountain is v, the total area around the fountain that gets wet is:

(2) $\frac{\pi}{2} \frac{v^4}{\sigma^2}$

internal energy is (specific heat of water is 4148 J/kg/K):

(2) 84 kJ

(2) 20 min

surface are linearly dependent on the frequency of incident light.

choose the one that best describes the two statements.

(3) Statement-1 is false, Statement-2 is true. (4) Statement-1 is true, Statement-2 is false.

the time t_2 when $\frac{2}{3}$ of it has decayed and time t_1 and $\frac{1}{3}$ of it had decayed is :

frequency incident on the surface doubled, both the K_{max} and V_0 are also doubled.

(2) 10m/s

(3) 122.4 eV The electrostatic potential inside a charged spherical ball is given by $\phi = \alpha \rho^2 + b$ where r is the distance

(3) $-6a\varepsilon_0$

100g of water is heated from 30°C to 50°C. Ignoring the slight expansion of the water, the change in its

The half life of a radioactive substance is 20 minutes. The approximate time interval $(t_2 - t_1)$ between

This question has Statement – 1 and Statement – 2. Of the four choices given after the statements,

Statement-1: A metallic surface is irradiated by a monochromatic light of frequency v > v₀ (the threshold frequency). The maximum kinetic energy and the stopping potential are K_{max} and V₀ respectively. If the

Statement-2: The maximum kinetic energy and the stopping potential of photoelectrons emitted from a

(1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1. (2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1.

(3) 28 min

(3) 2.1 kJ

A car is fitted with a convex side-view mirror of focal length 20cm. A second car 2.8 m behind the first car is overtaking the first car at relative speed of 15 m/s. The speed of the image of the second car as

(3) 15m/s

from the centre; a, b are constants. Then the charge density inside ball is

(4) $\pi \frac{v^4}{c}$

(4) 4.2 kJ

(4) 7 min

A water fountain on the ground sprinkles water all around it. If the speed of water coming out of the

(4) $\frac{1}{10}$ m/s

(4) 12.1 eV

(4) –24πaε_∘r

PART B: MATHEMATICS

The lines $L_1: y-x=0$ and $L_2: 2x+y=0$ intersect the line $L_3: y+2=0$ at P and Q respectively. The

bisector of the acute angle between
$$L_1$$
 and L_2 intersect L_3 at R .

The ratio PR: RQ equals $2\sqrt{2}:\sqrt{5}$. Statement - 1 :

- In any triangle, bisector of an angle divides the triangle into two similar triangles. Statement – 2 : (1) Statement – 1 is true, Statement – 2 is true; Statement – 2 is not a correct explanation for Statement
 - _ 1 (2) Statement – 1 is true, Statement – 2 is false.
 - (3) Statement 1 is false, Statement– 2 is true.
 - (4) Statement 1 is true, Statement 2 is true; Statement 2 is a correct explanation for Statement 1

If
$$A = \sin^2 x + \cos^4 x$$
, then for all real x

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31.

32.

33.

35.

36.

(1) - 132

(1) equals $\sqrt{2}$

_ 1

 $\frac{d^2x}{dv^2}$ equals

 $\lim_{x \to 2} \left| \frac{\sqrt{1 - \cos\{2(x - 2)\}}}{x - 2} \right|$

- $(1) \frac{13}{16} \le A \le 1$
 - (2) 1≤ A ≤ 2

(2) equals $-\sqrt{2}$

box is empty is 9C3

(2) Statement - 1 is true, Statement - 2 is false. (3) Statement – 1 is false, Statement– 2 is true.

- The coefficient of x^7 in the expansion of $\left(1-x-x^2+x^3\right)$

(3) equals $\frac{1}{\sqrt{2}}$

The number of ways of choosing any 3 places from 9 different places is ${}^9\mathrm{C}_3$.

(1) Statement – 1 is true, Statement – 2 is true; Statement – 2 is not a correct explanation for Statement

(4) Statement – 1 is true, Statement – 2 is true; Statement – 2 is a correct explanation for Statement – 1

 $(1) - \left(\frac{d^2y}{dx^2}\right)^{-1} \left(\frac{dy}{dx}\right)^{-3} \qquad (2) \left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-2} \qquad (3) - \left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-3} \qquad (4) \left(\frac{d^2y}{dx^2}\right)^{-1}$

The number of ways of distributing 10 identical balls in 4 distinct boxes such that no

- (4) 144
- (4) $\frac{3}{4} \le A \le 1$

(4) does not exist

7. If
$$\frac{dy}{dx} = y + 3 > 0$$
 and $y(0) = 2$, then $y(\ln 2)$ is equal to
(1) 5 (2) 13 (3) -2

39.

40.

41.

42.

44.

(2) Statement – 1 is true, Statement – 2 is false. (3) Statement – 1 is false, Statement– 2 is true.

(2) $\frac{\pi}{2}$ log2

one failure is greater than or equal to $\frac{31}{32}$, then p lies in the interval

(2) 20 months

The value of $\int_{-1}^{1} \frac{8 \log(1+x)}{1+x^2} dx$ is

Rez = 1, then it is necessary that

the start of service will be Rs. 11040 after

The domain of the function $f(x) = \frac{1}{\sqrt{|x| - x}}$ is

(2) $\frac{2}{5}$

 $(1) \frac{\pi}{8} \log 2$

(1) $\beta \in (-1, 0)$

 $(1) \left[\frac{3}{4}, \frac{11}{12} \right]$

(1) 19 months

(1) (0, ∞)

equals $(1) \frac{3}{2}$

Let R be the set of real numbers
$$\text{Statement} = 1 \quad : \quad A = \{(x,y) \in R \times R : y - x \text{ is an integer} \} \text{ is an equivalence relation on } R .$$

Statement -2: $B = \{(x, y) \in R \times R : x = \alpha y \text{ for some rational number } \alpha\}$ is an equivalence relation on

(1) Statement - 1 is true, Statement - 2 is true; Statement - 2 is not a correct explanation for Statement

(4) Statement – 1 is true, Statement – 2 is true; Statement – 2 is a correct explanation for Statement – 1

(3) log2

Let α , β be real and z be a complex number. If $z^2 + \alpha z + \beta = 0$ has two distinct roots on the line

Consider 5 independent Bernoulli's trials each with probability of success p. If the probability of at least

A man saves Rs. 200 in each of the first three months of his service. In each of the subsequent months

his saving increases by Rs. 40 more than the saving of immediately previous month. His total saving from

(3) 21 months

(2) $\left(-\infty, 0\right)$ (3) $\left(-\infty, \infty\right) - \left\{0\right\}$ (4) $\left(-\infty, \infty\right)$

If the angle between the line $x = \frac{y-1}{2} = \frac{z-3}{\lambda}$ and the plane x+2y+3z=4 is $\cos^{-1}\left(\sqrt{\frac{5}{14}}\right)$, then λ

(3) $\frac{5}{3}$

(3) $\beta \in (1, \infty)$

(3) $\left[\frac{11}{12}, 1\right]$ (4) $\left[\frac{1}{2}, \frac{3}{4}\right]$

(4) πlog2

(4) 18 months

 $(4) \frac{2}{3}$

(4) $\beta \in (0, 1)$

(1) -3

45.

47.

50.

(1) $\frac{3\sqrt{2}}{8}$

Equation of the ellipse whose axes are the axes of coordinates and which passes through the point 46. (-3, 1) and has eccentricity $\sqrt{\frac{2}{5}}$ is

(3)3

(4) -5

 $(4) \frac{\sqrt{3}}{4}$

If $\vec{a} = \frac{1}{\sqrt{10}} (3\hat{i} + \hat{k})$ and $\vec{b} = \frac{1}{7} (2\hat{i} + 3\hat{j} - 6\hat{k})$, then the value of $(2\vec{a} - \vec{b}) \cdot [(\vec{a} \times \vec{b}) \times (\vec{a} + 2\vec{b})]$ is

(2)5

(1)
$$5x^2 + 3y^2 - 48 = 0$$
 (2) $3x^2 + 5y^2 - 15 = 0$ (3) $5x^2 + 3y^2 - 32 = 0$ (4) $3x^2 + 5y^2 - 32 = 0$
Let I be the purchase value of an equipment and $V(t)$ be the value after it has been used for t years $dV(t)$

The value V(t) depreciates at a rate given by differential equation $\frac{dV(t)}{dt} = -k(T-t)$, where k > 0 is a constant and T is the total life in years of the equipment. Then the scrap value V(T) of the equipment is (2) $1 - \frac{k(T-t)^2}{2}$ (1) $1 - \frac{kT^2}{2}$ (3) e^{-kT} (4) $T^2 - \frac{1}{k}$

The vector
$$\vec{a}$$
 and \vec{b} are not perpendicular and \vec{c} and \vec{d} are two vectors satisfying: $\vec{b} \times \vec{c} = \vec{b} \times \vec{d}$ and $\vec{a}.\vec{d} = 0$. Then the vector \vec{d} is equal to
$$(1) \ \vec{c} + \left(\frac{\vec{a}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{b} \qquad (2) \ \vec{b} + \left(\frac{\vec{b}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{c} \qquad (3) \ \vec{c} - \left(\frac{\vec{a}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{b} \qquad (4) \ \vec{b} - \left(\frac{\vec{b}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{c}$$

The two circles $x^2 + y^2 = ax$ and $x^2 + y^2 = c^2(c > 0)$ touch each other if 49. (2) a = 2c (3) |a| = 2c(4) 2|a| = c (1) |a| = c

If C and D are two events such that
$$C \subset D$$
 and $P(D) \neq 0$, then the correct statement among the following is

(1)
$$P(C|D) \ge P(C)$$
 (2) $P(C|D) < P(C)$ (3) $P(C|D) = \frac{P(D)}{P(C)}$ (4) $P(C|D) = P(C)$

51. The number of values of k for which the linear equations

4x + ky + 2z = 0; kx + 4y + z = 0; 2x + 2y + z = 0 possess a non-zero solution is (1).2(3) zero (4) 3

The negation of the statement "Suman is brilliant and dishonest if and only if Suman is rich" can be expressed as

 $(1) \sim \left(\mathsf{Q} \leftrightarrow \left(\mathsf{P} \wedge \sim \mathsf{R} \right) \right) \quad (2) \sim \mathsf{Q} \leftrightarrow \sim \mathsf{P} \wedge \mathsf{R} \\ \qquad (3) \sim \left(\mathsf{P} \wedge \sim \mathsf{R} \right) \leftrightarrow \mathsf{Q} \\ \qquad (4) \sim \mathsf{P} \wedge \left(\mathsf{Q} \leftrightarrow \sim \mathsf{R} \right)$ The shortest distance between line y - x = 1 and curve $x = y^2$ is 53.

(2) $\frac{8}{3\sqrt{2}}$

(3) $\frac{4}{\sqrt{3}}$

(1) 3(2)4(4) 2Statement -1: The point A(1, 0, 7) is the mirror image of the point B(1, 6, 3) in the line

If the mean deviation about the median of the numbers a, 2a, ..., 50a is 50, then |a| equals

54.

55.

57.

60.

$$\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}.$$
Statement - 2: The line: $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$ bisects the line segment joining A(1, 0, 7) and B(1, 6, 3).

(1) Statement – 1 is true, Statement–2 is true; Statement–2 is not a correct explanation for Statement – 1 (2) Statement – 1 is true, Statement– 2 is false.

(3) Statement – 1 is false, Statement – 2 is true. (4) Statement – 1 is true, Statement – 2 is true; Statement – 2 is a correct explanation for Statement – 1

56. Let A and B be two symmetric matrices of order 3. A(BA) and (AB) A are symmetric matrices. Statement – 1 : Statement – 2 : AB is symmetric matrix if matrix multiplication of A and B is commutative. (1) Statement – 1 is true, Statement – 2 is true; Statement – 2 is not a correct explanation for Statement

_1 (2) Statement – 1 is true, Statement– 2 is false. (3) Statement – 1 is false, Statement– 2 is true.

(4) Statement – 1 is true, Statement – 2 is true; Statement – 2 is a correct explanation for Statement – 1

If $\omega(\neq 1)$ is a cube root of unity, and $(1+\omega)' = A + B\omega$. Then (A, B) equals (2)(1,0)(3)(-1,1)(1)(1,1)(4) (0, 1)

The value of p and q for which the function $f\left(x\right) = \begin{cases} \frac{sin(p+1)x + sinx}{x} &, & x < 0 \\ q &, & x = 0 \\ \frac{\sqrt{x + x^2} - \sqrt{x}}{x^{3/2}} &, & x > 0 \end{cases}$ 58.

is continuous for all x in R, is (1) $p = \frac{5}{3}, q = \frac{1}{3}$ (2) $p = -\frac{3}{3}, q = \frac{1}{3}$ (3) $p = \frac{1}{3}, q = \frac{3}{3}$ (4) $p = \frac{1}{3}, q = -\frac{3}{3}$

The area of the region enclosed by the curves y = x, x = e, $y = \frac{1}{x}$ and the positive x-axis is

59. (1) 1 square units (2) $\frac{3}{2}$ square units (3) $\frac{5}{2}$ square units (4) $\frac{1}{2}$ square units

For $x \in \left(0, \frac{5\pi}{2}\right)$, define $f(x) = \hat{\int} \sqrt{t} \sin t \, dt$. Then f has (1) local minimum at π and 2π

(2) local minimum at π and local maximum at 2π (3) local maximum at π and local minimum at 2π (4) local maximum at π and 2π

64.

65.

66.

67.

68.

69.

70.

71.

reaction is:

(1) HCOOH

expression:

(1) 3 atm

(1) BH₄

(3) CICH, CH, CH, COOH

(1) 2-Butanone

(1) $p(H_2) = 1$ atm and $[H^+] = 1.0$ M

(1) a and b for $Cl_2 < a$ and b for C_2H_6

(4) a and b for $Cl_2 > a$ and b for C_2H_6

The complex is paramagnetic

(2) a for $Cl_2 < a$ for C_2H_6 but b for $Cl_2 > b$ for C_2H_6 (3) a for $Cl_2 > a$ for C_2H_6 but b for $Cl_2 < b$ for C_2H_6

(2) 0.3 atm

Boron cannot form which one of the following anions?

61. Among the following the maximum covalent character is shown by the compound :

The presence or absence of hydroxyl group on which carbon atom of sugar differentiates RNA and DNA

 $(1) 2^{nd}$ (3) 4th (4) 1st (2) 3rd 63.

Trichloroacetaldehyde was subjected to Cannizzaro's reaction by using NaOH. The mixture of the

products contains sodium trichloroacetate and another compound. The other compound is (1) Trichloromethanol (2) 2, 2, 2-Trichloropropanol

(4) 2, 2, 2-Trichloroethanol (3) Chloroform

(3) $p(H_2) = 2$ atm and $[H^+] = 2.0 \text{ M}$ (4) $p(H_2) = 1$ atm and $[H^+] = 2.0 \text{ M}$

(2) Ethyl chloride

The reduction potential of hydrogen half cell will be negative if :

The strongest acid amongst the following compounds is:

(1) SnCl₂ (2) AICI₃ (3) MgCl₂

Sodium ethoxide has reacted with ethanoyl chloride. The compound that is produced in the above

(3) Ethyl ethanoate (4) Diethyl ether

(2) $p(H_2) = 2$ atm and $[H^+] = 1.0$ M

(2) CH₃CH₂CH(CI)CO₂H

(4) CH₂COOH

The degree of dissociation (α) of a weak electrolyte, $A_{\nu}B_{\nu}$ is related to van't Hoff factor (i) by the

`a' and `b' are van der Waals' constants for gases. Chlorine is more easily liquefied than ethane because

A vessel at 1000 K contains CO2 with a pressure of 0.5 atm. Some of the CO2 is converted into CO on

(3) 0.18 atm

(4) 1.8 atm

(4) BF₆³⁻

(2) The complex is an outer orbital complex

(1) $\alpha = \frac{i-1}{x+y+1}$ (2) $\alpha = \frac{x+y-1}{i-1}$ (3) $\alpha = \frac{x+y+1}{i-1}$ (4) $\alpha = \frac{i-1}{(x+y-1)}$

the addition of graphite. If the total pressure at equilibrium is 0.8 atm, the value of K is

(2) $B(OH)_4^-$ (3) BO_2^-

Which of the following facts about the complex $\left[\text{Cr} \left(\text{NH}_{3} \right)_{\epsilon} \right] \text{Cl}_{3}$ s wrong?

(3) The complex gives white precipitate with silver nitrate solution (4) The complex involves d²sp³ hybridization and is octahedral in shape.

PART C: CHEMISTRY

(4) 804.32g

(4) sp. sp^{2} , sp^{3}

73. Which one of the following order represents the correct sequence of the increasing basic nature of the given oxides? (1) $MgO < K_2O < Al_2O_3 < Na_2O$ (2) $Na_2O < K_2O < MgO < Al_2O_3$ (3) $K_2O < Na_2O < Al_2O_3 < MgO$ (4) $Al_2O_3 < MgO < Na_2O < K_2O$ The rate of a chemical reaction doubles for every 10°C rise of temperature. If the temperature is raised 74. by 50°C, the rate of the reaction increases by about : (4) 10 times (1) 24 times (2) 32 times (3) 64 times

Ethylene glycol is used as an antifreeze in a cold climate. Mass of ethylene glycol which should be

(3) 304.60 g

added to 4 kg of water to prevent it from freezing at -6°C will be:

(2) 400.00 g

 $[K_r]$ for water = 1.86 K kg mol⁻¹, and molar mass of ethylene glycol = 62g mol⁻¹)

72.

77.

81.

82.

(1) 204.30g

(1) sp^2 , sp, sp^3

- The magnetic moment (spin only) of $[NiCl_4]^{2-}$ is (1) 5.46 BM (2) 2.83 BM (4) 1.82 BM (3) 1.41 BM
- 75. The hybridization of orbitals of N atom in NO₃, NO₂ and NH₄ are respectively: 76.
 - (2) sp, sp^3, sp^2 (3) sp^2, sp^3, sp^3 In context of the lanthanoids, which of the following statements is not correct? (1) All the members exhibit +3 oxidation state (2) Because of similar properties the separation of lanthanoids is not easy.
 - (3) Availability of 4f electrons results in the formation of compounds in +4 state for all the members (4) There is a gradual decrease in the radii of the members with increasing atomic number in the
 - series.
- 78. A 5.2 molal aqueous solution of methyl alcohol, CH₂OH, is supplied. What is the mole fraction of methyl alcohol in the solution? (2) 0.086(3) 0.050(1) 0.190 (4) 0.100
- 79. Which of the following statement is wrong? (1) Nitrogen cannot form $d\pi - p\pi$ bond.
 - (2) Single N- N bond is weaker than the single P P bond, (3) N₂O₄ has two resonance structures
 - (4) The stability of hydrides increases from NH, to BiH, in group 15 of the periodic table
- 80.

(2) At 600°C the gas mainly consists of S₂ molecules

- The outer electron configuration of Gd (Atomic No : 64 is : (1) 4f⁸ 5d⁰ 6s² (4) 4f³ 4d⁵ 6s² (2) $4f^4 5d^4 6s^2$ (3) $4f^7 5d^1 6s^2$
- Which of the following statements regarding sulphur is incorrect? The vapour at 200°C consists mostly of S₈ rings
- (3) The oxidation state of sulphur is never less than +4 in its compounds (4) S₂ molecule is paramagnetic.
 - The structure of IF, is: (1) trigonal bipyramid (2) octahedral (3) pentagonal bipyramid (4) square pyramid

AIEEE-2011-12 83. Ozonolysis of an organic compound gives formaldehyde as one of the products. This confirms the presence of :

(1) a vinyl group

(3) an acetylenic triple bond

84. A gas absorbs a photon of 355 nm and emits at two wavelengths. If one of the emissions is at 680 nm, the other is at : (1) 325 nm (4) 1035 nm (2) 743 nm (3) 518 nm

(2) an isopropyl group

(4) two ethylenic double bonds

Silver Mirror test is given by which one of the following compounds? 85. (2) Formaldehyde (1) Acetone (3) Benzophenone (4) Acetaldehyde

86. Which of the following reagents may be used to distinguish between phenol and benzoic acid? (1) Tollen's reagent (2) Molisch reagent (4) Aqueous NaOH (3) Neutral Fe Cl.

Phenol is heated with a solution of mixture of KBr and KBrO₃. The major product obtained in the above 87. reaction is

(3) 2, 4, 6- Tribromophenol (1) 3-Bromophenol (2) 4-Bromophenol (4) 2-Bromophenol In a face centred cubic lattice, atom A occupies the corner positions and atom B occupies the face centre 88. positions. If one atom of B is missing from one of the face centred points, the formula of the compound is

(3) A₂B₅ (1) AB₂ (4) A₂B

The entropy change involved in the isothermal reversible expansion of 2 moles of an ideal gas from a 89. volume of 10 dm3 to a volume of 100 dm3 at 27°C is: (1) 35.8J mol -1K-1 (2) 32.3J mol⁻¹K⁻¹ (3) 42.3J mol⁻¹K⁻¹ (4) 38.3J mol⁻¹K⁻¹

Identify the compound that exhibits tautomerism. 90. (4) 2- Butene

(1) Lactic acid (2) 2-Pentanone (3) Phenol

The candidates should fill in the required particulars on the Test Booklet and Answer Sheet (Side-1) with

1.

4.

5.

6.

7.

8.

Blue/Black Ball Point Pen.

READ THE FOLLOWING INSTRUCTIONS CAREFULLY

- For writing/marking particulars on Side-2 of the Answer Sheet, use Blue/Black Ball Point Pen only 2.
- The candidates should not write their Roll Numbers anywhere else (except in the specified space) on the 3.
- Test Booklet/Answer Sheet.
- Out of the four options given for each question, only one option is the correct answer.
- For each incorrect response, one-fourth (1/4) of the total marks allotted to the question would be deducted
- from the total score. No deduction from the total score, however, will be made if no response is indicated for an item in the Answer Sheet.
- Handle the Test Booklet and Answer Sheet with care, as under no circumstances (except for discrepancy in Test Booklet Code and Answer Sheet Code), will another set be provided.
- The candidates are not allowed to do any rough work or writing work on the Answer Sheet. All calculations/writing work are to be done in the space provided for this purpose in the Test Booklet itself,
- 23) at the end of the booklet.
- Room/Hall. However, the candidates are allowed to take away this Test Booklet with them.

marked 'Space for Rough Work'. This space is given at the bottom of each page and in 4 pages (Pages 20 -

On completion of the test, the candidates must hand over the Answer Sheet to the Invigilator on duty in the

- Each candidate must show on demand his/her Admit Card to the Invigilator. 9.
- 10. No candidate, without special permission of the Superintendent or Invigilator, should leave his/her seat.
- The candidates should not leave the Examination Hall without handing over their Answer Sheet to the 11. Invigilator on duty and sign the Attendance Sheet again. Cases where a candidate has not signed the Attendance Sheet a second time will be deemed not to have handed over the Answer Sheet and dealt with
- as an unfair means case. The candidates are also required to put their left hand THUMB impression in the space provided in the Attendance Sheet.
- Use of Electronic/Manual Calculator and any Electronic Item like mobile phone, pager etc. is prohibited. 12.
- The candidates are governed by all Rules and Regulations of the Board with regard to their conduct in the 13. Examination Hall. All cases of unfair means will be dealt with as per Rules and Regulations of the Board.
- 14. No part of the Test Booklet and Answer Sheet shall be detached under any circumstances.
- 15.
 - Candidates are not allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, electronic device or any other material except the Admit Card inside the examination hall/room.

PART A

SOLUTIONS

PHYSICS

1.

2.

Sol.

4.

5. Sol.

Sol.

7.

Sol.

3

 $\tau = 0$

 $y_{(x,t)} = e^{-} (\sqrt{a} x + \sqrt{b} t)^{2} V = \sqrt{\frac{b}{a}}$ Wave moving in - ve x -direction.

2. 1 Sol. Diameter of wire =
$$\frac{1}{2} \times 52 = 0.52$$

I. Diameter of wire
$$=\frac{1}{100} \times 52 = 0.52 \text{mm} = 0.052 \text{cm}$$

 $T \times R = I\alpha = \frac{1}{2}MR^2\alpha$

 $T = \frac{1}{2}Ma$ $(a = \alpha R)$

From (1) and (2) $a = \frac{2g}{3}$

Diameter of wire
$$=\frac{1}{100} \times 52 = 0.52$$

Diameter of wire =
$$\frac{1}{100} \times 52 = 0.52$$
n

Diameter of wire =
$$\frac{100}{100} \times 52 = 0.52$$
r
2
Mg –T = Ma ...

Diameter of wire
$$=\frac{1}{100} \times 52 = 0.52$$

Diameter of wire =
$$\frac{1}{100} \times 52 = 0.52$$

Diameter of wire
$$=\frac{1}{100} \times 52 = 0.52$$
r

 $W = T \times \Delta A = T \times 8\pi (r_2^2 - r_1^2) = 0.4\pi \,\text{mJ}$

Angular momentum is conserve

l₂ first decreases and then increases ∴ o first increases and then decreases.

Position of the null point from mass m, $x = \frac{r}{1 + \sqrt{\frac{4m}{m}}} = \frac{r}{3}$

 $I_1\omega_1 = I_2\omega_2 \Rightarrow \omega_2 = \frac{I_1\omega_1}{I_2}$

 $V = -Gm \left(\frac{3}{r} + \frac{12}{2r} \right) = -9 \frac{Gm}{r}$











Sol.

Sol.

10.

Sol.

11.

Sol.

12.

13.

Sol.

Sol.

equilibrium condition = $K \frac{\sim}{x^2} = \omega \frac{\cdots}{2\ell}$ \Rightarrow Q² = Cx³

$$\Rightarrow Q^2 = Cx^3$$
$$\Rightarrow 2Q \frac{dQ}{dt} = C3x^2$$

 \Rightarrow 2Q $\frac{dQ}{dt}$ = C3x² $\frac{dx}{dt}$ $\Rightarrow \frac{dx}{dt} \propto \frac{x^{3/2}}{x^2} \propto x^{-1/2}$

 $E = B_H \ell V = 0.15 mV$

 $\Rightarrow 2\sqrt{v} = -2.5t + C$ at $t = 0, v = 6.25 \Rightarrow C = 5$

 $q = \frac{q_0}{\sqrt{2}} \Rightarrow \omega t = \frac{\pi}{4}$

 $\Rightarrow t = \frac{T}{8} = \frac{2\pi}{8} \sqrt{LC} = \frac{\pi}{4} \sqrt{LC}$

Normal to the plane is z -axis

 $\cos \theta_1 = \frac{A_z}{A} = \frac{10}{20} = \frac{1}{2}, \theta_1 = 60$

 $\overrightarrow{dB} = \frac{\mu_0 di}{2\pi R} \left[-\cos\theta \hat{i} - \sin\theta \hat{j} \right]$

 $d\vec{B} = \frac{\mu_0 I}{2\pi^2 R} \left(-\cos\theta \hat{i} - \sin\theta \hat{j} \right)$

 $di = \frac{T}{\pi R} R d\theta$

 $=\frac{1}{\pi}d\theta$

at $v = 0 \Rightarrow t = \frac{5}{2.5} = 2s$

Integrating the above equation.

 $\frac{dv}{dt} = -2.5\sqrt{v}$

any instant of separation between charges is x.
$Q^2 - Q^2$

Charge oscillates simple harmonic motion $q = q_0 \sin \omega t$, $U = \frac{1}{2} \frac{q^2}{C}$

 $\mu_1 \sin \theta_1 = \mu_2 \sin \theta_2 \Rightarrow \sqrt{2} \times \frac{\sqrt{3}}{2} = \sqrt{3} \sin \theta_2 \Rightarrow \theta_2 = 45^\circ$

Αt

AIEEE-2011-16

$$\vec{B} = -\frac{\mu_0 I}{\pi^2 R} \hat{j}$$

$$3$$

$$W = \Delta U$$

 $\frac{1}{2}$ mv² = nC_vdT

 $dT = \frac{M \big(\gamma - 1 \big) v^2}{2 R} K$

 $\Rightarrow \frac{1}{2}M\omega^2 A_1^2 = \frac{1}{2}(m+M)\omega^2 A_2^2$

Energy of simple harmonic oscillator is constant.

 $v_b^2 - (0.4)^2 = 2 \times 9.8 \times 0.2 \lceil v^2 - u^2 = 2gh \text{ is used} \rceil$

Data \Rightarrow n, k, $t_1 + n_2 kT_2 + n_3 kT_3 = (n_1 + n_2 + n_3)kT$

Since ionospheric properties change with time, these signals are in general less stable than ground wave

 $=\frac{m}{M}\frac{R}{v-1}dT$

 $\frac{A_1^2}{A_2^2} = \frac{M+m}{M}$

 $\therefore \frac{A_1}{A_2} = \sqrt{\frac{M+m}{M}}$

Equation of continuity

 $v_b = 2m/s \text{ (nearly)}$

 $d \approx 3.6 \times 10^{-3} \, \text{m}$

signals.

 $r \times F = I \times \alpha$

 $\frac{d\omega}{dt} = 4t - t^2$

 $d\omega = \left(4t^2 - t^2\right)dt$

 $\omega = 0 \Longrightarrow t = 6s$

 \Rightarrow (a×v)top = (a×v)bottom

 $\pi \left[8 \times 10^{-3} \right] \times 0.4 = \pi d^2 \times 4$

 $\frac{n_1T_1 + n_2T_2 + n_3T_3}{n_1 + n_2 + n_3}$

 $2(20t-5t^2)=10\alpha \Rightarrow \alpha=4t-t^2$

 $\omega = 2t^2 - \frac{t^3}{3}$ (on integration)

Sol.

- 15. Sol.

- 16.

- 17.
- 18. Sol.

Sol.

- Sol.

- Sol.

$$d\theta = \left(2t^2 - \frac{t^3}{3}\right)dt$$

$$\Rightarrow \theta = \frac{2t^3}{3} - \frac{t^4}{12} \text{ (on integration)}$$

 $\omega = \frac{d\theta}{dt} = 2t^2 - \frac{t^3}{3}$

$$\frac{3}{3} = \frac{12}{12}$$

$$\theta(\text{in 6s}) = 36 \text{ rad}$$

$$\Rightarrow 2\pi n = 36$$

 $\eta_2 = \frac{T_1 - (T_2 - 62)}{T_2} = \frac{1}{3}$

 $\Rightarrow \frac{T_1 - T_2}{T_1} + \frac{62}{T_2} = \frac{1}{3}$

 $\therefore T_1 = 62 \times 6 = 372K$

 $\frac{1}{6} + \frac{62}{T_c} = \frac{1}{3}$

 \Rightarrow T₂ = 310K

 $R \propto \ell^2$ (for a given volume)

 $\frac{62}{T} = \frac{1}{6}$

$$\Rightarrow 2\pi n = 36$$

$$n = \frac{36}{2\pi} = <6$$

20. 2 Sol.
$$V_c = E(1 - e^{-t/Rc})$$
 $1 - e^{-t/Rc} = \frac{120}{200} = \frac{3}{5}$

1-e^{-t/Rc} =
$$\frac{120}{200}$$
 = $\frac{3}{5}$
⇒ R = $\frac{5}{1.84 \times 10^{-6}}$ = 2.7 × 10⁶ Ω

21. 4

Sol.
$$\eta_1 = \frac{T_1 - T_2}{T_1} = \frac{1}{6}$$







Sol.

 $\Rightarrow \frac{\Delta R}{R}\% = \frac{2\Delta \ell}{\ell}\%$ Thus when wire is stretched by 0.1% resistance increases by 0.2% destructive interference.

 $-\frac{1}{v^2}\frac{dv}{dt} - \frac{1}{u^2}\frac{du}{dt} = 0$

 $\frac{dv}{dt} = -\frac{v^2}{u^2} \left(\frac{du}{dt} \right)$

 $\frac{1}{11} + \frac{1}{-280} = \frac{1}{20}$

 \Rightarrow v = $\frac{280}{15}$ cm

 $v_1 = -\left(\frac{280}{15 \times 280}\right)^2 \times 15$

 $E_{Li}^{++} = -13.6 \times \frac{9}{1} = -122.4 eV$

 $E_{Li}^{+++} = -13.6 \times \frac{9}{9} = -13.6eV$

3 Potential inside $(\phi) = ar^2 + b$

 $\phi_{\text{net}} = \left(-2ar\right)4\pi r^2 = -8\pi ar^3$

Max. range = $\frac{u^2}{a}$ i.e., $\frac{v^2}{a}$ (radius of circle)

Area occupied = $\pi \left(\frac{v^2}{q}\right)^2 = \frac{\pi v^4}{q^2}$

 $\Delta E = -13.6 - (-122.4)$ = 108.8 eV

 $\therefore E_r = -\frac{\delta V}{8r} = -2ar$

 $-8\pi a r^3 = \frac{\sigma \times \frac{4}{3}\pi r^3}{c}$

 $\therefore \sigma = -6a\varepsilon_0$

f = 20 cm

 $=\frac{1}{15}$ m/s

 $E_n = -13.6 \frac{Z^2}{R^2}$

As light enters from air to glass it suffers a phase change on π and therefore at centre there will be

Electric field inside uniformly charged solid volume varies with 'r'. So charge density is constant

23. Sol.

Sol.

- $\frac{1}{1} + \frac{1}{11} = \frac{1}{f}$

- 25.
- Sol.

- 26. Sol.

- 27.
- Sol.

$$\Delta Q = \Delta U + \Delta W$$
 (ignoring expansion)
 $\Delta U = ms\Delta T = 0.1 \times 4.184 \times 20 = 8.368 \text{kJ}$

 $t_{\frac{1}{2}} = 20$ minutes

 $\frac{2}{3}N_0 = N_0 e^{-\lambda t_2}$

 $t_2 = \frac{1}{\lambda} \ln \frac{3}{2}$

= 20 min

 $N = N_0 e^{-\lambda t_2} \quad \lambda t_1 = In3$

 $t_2 - t_1 = \frac{1}{\lambda} \left[\ln \frac{3}{2} - \ln 3 \right]$

 $=\frac{1}{\lambda} \ln \left[\frac{1}{2}\right] = \frac{0.693}{\lambda}$

 $\text{KE}_{\text{max}} = h\upsilon - h\upsilon_0$

 $h\upsilon - h\upsilon_0 = e \times \Delta v$

 $V_0 = \frac{hv}{e} - \frac{hv_0}{e}$

'υ' is doubled $KE_{max} = 2hv - hv_0$

 $V_0' = (\Delta V)' =$

KE max = hυ - hυ₀

KE_{max} may not be equal to 2

may not equal to 2

 $\frac{2}{3}N_{0}=N_{0}e^{-\lambda t_{2}}\;t_{1}=\frac{1}{\lambda}In3$

- 30.
- Sol.

2

PART B: MATHEMATICS

31.

Sol:

Sol:



$$C_2 = 0$$

$$C_2 = 0$$

$$C_1 = 0$$

$$C_1 = 0$$

$$C_2 = 0$$

$$C_1 = 0$$

$$C_2 = 0$$

$$C_1 = 0$$

$$C_2 = 0$$

$$C_3 = 0$$

$$C_4 = 0$$

$$C_4 = 0$$

$$C_5 = 0$$

$$C_7 = 0$$

$$C_7$$

P(-2, -2); Q = (1, -2)

32. **4 Sol:**
$$A = \sin^2 x + \cos^4 x = \frac{7 + \cos^4 x}{1 + \cos^4 x}$$

ol:
$$A = \sin^2 x + \cos^4 x = \frac{7 + \cos 4x}{8} \Rightarrow \frac{3}{4} \le A \le 3$$

ol:
$$A = \sin^2 x + \cos^4 x = \frac{r + r}{r}$$

$$\begin{array}{c}
\mathbf{2} \\
\left[1 - x - x^2 (1 - x)\right]^6 = (1 - x)^6 (1 - x^2)^6
\end{array}$$

$$= \begin{bmatrix} {}^{6}\text{C}_{0} - {}^{6}\text{C}_{1}\text{x} + {}^{6}\text{C}_{2}\text{x}^{2} - {}^{6}\text{C}_{3}\text{x}^{3} + {}^{6}\text{C}_{4}\text{x}^{4} - {}^{6}\text{C}_{5}\text{x}^{5} + {}^{6}\text{C}_{6}\text{x}^{6} \end{bmatrix} \times \begin{bmatrix} {}^{6}\text{C}_{0} - {}^{6}\text{C}_{1}\text{x}^{2} \\ \text{Coefficient of } \text{x}^{7} = {}^{6}\text{C}_{1}{}^{6}\text{C}_{3} - {}^{6}\text{C}_{3}{}^{6}\text{C}_{2} + {}^{6}\text{C}_{5}{}^{6}\text{C}_{1} = 120 - 300 + 36 = -144 \end{bmatrix}$$

34. **4**
Sol:
$$\lim \frac{\sqrt{2\sin^2(x-2)}}{\sqrt{2\sin^2(x-2)}}$$

$$\begin{array}{c|c}
x - 2 \\
\hline
x - 2 \\
\hline
x - 2
\end{array}$$

$$\begin{array}{c|c}
\sqrt{2} |\sin(x - 2)| \\
x - 2
\end{array}$$

$$\lim_{x \to 2} \frac{\sqrt{2|\beta| \ln(x-2)|}}{|x-2|}$$

$$RHI = \sqrt{2} \quad IHI = -\sqrt{2}$$

$$x \rightarrow 2$$
 $x - 2$
RHL = $\sqrt{2}$, LHL = $-\sqrt{2}$

R.H.L. =
$$\sqrt{2}$$
, L.H.L. = $-\sqrt{2}$
Limit does not exist.

35. **4 Sol:**
$${}^{(n-1)}C_{(r-1)} = {}^{(10-1)}C_{(4-1)} = {}^{9}C_{3}$$
Statement 1 is correct

$$-\cos 4x = 3$$

$$\frac{\cos 4x}{8} \Rightarrow \frac{3}{4} \le A \le 1$$

$$\begin{split} & 2 \\ & \left[1 - x - x^2 (1 - x)\right]^6 = \left(1 - x\right)^6 \left(1 - x^2\right)^6 \\ & = \left[{}^6C_0 - {}^6C_1x + {}^6C_2x^2 - {}^6C_3x^3 + {}^6C_4x^4 - {}^6C_5x^5 + {}^6C_6x^6\right] \times \left[{}^6C_0 - {}^6C_1x^2 + {}^6C_2x^4 - {}^6C_3x^6 +\right] \end{split}$$

$$x^{6}$$
 $\times \begin{bmatrix} {}^{6}C_{0} - {}^{6}C_{1}x^{2} + {}^{6}C_{2}x^{4} - {}^{6}C_{3}x^{6} + ... \\ 300 + 36 = -144 \end{bmatrix}$

Statement 2 is also correct From 9 we can select 3 in ${}^9\mathrm{C}_3$ ways. It is correct explanation.

- $\frac{d}{dy}\left(\frac{dx}{dy}\right) = \frac{d}{dy}\left|\frac{1}{\left(\frac{dy}{dy}\right)}\right| = -\frac{1}{\left(\frac{dy}{dy}\right)^2}\frac{d}{dy}\left(\frac{dy}{dx}\right)$

 $= - \left(\frac{dy}{dx}\right)^{\!\!-2} \frac{1}{\left(\frac{dy}{dx}\right)^{\!\!-}} \frac{d}{dx} \left(\frac{dy}{dx}\right) = - \left(\frac{d^2y}{dx^2}\right) \! \left(\frac{dy}{dx}\right)^{\!\!-3}$

 $\frac{dy}{dx} = y + 3 \Rightarrow \frac{dy}{y + 3} = dx$

ln(y+3) = x+c $x = 0 \Rightarrow y = 2$ \Rightarrow In5 = 0 + c c = ln5

ln(y+3) = x + ln5

 $v + 3 = 10 \Rightarrow v = 7$

x - y is an integer

x - y, y - z are integers

 $v + 3 = e^{x + \ln 5} \implies v + 3 = e^{\ln 2 + \ln 5}$

x - x = 0 is an integer \Rightarrow A is Reflexive

⇒ A is transitive. Hence statement – 1 is true.

Also $\frac{x}{a} = 1$ is a rational number $\Rightarrow B$ is reflexive

 $\frac{x}{y} = \alpha$ is rational $\Rightarrow \frac{y}{x}$ need not be rational

i.e., $\frac{0}{1}$ is rational $\Rightarrow \frac{1}{0}$ is not rational

⇒ B is not an equivalence relation.

Hence B is not symmetric

As sum of two integers is an integer. \Rightarrow (x-y)+(y-z)=x-z is an integer

x - y is an integer $\Rightarrow y - x$ is an integer $\Rightarrow A$ is symmetric

- 37.
- Sol:

38.

Sol:

 $I = 8 \int_{-1}^{1} \frac{\log(1+x)}{1+x^2} dx$

 $=8\log 2\frac{\pi}{4}-1$ $2l = 2\pi \log 2$ $I = \pi log 2$

Suppose roots are 1+pi, 1+qi

 $p \neq 0$ since roots are distinct

Product of roots = $\beta = 1 + p^2 \in (1, \infty)$

 \Rightarrow roots of 1+pi, 1-pi

P (at least one failure) ≥

1 - P (no failure) $\geq \frac{31}{32}$

 $1 - P(x = 5) \ge \frac{31}{32}$

 $1-{}^5C_5p^5 \ge \frac{31}{32}$

 $-p^{5} \geq -\frac{1}{32}$

 $p^5 \le \frac{1}{32}$

 $p \le \frac{1}{2}$

 $p \in \left[0, \frac{1}{2}\right]$

Sum of roots $1+pi+1+qi=-\alpha$ which is real

 $=8\int_{-1}^{\frac{\pi}{4}}\frac{\log(1+\tan\theta)}{1+\tan^2\theta}\sec^2\theta\,d\theta\,(\text{let }x=\tan\theta)$

 $=8\int_{\frac{\pi}{4}}^{\frac{\pi}{4}}\log\left(1+\tan\left(\frac{\pi}{4}-\theta\right)\right)d\theta =8\int_{\frac{\pi}{4}}^{\frac{\pi}{4}}\log\left(1+\frac{1-\tan\theta}{1+\tan\theta}\right)d\theta =8\int_{\frac{\pi}{4}}^{\frac{\pi}{4}}\log2d\theta -8\int_{\frac{\pi}{4}}^{\frac{\pi}{4}}\log\left(1+\tan\theta\right)d\theta$

39.

Sol:

- 40. Sol:

- 41.
- Sol:

2

n = 5

Success = p Failure = q

Sol:

42.

- Sum = 11040

1

200

2

200

 $\frac{1}{\sqrt{|x|-x}} \Rightarrow |x|-x > 0 \Rightarrow |x| > x \Rightarrow x \text{ is negative}$

 $\left(2\overline{a}-\overline{b}\right).\left\{\left(\overline{a}\times\overline{b}\right)\times\left(\overline{a}+2\overline{b}\right)\right\}=\left(2\overline{a}-\overline{b}\right).\left\{\left[\overline{a}.\left(\overline{a}+2\overline{b}\right)\right]\overline{b}-\left[\overline{b}.\left(\overline{a}+2\overline{b}\right)\overline{a}\right]\right\}$

 $\frac{n}{2}$ [240 + (n-1)40] = 10920

 $n\lceil 6+n-1\rceil = 546$ n(n+5) = 546

n = 21

 $x \in (-\infty, 0)$

 $\cos\theta = \sqrt{\frac{5}{14}}$

 $\sin\theta = \frac{3}{\sqrt{1/4}}$

 $\sin\theta = \frac{1+4+3\lambda}{\sqrt{1+4+\lambda^2}\sqrt{1+4+9}}$

 $\frac{3}{\sqrt{14}} = \frac{5+3\lambda}{\sqrt{5+\lambda^2}\sqrt{14}} \Rightarrow \lambda = \frac{2}{3}$

 $=-5\left(\overline{a}\right)^2\left(\overline{b}\right)^2+5\left(\overline{a}.\overline{b}\right)^2=-5$

Sol: $b^2 = a^2 (1 - e^2) = a^2 (1 - \frac{2}{5}) = a^2 \frac{3}{5} = \frac{3a^2}{5}$

 \therefore Required equation of ellipse $3x^2 + 5y^2 - 32 = 0$

 $\frac{x^2}{a^2} + \frac{y^2}{h^2} = 1 \Rightarrow \frac{9}{a^2} + \frac{5}{3a^2} = 1$

 $a^2 = \frac{32}{3}$

 $b^2 = \frac{32}{5}$

3

200

240

5

280

6

3

- 120 + 80 + 160 + 40 + 200 + 240 + ... = 11040
- $\frac{n}{2}$ [2a + (n-1)d] + 80 + 40 = 11040

- 43.
- Sol:

44.

Sol:

45.

Sol:

 $\frac{dV}{dt} = -k(T-t) \Rightarrow dV = -k(T-t)dt$

 $c_1c_2 = r_1 - r_2 \Rightarrow \frac{a}{2} = c - \frac{a}{2} \Rightarrow c = a$

 $\begin{vmatrix} 4 & k & 2 \\ k & 4 & 1 \\ 2 & 2 & 1 \end{vmatrix} = 0 \Rightarrow k^2 - 6k + 8 = 0 \Rightarrow k = 4, 2$

 $\sim \{(P \land \sim R) \leftrightarrow Q\} = \sim \{Q \leftrightarrow (P \land \sim R)\}$

 $C \cap D = C \Rightarrow P(C \cap D) = P(C) \Rightarrow P\left(\frac{C}{D}\right) = \frac{P(C \cap D)}{P(D)} \ge P(C)$

 $I = \frac{kT^2}{2} + c \Rightarrow c = I - \frac{kT^2}{2} \Rightarrow c = V(T) = I - \frac{kT^2}{2}$

Integrate

at $t = 0 \Rightarrow V = I$

- $V = \frac{-k(T-t)^2}{(-2)} + c \Rightarrow V = \frac{k(T-t)^2}{2} + c$

47.

Sol:

- 48. Sol:

- 49.

50.

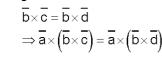
Sol:

52.

Sol:

- Sol:
 - $c_1 = \left(\frac{a}{2}, 0\right); c_2 = (0, 0)$ $r_1 = \frac{a}{2}$; $r_2 = c$

- $\therefore \overline{d} = \overline{c} \left(\frac{\overline{a} \cdot \overline{c}}{\overline{a} \cdot \overline{b}}\right) \overline{b}$
- $\Rightarrow (\overline{a}.\overline{c})\overline{b} (\overline{a}.\overline{b})\overline{c} = -(\overline{a}.\overline{b})\overline{d}$
- $\Rightarrow \left(\overline{a}.\overline{c}\right)\overline{b} \left(\overline{a}.\overline{b}\right)\overline{c} = \left(\overline{a}.\overline{d}\right)\overline{b} \left(\overline{a}.\overline{b}\right)\overline{d}$



- Sol:

 - Perpendicular distance from P to x y + 1 = 0 is $\frac{|y^2 y + 1|}{\sqrt{2}}$

 $v^2 - v + 1 > 0 \ \forall v \in R$ \therefore Coefficient $y^2 > 0$

 $\frac{1}{n}\sum |x_i - A|$

 $\therefore \text{ Min value} = \frac{1}{\sqrt{2}} \left(\frac{4ac - b^2}{4a} \right) = \frac{3}{4\sqrt{2}}$

A = Median = $\frac{25a + 26a}{2}$ = 25.5a

 $=\frac{2}{50}$ {312.5a} = 50 (Given)

 \Rightarrow 625a = 2500 \Rightarrow a = 4

Mean deviation = $\frac{1}{50} \{ |a - 25.5a| + |2a - 25.5a| \} = \frac{2}{50} \{ (24.5a + 23.5a) + ... (0.5a) \}$

Statement - 1: AB is perpendicular to given line and mid point of AB lies on line Statement – 2 is true but it is not correct explanation as it is bisector only. If it is perpendicular bisector then only statement – 2 is correct explanation.

Statement - 2 is also correct but it is not correct explanation of Statement - 1

 $(A(BA))^T = (BA)^T A^T = (A^TB^T)A = (AB)A = A(BA)$

 $((AB)A)^{T} = A^{T}(AB)^{T} = A(B^{T}A^{T}) = A(BA) = (AB)A$

B (1,6,3)

A (1,0,7)

1, 2, 3

(∵ AB is commutative)

54.

Sol:

55. Sol:

56.

Sol:

 $A^T = A, B^T = B$

Statement - 2

:. Statement - 1 is correct

 $(AB)^T = B^TA^T = BA = AB$

53.

$P = (y^2, y)$

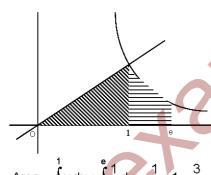
$$1 + \omega = -\omega^{2}$$

$$(1 + \omega)^{7} = (-\omega^{2})^{7} = -\omega^{14} = -\omega^{2} = 1 + \omega = A + B\omega \Longrightarrow (A, B) = (1, 1)$$

58.
$$2 = \lim_{x \to 0} \frac{\sin(p+1) + \sin x}{x} = q = \lim_{x \to 0} \frac{\sqrt{x + x^2} - \sqrt{x}}{x^{3/2}}$$

$$\lim_{x \to 0} (p+1)\cos(p+1)x + \cos x = q = \frac{1}{2}$$

$$\Rightarrow p+1+1 = \frac{1}{2} \Rightarrow p = -\frac{3}{2}; q = \frac{1}{2}$$



Area =
$$\int_{0}^{1} x dx + \int_{1}^{e} \frac{1}{x} dx = \frac{1}{2} + 1 = \frac{3}{2}$$

Sol:
$$f'(x) = \sqrt{x} \sin x$$

60.

Given
$$x \in \left(0, \frac{5\pi}{2}\right)$$

f'(x) changes sign from +ve to –ve at π f'(x) changes sign from -ve to +ve at 2π f has local max at π , local min at 2π

PART C: CHEMISTRY

61.

Greater charge and small size of cation cause more polarization and more covalent is that compound

62. (1) In RNA, the sugar is β – D – Ribose, where as in DNA the Sugar is β -D-2-deoxy Ribose Sol:

(4)

2CCI₃CHO OH⁽⁻⁾ CCI₃COONa + CCI₃CH₂OH

Cannizaro reaction is a disproportionation reaction One aldehyde molecule is oxidized to salt of the carboxylic Acid, other one is reduced to

- Alcohol. So the compound is CCl₃CH₂OH
 - IUPAC Name is 2, 2, 2, Trichloro ethanol

64. Sol:

 C_2H_5 O N a + CH₃ - C - CI \rightarrow CH₃ - C - O - C₂H₅ Ethyl ethanoate

65. $2H^+ + 2e^- \rightarrow H_2(g)$

Sol:

- $E = E^{\circ} 0.059 \log \left(\frac{P_{H_2}}{\left[H^{+} \right]^2} \right)$ (here E is –ve when $P_{H_2} > \left[H^{+} \right]^2$)
- $= \frac{-0.0591}{2} \log_{10} \left(\frac{2}{1}\right) = \frac{-.0591}{2} \times .3010 = \text{negative value}$
- 66. (2)Electron releasing groups (Alkyl groups) de stabilizes conjugate base. Sol:
- The +I effect of C3H7 is less than I effect of CI K_a of HCOOH is 17.9×10⁻⁵ K_a of CH_3CH_2 CH_3CH_3 COOH is 139×10^{-5}
- 67.

Sol:
$$i = 1 - \alpha + n\alpha = 1 + \alpha(n-1)$$

$$\frac{i-1}{n-1} = \alpha$$

$$A_x B_y \rightarrow x A^{+y} + y B^{-x}$$

n = x+ySo $\alpha = \frac{i-1}{x+v-1}$

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(3)

ease of liquefaction $\propto \frac{a}{b}$

 $CO_2(g) + C = \Box \Box \Box$

Therefore $p \propto n$; $\frac{0.5}{0.8} = \frac{p}{p+x} \Rightarrow x = 0.3$

 $K_p = \frac{P_{CO}^2}{P_{CO}} = \frac{0.6 \times 0.6}{0.2} = 1.8 \text{ atm}$

Therefore $[BF_{\epsilon}]^{3-}$ is not possible

 $\Delta T_f = K_f \times m = K_f \times \frac{w_2 \times 1000}{w_1 \times m_2}$

Temperature coefficient μ =2;

 $m_2 = mw \text{ of solute}$

Therefore $w_2 = 800g$

 $\mu^{\frac{\Delta T}{10}} = \frac{\mathbf{k}_2}{\mathbf{k}_4};$

 $2^{\frac{50}{10}} = 2^5 = 32 = \frac{k_2}{k_1}$

Therefore $32 k_1 = k_2$

 $w_1 \& w_2$ = wt of solvent & solute respecting

 $\Delta T_f = 0^\circ - (-6^\circ) = 6 = 1.86 \times \frac{w_2 \times 1000}{4000 \times 62}$

valency of four only.

Total pressure at equilibrium = 0.8 atm; Total no.of moles = p + x.

[Cr(NH₃)_s]Cl₃ involves d²sp³ hybridization and it is an inner orbital complex.

Across a period metallic strength decreases & down the group it increases

2CO(q)

68.

Sol:

for ethane a = 5.49, b = 0.0638

for Cl_2 a = 6.49, b = 0.0562 (4)

69. Sol: Initial moles Equilibriumm moles p-x

70. Sol:

71.

Sol:

72.

Sol:

73.

74.

Sol:

Sol:

As Boron has only four orbitals in the valence shell (i.e. 2s, 2px, 2py & 2pz) it can show a maximum

Sol: In
$$[NiCl_4]^{2^-}$$
, $n = 2$
 $\mu = \sqrt{n(n+2)}$ Bl

$$\mu = \sqrt{n(n+2)}$$
 BM
= $\sqrt{2(2+2)} = 2.8$

 $=\sqrt{2(2+2)}=2.82BM$

The general o.s of lanthanides is +3, only few elements exhibit +4 o.s.

 $=\frac{5.2}{5.2+\frac{1000}{400}}$

Stability of hydrides decreases down the group from NH_3 to BiH_3 as M-H bond energy decreases.

Formaldehyde and Acetaldehyde can be oxidized by tollen's reagent to give silver mirror.

= 0.09

Molefraction of solute (X_2) in aqueous solution =

'S' can exhibit a minimum oxidation state of -2

In IF₇, I undergoes sp³d³ hybridisation

on ozonolosys give formaldehyde

(2)

- - (1)

(2)

(4)

(3)

(3)

(Ex. H₂S)

Vinyl group

CH₂ CH-

 $\Rightarrow \frac{1}{355} = \frac{1}{680} + \frac{1}{\lambda_2}$

 \Rightarrow $\lambda_2 = 742.8 \cong 743 \text{ nm}$

- 76.
- Sol:
- 77. Sol:
- 78.
- Sol:
- 79.
- Sol: 80.
- 81.
- 82.
- 83.

- Sol:

- Sol:
- Sol:

84.

Sol:

- 85.

(3)

(3)

87.

Sol:

86. Sol:

88. Sol:

89.

90.

Sol:

Effective no. of A atoms = $\frac{1}{8} \times 8 = 1$

trinitrophenol

 $= 38.3 \text{ J mol}^{-1}.\text{k}^{-1}$

2, (2, 3)

ppt. with neutral FeCl₃

Phenol gives violet coloured comlex compound with neutral FeCl₃, benzoic acid gives pale dull yellow

In acidic medium, KBr + KBrO₃ in turn produces Br₂. Phenol reacts with Br₂ (aq) to give 2, 4, 6-

Effective no. of B atoms = $\frac{1}{2} \times 5$ (One is missing) = $\frac{5}{2}$ Therefore formula is $A_1B_{\underline{5}} = A_2B_5$

For an ideal gas, for isothermal reversible process, $\Delta S = 2.303 \text{ nR log} \left(\frac{V_2}{V_4} \right)$

both 2-pentanone, phenol can exhibit tautomerism

 $= 2.303 \times 2 \times 8.314 \times \log \left(\frac{100}{10} \right)$



(4)

Sol: