DU MPhil Phd in Mathematics Topic:- DU_J18_MPHIL_MATHS_Topic01 1) The mathematician who was awarded Abel's prize for a proof of Fermat's Last Theorem is [Question ID = 19249] 1. Andrew Wiles. [Option ID = 46987] 2. Johan F. Nash. [Option ID = 46988] 3. S. R. Srinivasa Varadhan. [Option ID = 46989] 4. Lennart Carleson. [Option ID = 46990] Correct Answer :-• Andrew Wiles. [Option ID = 46987] 2) Founder of Indian Mathematical Society(IMS) was [Question ID = 19252] 1. Asutosh Mukheriee. [Option ID = 47000] 2. S. Narayana Aiyer. [Option ID = 47001] 3. M.T. Narayaniyengar. [Option ID = 47002] 4. V. Ramaswamy Aiyer. [Option ID = 46999] Correct Answer :-• V. Ramaswamy Aiyer. [Option ID = 46999] 3) Let R be a commutative ring with identity. If R is an Artinian domain, then the total number of prime ideals in R is [Question ID = 19280] 1. 1 [Option ID = 47111] 2. infinite. [Option ID = 47114] 3. 3 [Option ID = 47113] 4. 2 [Option ID = 47112] Correct Answer :-• 1 [Option ID = 47111] 4) Riemann hypothesis is associated with the function [Question ID = 19250] $\int_{2}^{1} f(x, y) = \int_{0}^{1} t^{x-1} (1-t)^{y-1} dt$ [Option ID = 46992] 3. Hermite polynomial [Option ID = 46994] $f(s) = \sum_{n=1}^{\infty} \frac{1}{n^s}, \ s \in \mathbb{C}$ Correct Answer : $f(s) = \sum_{n=1}^{\infty} \frac{1}{n^s}, \ s \in \mathbb{C}$ [Option ID = 46993] 5) For the stream function of a two dimensional motion, which of the following is not true [Question ID = 19297] 1. Stream function is constant along a stream line. [Option ID = 47181] 2. Stream function is harmonic. [Option ID = 47180] 3. Stream function exists for steady motion of compressible fluid. [Option ID = 47179] ₄ Stream function has dimension L^2T^{-2} . [Option ID = 47182] Correct Answer :-. Stream function has dimension L^2T^{-2} . [Option ID = 47182] 6) The famous Indian mathematician Srinivas Ramanujan passed away in the year [Question ID = 19248] 1. 1920 [Option ID = 46984] 2. 1922 [Option ID = 46985] 3. 1921 [Option ID = 46983] 4. 1919 [Option ID = 46986] Correct Answer :-• 1920 [Option ID = 46984] 7) Let F be a finite field with 9 elements. How many elements of F have order 8? [Question ID = 19287]

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1. 1 [Option ID = 47142]
2. 4 [Option ID = 47140]
3. 8 [Option ID = 47139]
4. 2 [Option ID = 47141]
Correct Answer :-
• 4 [Option ID = 47140]
<sup>8)</sup> For a viscous compressible fluid Consider the following statements:
     (I) Stress matrix is symmetric.
    (II) Kinematic coefficient of viscosity is dependent on the mass.
  (III) Rate of dilatation is \nabla . \bar{q}.
   Then
[Ouestion ID = 19293]
1. all of I, II and III are true. [Option ID = 47163]
2. only I and III are true. [Option ID = 47164]
3. only I and II are true. [Option ID = 47165]
4. only II and III are true. [Option ID = 47166]
Correct Answer :-
• only I and III are true. [Option ID = 47164]
<sup>9)</sup> Let f: R \to R' be a ring homomorphism. Assume that 1 and 1' are multiplicative
   identities of the rings R and R' respectively. Then f(1) = 1' if
      I f is onto.
     II f is one-one.
    III R is a domain.
    IV R' is a domain.
   The correct options are
[Question ID = 19276]
1. III and IV only. [Option ID = 47096]
2. II and III only [Option ID = 47098]
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3. I and IV only. [Option ID = 47097]
4. I and II only. [Option ID = 47095]
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Correct Answer :-

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• I and IV only. [Option ID = 47097]
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10)

For a solid stationary sphere of radius a placed in an incompressible fluid of uniform stream with velocity -Ui:

(I) velocity potential $\phi(r, \theta) = U \cos \theta (r + \frac{a^3}{2r^2}).$

(II) there exist two stagnation points $(a, 0), (a, \pi)$.

(III) stagnation pressure $p_{\infty} + \frac{1}{2}\rho U^2$, p_{∞} is a pressure at ∞ .

(IV) velocity at any point of surface of sphere is $(0, U \sin \theta, 0)$. Then

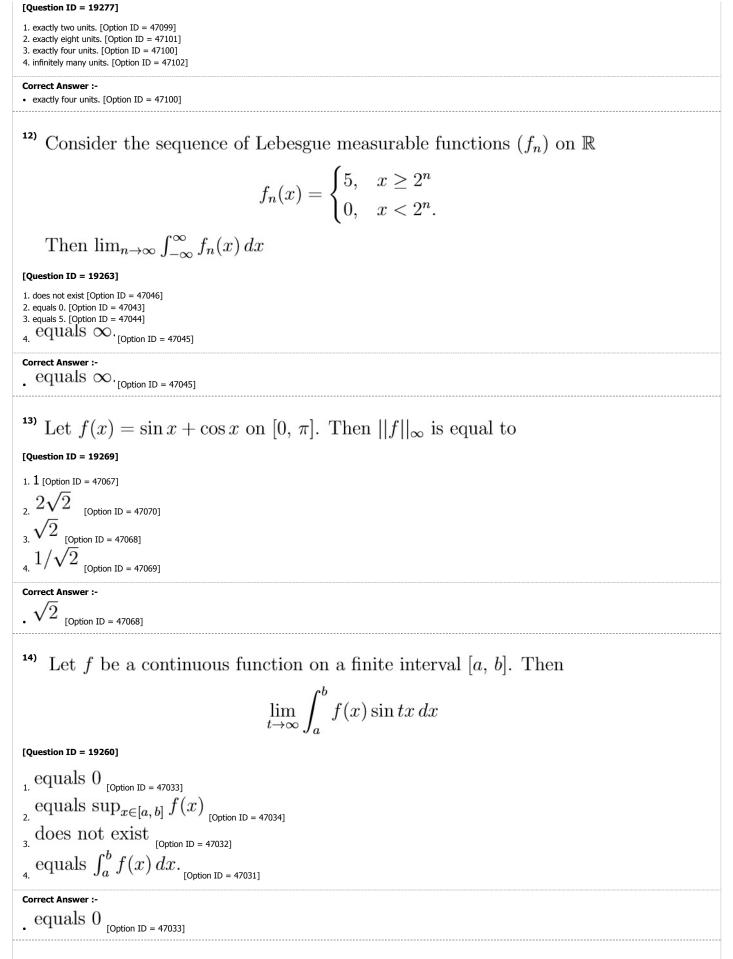
[Question ID = 19296]

- 1. only I, II, IV are true. [Option ID = 47175]
- 2. only I, III, IV are true. [Option ID = 47177]
- 3. only I, II, III are true. [Option ID = 47176] 4. only II, III, IV are true. [Option ID = 47178]

Correct Answer :-

• only I, II, III are true. [Option ID = 47176]

¹¹⁾ Let $R = \{a + ib : a, b \in \mathbb{Z}$. Then R is a Euclidean domain with



Let (X, d) be a metric space and $A \subseteq X$, $B \subseteq X$. Consider the following statements:

I If $x \notin A$ then d(x, A) > 0. II If $A \cap B = \phi$, then $d(A, B) \ge 0$. III If A is closed and $x \notin A$ then d(x, A) > 0. IV If A and B are closed and $A \cap B = \phi$ then $d(A, B) \ge 0$. Then, [Question ID = 19259]

all statements are correct. [Option ID = 47030]
 only III is correct. [Option ID = 47028]
 only II, III, IV are correct. [Option ID = 47027]
 only III and IV are correct. [Option ID = 47029]

Correct Answer :-

¹⁶⁾ The set $A = \{x \in \mathbb{Q} \mid -\sqrt{7} \le x \le \sqrt{7}\}$ in the subspace \mathbb{Q} of the real line \mathbb{R} is

[Question ID = 19271]

1. neither open nor closed [Option ID = 47078]

open but not closed [Option ID = 47075]
 both open and closed [Option ID = 47077]

4. closed but not open [Option ID = 47077]

Correct Answer :-

• both open and closed [Option ID = 47077]

A Lipschitz's constant associated with the function $f(x, y) = y^{2/3}$ on $R : |x| \le 1, |y| \le 1$

[Question ID = 19288]

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1. does not exist. [Option ID = 47146]
2. equals 1/2. [Option ID = 47145]
3. equals 0. [Option ID = 47143]
4. equals 1. [Option ID = 47144]
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Correct Answer :-does not exist. [Option ID = 47146]

18)

Let $I = \int_C y \, dx + (x+2y) \, dy$, where $C = C_1 + C_2$, C_1 being the line joining (0, 1) to (1, 1) and C_2 is the line joining (1, 1) to (1, 0). The value of I is

[Question ID = 19256]

1. 2 [Option ID = 47017] 2. -1 [Option ID = 47018] 3. 1 [Option ID = 47015] 4. 0 [Option ID = 47016]

Correct Answer : 1 [Option ID = 47015]

• I [Option ID =
$$4/01$$

¹⁹⁾ Let
$$F(x) = \int_0^x \frac{\sin t}{t^{3/2}} dt$$
, $0 < x < \infty$. The local maximum value is at the point

[Question ID = 19255]

. $x=\pi/2$ [Option ID = 47013] 2. $x=4\pi$ [Option ID = 47014]

3.
$$x=\pi$$
 [Option ID = 47011]
4. $x=2\pi$ [Option ID = 47012]

Correct Answer :-

. $x=\pi$ [Option ID = 47011]

20)

The general integral of the partial differential equation yzp + xzq = xy, where $p = \frac{\partial z}{\partial x}, q = \frac{\partial z}{\partial y}$ (G being an arbitrary function) is

[Question ID = 19289]

$$\begin{array}{l} z^2 = x^2 - G(x^2 + y^2). \\ {}_{\text{[Option ID = 47150]}} \\ z^2 = y^2 + G(x^2 + y^2). \\ {}_{\text{[Option ID = 47147]}} \\ z^2 = y^2 + G(x^2 - y^2). \\ {}_{\text{[Option ID = 47148]}} \\ z^2 = x - G(x^2 - y^2). \end{array}$$

Correct Answer :-

$$x^2 = y^2 + G(x^2 - y^2).$$
 [Option ID = 47149]

21)

Let
$$f(x) = \begin{cases} x^2 \sin \frac{1}{x}, & x \neq 0\\ 0, & x = 0 \end{cases}$$
. Then

[Question ID = 19257]

. For any $\delta > 0, f$ is not monotonic on $[0, \delta)$ [Option ID = 47020] , f has a local extremum at x = 0 [Option ID = 47021]

. For any $\delta>0,\,f$ is convex on $[0,\,\delta)$ $_{\rm [Option \, ID \, = \, 47022]}$

, f' is continuous at x = 0 [Option ID = 47019]

Correct Answer :-

. For any $\delta > 0, f$ is not monotonic on $[0, \delta)$ [Option ID = 47020]

22)

Let $F = \mathbb{Q}((\sqrt{2}, \sqrt{3}))$. Then F is minimal splitting field of the polynomial $(x^2 - x^2)$ $2(x^2-3)$ over \mathbb{Q} . The field F is not the minimal splitting field of which of the following polynomials over \mathbb{Q}

[Question ID = 19286]

 $_{1.} x^4 - 10x^2 + 1.$ [Option ID = 47135] $_{\rm 2.}\,x^{-4}-x^2+6.\,_{\rm [Option \ ID\ =\ 47137]}$ 3. $x^4 + x^2 + 1$. [Option ID = 47136] $_{4}x^{4} + x^{2} + 25..$ [Option ID = 47138]

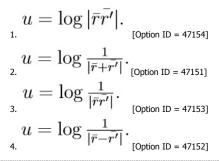
Correct Answer

An elementary solution of the partial differential equation

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$$

is of the form $(\bar{r} = xi + yj, \bar{r'} = x'i + y'j)$

[Question ID = 19290]



Correct Answer :-

$$= \log \frac{1}{|\bar{r} - \bar{r'}|}.$$
[Option ID = 47152]

24)

u

Let $E = \{x \in (0, \sqrt{2}] : x \text{ is a rational number}\} \cup \{y \in [2, 3] : y \text{ is an irrational number}\}$ Then the Lebesgue measure of E is

[Question ID = 19264]

1. 1 [Option ID = 47048] 2. $\sqrt{2}$ [Option ID = 47049] 3. 1/2 [Option ID = 47050] 4. $\sqrt{2} + 1$ [Option ID = 47047]

Correct Answer :-

• 1 [Option ID = 47048]

25)

Let H be a Sylow p-subgroup and K be a p-subgroup of a finite group G. Which of the following is incorrect is incorrect (H char G means H is characteristic in G)

[Question ID = 19282]

 $\begin{array}{l} {}_{1\cdot} K \lhd G \Rightarrow K \subset H \cdot {}_{[\operatorname{Option ID} = 47119]} \\ {}_{2\cdot} K \lhd G \Rightarrow K \mathrm{char} H \cdot {}_{[\operatorname{Option ID} = 47121]} \\ {}_{3\cdot} K \subset H \text{ if } K \lhd G \cdot {}_{[\operatorname{Option ID} = 47120]} \\ {}_{4\cdot} K \lhd G \not\Rightarrow H \cap K \lhd H \cdot {}_{[\operatorname{Option ID} = 47122]} \end{array}$

Correct Answer :-

 $K \triangleleft G \not\Rightarrow H \cap K \triangleleft H$. [Option ID = 47122]

A two dimensional motion with complex potential $w = U(z + \frac{a^2}{z}) + ik \log \frac{z}{a}$ has

- (I) stream lines as circle |z| = a.
- (II) circulation zero about circle |z| = a.
- (III) has two stagnation points in general.
- (IV) velocity at infinity equal to (-U).

Then

[Question ID = 19295]

1. only I, II, IV are true. [Option ID = 47172] 2. only I, III, IV are true. [Option ID = 47173] 3. only I, II, III are true. [Option ID = 47171] 4. only II, III, IV are true. [Option ID = 47174]

Correct Answer :-

• only I, III, IV are true. [Option ID = 47173]

27)

Let G be an abelian group of order 15. Define a map $\phi: G \to G$ by $\phi(g) = g^8$ for all $g \in G$. Consider the statements:

I ϕ is a homomorphism.

II ϕ is one-to-one.

III ϕ is onto.

Then

[Question ID = 19281]

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1. only I and III are true. [Option ID = 47117]
2. only I and II are true. [Option ID = 47116]
3. only I is true. [Option ID = 47115]
4. all statements are true. [Option ID = 47118]
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Correct Answer :-

• all statements are true. [Option ID = 47118]

28)

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Let \xi be a primitive n^{th} root of unity where n \equiv 2 \pmod{4}. Then [\mathbb{Q}(\xi) : \mathbb{Q}(\xi^2)] is
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(Here [V: F] denotes the dimension of the vector space V over F)

[Question ID = 19285]

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1. 1 [Option ID = 47131]

2. 2 [Option ID = 47132]

3. \phi(n) [Option ID = 47133]

4. \phi(n)/2 [Option ID = 47134]
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Correct Answer :-

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• 1 [Option ID = 47131]
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29)

The closed topologist's sine curve $\{(x,\,\sin\frac{1}{x})\,|\,x\in(0,\,1])$ as subspace of real line $\mathbb R$ is

[Question ID = 19272]

a path connected space [Option ID = 47081]
 connected but not locally connected [Option ID = 47079]

Correct Answer :-

• connected but not locally connected [Option ID = 47079]

30)

Let R(T) and N(T) denote the range space and null space of the linear transformation $T: P_2(\mathbb{R}) \to M_{2 \times 2}(\mathbb{R})$ which is given by

$$T(f) = \begin{pmatrix} f(1) - f(2) & 0 \\ 0 & f(0) \end{pmatrix}.$$

Then

[Question ID = 19275]

 $\lim_{\mathbf{1}_{\cdot}} \dim(R(T)) = 2 \text{ and } \dim(N(T)) = 1$ $\lim_{2} \dim(R(T)) = 0$ and $\dim(N(T)) = 2 \lim_{[\text{Option ID} = 47093]}$ $\lim_{3.3} \dim(R(T)) = 2 \text{ and } \dim(N(T)) = 0$ [Option ID = 47091] $\dim(R(T)) = 1$ and $\dim(N(T)) = 1$ [Option ID = 47092]

Correct Answer :-

 $\dim(R(T)) = 2$ and $\dim(N(T)) = 1$ [Option ID = 47094]

³¹⁾ The bilinear transformation on \mathbb{C} which maps z = 0, -i, -1 into w = i, 1, 0 is

[Question ID = 19265]

 $-irac{z+1}{z-1}$ [Option ID = 47053] z+12. *z*-1 [Option ID = 47052] 3. $i \frac{z+1}{z-1}$ [Option ID = 47051] $i^{\underline{z-1}}$ 4. vz+1 [Option ID = 47054] Correct Answer :-

 $-irac{z+1}{z-1}$ [Option ID = 47053]

³²⁾ Let $A, B \in M_n(\mathbb{C})$. Consider the following statements I If A, B and A + B are invertible, then $A^{-1} + B^{-1}$ is invertible. II If A, B and A + B are invertible, then $A^{-1} - B^{-1}$ is invertible. III If AB is nilpotent, then BA is nilpotent. IV Characteristic polynomials of AB and BA are equal if A is invertible. Then [Question ID = 19274] 1. only I, III, and IV are true [Option ID = 47089] 2. all the statements are true.. [Option ID = 47090] 3. only III is true [Option ID = 47088]

4. only I and II are true [Option ID = 47087]

Correct Answer :-

• only I, III, and IV are true [Option ID = 47089]

33)

For the boundary value problem: L(y) = y'' = 0, y(0) = 0, y'(1) = 0, the Green's function is

[Question ID = 19291]

[Question ID = 19291]
$G(x, \xi) = \begin{cases} \xi, & x \leq \xi \\ x, & x > \xi \end{cases}$ [Option ID = 47156]
$G(x, \xi) = \begin{cases} -x, & x \le \xi \\ -\xi, & x > \xi \end{cases}$ [Option ID = 47157]
$G(x, \xi) = \begin{cases} -x, & x \le \xi \\ -\xi, & x > \xi \end{cases}$ 3. [Option ID = 47158]
$G(x, \xi) = \begin{cases} x, & x \leq \xi \\ \xi, & x > \xi \end{cases}$ (Option ID = 47155]
Correct Answer :- $G(x, \xi) = \begin{cases} x, & x \leq \xi \\ \xi, & x > \xi \end{cases}$ [Option ID = 47155]
³⁴⁾ Let $E = \{x \in [0, \pi) : \sin 4x < 0\}$. Then Lebesgue measure of E is
[Question ID = 19262]
$\frac{\pi/2}{\pi/4}$ [Option ID = 47040]
2. $\frac{\pi/4}{3\pi/4}$ [Option ID = 47039]
3. $\frac{3\pi/4}{\pi/3}$ [Option ID = 47041]
4. $\pi/3$ [Option ID = 47042]
Correct Answer :- $\pi/2$ [Option ID = 47040]
35)
Let x_1, x_2, \dots, x_n be non-zero real numbers. With $x_{ij} = x_i x_j$, let X be the $n \times n$
matrix (x_{ij}) . Then

[Question ID = 19273]

the matrix X is positive definite if (x_1, x_2, \dots, x_n) is a non-zero vector [Option ID = 47084] the matrix X is positive semi definite for all (x_1, x_2, \dots, x_n) [Option ID = 47085] for all (x_1, x_2, \dots, x_n) , zero is an eigenvalue of X. [Option ID = 47086] it is possible to chose x_1, x_2, \dots, x_n so as to make the matrix X non singular [Option ID = 47083] Let $A = \{f : \mathbb{R} \to \mathbb{R} \mid f \text{ is continuous on } \mathbb{Q} \text{ and discontinuous } \mathbb{Q}'\}$, where \mathbb{Q} is the set of all rational numbers and \mathbb{Q}' is the set of all irrational numbers. Let μ be a counting measure on A. Then

[Question ID = 19258]

$$\begin{split} \mu(A) &= \sum_{q \in \mathbb{Q}} \frac{1}{2^{q}} \\ _{\text{[Option ID = 47026]}} \\ _{\text{2}} \mu(A) \text{ is infinite } \\ _{\text{[Option ID = 47023]}} \\ _{\text{3}} \mu(A) &= 0 \\ _{\text{[Option ID = 47024]}} \\ _{\text{4}} \mu(A) &= 2 \\ _{\text{[Option ID = 47025]}} \end{split}$$

³⁷⁾ Let $R = \mathbb{Z}_2 \oplus \mathbb{Z}_3 \oplus \mathbb{Z}_5$. Then the total number of zero divisors in R is

[Question ID = 19278]

1. 15 [Option ID = 47106] 2. 10 [Option ID = 47105] 3. 20 [Option ID = 47104] 4. 22 [Option ID = 47103]

Correct Answer :-

38)

Let $a, b \in \mathbb{C}$ such that 0 < |a| < |b|. Then the Laurent expression of $\frac{1}{(z-a)(z-b)}$ in the annulus |a| < |z| < |b| is

[Option ID = 47055]

[Question ID = 19266]

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$$\frac{1}{a-b} \left[\sum_{n=0}^{\infty} \frac{z^n}{b^n} + \sum_{n=0}^{\infty} \frac{a^n}{z^{n+1}} \right]_{\text{[Option ID = 47057]}}$$

$$\frac{1}{a-b} \left[\sum_{n=0}^{\infty} \frac{z^n}{b^{n+1}} + \sum_{n=0}^{\infty} \frac{a^n}{z^{n+1}} \right]_{\text{[Option ID = 47055]}}$$

$$\frac{1}{a-b} \left[\sum_{n=0}^{\infty} \frac{z^n}{a^{n+1}} + \sum_{n=0}^{\infty} \frac{b^n}{z^{n+1}} \right]_{\text{[Option ID = 47056]}}$$

$$\frac{1}{a-b} \left[\sum_{n=0}^{\infty} \frac{z^n}{a^n} + \sum_{n=0}^{\infty} \frac{b^{n+1}}{z^n} \right]_{\text{[Option ID = 47058]}}$$
Correct Answer :-

$$\frac{1}{a-b} \left[\sum_{n=0}^{\infty} \frac{z^n}{b^{n+1}} + \sum_{n=0}^{\infty} \frac{a^n}{z^{n+1}} \right]$$

³⁹⁾ Consider the following statements:

I
$$x^3 - 9$$
 is not irreducible over \mathbb{Z}_7 .

If
$$x^3 - 9$$
 is not irreducible over \mathbb{Z}_{11}

[Question ID = 19279]

1. II is false but I is true. [Option ID = 47107]

- 2. both I and II are true. [Option ID = 47109]
- 3. both I and II are false. [Option ID = 47110]

40)

The contour integral $\int_C \frac{e^z}{(z^2+\pi^2)^2} dz$, where C is the circle |z| = 4 taken anticlockwise equals

[Question ID = 19267]

1. $\frac{2\pi}{2\pi}$ [Option ID = 47061] 2. πi [Option ID = 47059] 4 3. π . [Option ID = 47060] 4. π [Option ID = 47062]

Correct Answer :-

 π [Option ID = 47062]

41)

The pressure p(x, y, z) in steady flow of inviscid incompressible fluid of density ρ with velocity $\bar{q} = (kx, -ky, 0), k$ is a constant, under no external force when $p(0,0,0) = p_0$, is

[Question ID = 19341]

, $p_0 - \rho k^2 (y^2 - x^2)/2$. [Option ID = 47358] $p_0 - \rho k^2 (y^2 + x^2).$ [Option ID = 47354] . $p_0 - \rho k^2 (y^2 - x^2)$. [Option ID = 47352] $_{\rm 4} p_0 - \rho k^2 (y^2 + x^2)/2.$ [Option ID = 47356]

Correct Answer :-

 $p_0 - \rho k^2 (y^2 + x^2)/2.$ [Option ID = 47356]

⁴²⁾ let E be a Lebesgue non-measurable subset of \mathbb{R} . Define $f: \mathbb{R} \to \mathbb{R}$ by

$$f(x) = \begin{cases} 2, & x \in E \\ -2, & x \in E^c. \end{cases}$$

Then

[Question ID = 19261]

neither f nor |f| is Lebesgue measurable [Option ID = 47038] $_{2}$ f is Lebesgue measurable but |f| is not Lebesgue measurable [Option ID = 47036] $_{3.}$ f is not Lebesgue measurable but |f| is Lebesgue measurable [Option ID = 47037] 4. f and |f| both are Lebesgue measurable. [Option ID = 47035]

Every non trivial solution of the equation $y'' + (\sinh x)y = 0$ has [Question ID = 19292] only finitely many zeros in $(0, \infty)$. [Option ID = 47162] infinitely many zeros in $(-\infty, 0)$. [Option ID = 47160] infinitely many zeros in $(0, \infty)$. [Option ID = 47159] at most one zero in $(0, \infty)$. [Option ID = 47161] Correct Answer :infinitely many zeros in $(0, \infty)$. 44) Which of the following statements is true [Question ID = 19253] If $0 \le a_n \le b_n$ and $\sum b_n$ diverges then $\sum a_n$ diverges $a_n = 47005$ If $\lim_{n\to\infty} a_n = 0$, then $\sum \frac{a_n}{a_n^2 + n^2}$ converges [Option ID = 47004] $\sum_{k=1}^{\infty} \left(\tan^{-1} \frac{1}{k} - \tan^{-1} \frac{1}{k+1} \right) = \frac{\pi}{8} \left[\text{Option ID} = 47003 \right]$ $\sum_{\rm A.}^{\infty} \sum_{n=1}^{\infty} \frac{1}{n^n} \geq 2 \ {\rm [Option \ ID = 47006]}$ Correct Answer :-If $\lim_{n\to\infty} a_n = 0$, then $\sum \frac{a_n}{a_n^2 + n^2}$ converges [Option ID = 47004] 45) Which of the following statements is not true [Question ID = 19254] 1. The set of all algebraic numbers is countable. [Option ID = 47010] 2. The set of rational numbers is equivalent to the set of natural numbers [Option ID = 47008] Given a set A, there exists a function $f: A \to P(A)$ that is onto (P(A) denotes power set of A)[Option ID = 47009] There is one-one function taking (-1, 1) onto \mathbb{R} . Correct Answer :-Given a set A, there exists a function $f: A \to P(A)$ that is onto (P(A) denotes power set of A)[Option ID = 47009] 46) Which of the following statements is not true [Ouestion ID = 19270] 1. An uncountable discrete space is not separable. [Option ID = 47072] 2. Every closed subspace of a separable space is separable. [Option ID = 47073] 3. Every compact metric space is Lindelof. [Option ID = 47074] 4. Every second countable space is separable. [Option ID = 47071] Correct Answer :-• Every closed subspace of a separable space is separable. [Option ID = 47073] 47) Which of the following is not correct (Here [V : F] denotes the dimension of the vector space V over F) [Question ID = 19284] , $[\mathbb{Q}(\sqrt{2}, \sqrt{3}, i, \sqrt{6}) : \mathbb{Q}] = 16.$ [Option ID = 47130] $\mathbb{Q}[\mathbb{Q}(\sqrt{2}, \sqrt{3}, i) : \mathbb{Q}] = 8.$ [Option ID = 47129] $\mathbb{Q}\left[\mathbb{Q}(\sqrt{3}):\mathbb{Q}\right]=2.$ [Option ID = 47127]

$_{_{4.}}\left[\mathbb{Q}(\sqrt{3},i):\mathbb{Q} ight]=4.$ [Option ID = 47128]
Correct Answer :- $[\mathbb{Q}(\sqrt{2},\sqrt{3},i,\sqrt{6}):\mathbb{Q}]=16.$ [Option ID = 47130]
48) Which of the following Banach spaces is not a Hilbert space [Question ID = 19268]
$(L^2([0, 1]), . _2)$ [Option ID = 47064]
2. \mathbb{R}^n with the norm $ x = \sqrt{\xi_1^2 + \xi_2^2 + \dots + \xi_n^2}$, where $x = (\xi_1, \xi_2, \dots, \xi_n)$ [Option ID = 47065]
$\mathbb{R}^{n} \text{ with the norm } x = \max\{ \xi_{1} , \xi_{2} , \cdots, \xi_{n} \}, \text{ where } x = (\xi_{1}, \xi_{2}, \cdots, \xi_{n}) _{\text{[Option ID = 47066]}}$
$_{4.}(l^2, . _2)_{[Option ID = 47063]}$
Correct Answer:- \mathbb{R}^n with the norm $ x = \max\{ \xi_1 , \xi_2 , \cdots, \xi_n \}$, where $x = (\xi_1, \xi_2, \cdots, \xi_n)$ [Option ID 47066]
49) Which of the following websites is of Mathematical Reviews [Question ID = 19251]
1. https://mathscinet.ams.org [Option ID = 46997]
2. https://mathscinet.ac.in [Option ID = 46995] 3. https://math.ac.au [Option ID = 46996] 4. https://www.mathjournal.org. [Option ID = 46998]
Correct Answer :- • https://mathscinet.ams.org [Option ID = 46997]
50) Let G be a cyclic group of order 42. The number of distinct composition series of G is [Question ID = 19283]
1. 8 [Option ID = 47126]
2. 16 [Option ID = 47123] 3. 10 [Option ID = 47125]
4. 6 [Option ID = 47124]
Correct Answer :-
• 6 [Option ID = 47124]