

SATHYABAMA UNIVERSITY

(Established under section 3 of UGC Act, 1956)

Course & Branch: B.E /B.Tech- Common to ALL Branches

Title of the paper: Engineering Mathematics – IV

Semester: IV

Sub.Code: 6C0054/401

Date: 22-04-2008

Max. Marks: 80

Time: 3 Hours

Session: FN

PART – A

(10 x 2 = 20)

Answer All the Questions

1. Find Fourier series given $f(x) = x$ in $-\pi \leq x \leq \pi$.
2. Define complex form of Fourier Series.
3. Form Partial differential equation by eliminating 'f' from $z = f(x^3 - y^3)$
4. Find the complete solution of $\sqrt{p} + \sqrt{q} = x + y$.
5. State any two assumptions in the derivation of one dimensional wave equation.
6. Define α^2 in $u_t = \alpha^2 u_{xx}$.
7. State the two dimensional heat equation in Cartesian as well as polar co-ordinates.
8. Write the three positive solutions of the Laplace equation in polar co-ordinates.
9. State Convolution Theorem of Fourier Transform.
10. If $F\{f(x)\} = \bar{f}(s)$ then Prove that $F\{f(ax)\} = \frac{1}{|a|} \bar{f}\left(\frac{s}{a}\right)$

PART – B

(5 x 12 = 60)

Answer All the Questions

11. Find the fourier Series expansion of $f(x)$ of period ' l '.

$$f(x) = \begin{cases} x & \left(0, \frac{l}{2}\right) \\ l-x & \left(\frac{l}{2}, l\right) \end{cases}$$

Hence deduce the sum of the series $\sum_{n=1}^{\infty} \frac{1}{(2n-1)^4}$

(or)

12. Find first three harmonics in the Fourier Series of $y = f(x)$

x	0	1	2	3	4	5	6
y	1.0	1.4	1.9	1.7	1.5	1.2	1.0

13. Solve $(y+z)p + (z+x)q = x+y$.

(or)

14. Solve $(D^2 - 2DD' + D'^2)z = x^2 y^2 e^{x+y}$ where $D = \frac{\partial}{\partial x}$, $D' = \frac{\partial}{\partial y}$.

15. Solve $y_{tt} = a^2 y_{xx}$ $0 \leq x \leq l$, $t > 0$ subject to $y(0, t) = 0$, $y(l, t) = 0$, $y_t(x, 0) = 0$

$$y(x, 0) = \begin{cases} kx & 0 \leq x \leq \frac{l}{2} \\ k(l-x) & \frac{l}{2} \leq x \leq l \end{cases}$$

(or)

16. A rod of length 20cm has its ends A and B kept at 30°C and 90°C respectively until steady state conditions prevail. If the temperature at each end is then suddenly reduced to 0°C and maintained so, find the temperature $u(x, t)$ at a distance ' x ' from A, at any time ' t '.

17. An uniformly ling metal plate in the form of an area is enclosed between the lines $y = 0$ and $y = \pi$ for positive values of x . The temperature is zero along the edges $y = 0$ and $y = \pi$ and the edge at infinity. If the edge $x = 0$ s kept at temperature 'ky', find the steady state temperature distribution in the plate.

(or)

18. A semi circular plate of radius a has its boundary dimeter kept at temperature zero and circumference at $f(\theta) = k$, $0 < \theta < \pi$. Find the steady state temperature at any distribution point of the plate.

19. Find Fourier Transform of the distribution

$$f(x) = \begin{cases} 1-|x| & |x| \leq 1 \\ 0 & |x| > 1 \end{cases}$$

Hence evaluate $\int_0^{\infty} \frac{\sin^4 t}{t^4} dt$

(or)

20. Find Fourier Sine and Cosine Transform of e^{-ax} $a > 0$, and hence

find Fourier Sine Transform of $\frac{x}{x^2 + a^2}$ and Fourier cosine

transform of $\frac{1}{x^2 + a^2}$

