

Sample Paper
Class – X
Subject – Mathematics

Section – A

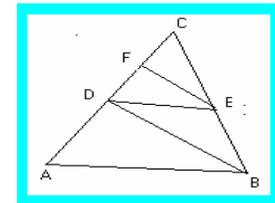
(Answer all the questions from this Section)

1.a) A certain sum gives Rs 1000 as SI and 1050 as CI for 2 years time . If the rate is same , find the sum (3)

b) What are the solutions to $|x| \geq 2$? .
Graph on a number line. (3)

c) $n = \frac{\sqrt{x^2+xy} + \sqrt{x^2-xy}}{\sqrt{x^2+xy} - \sqrt{x^2-xy}}$, show that $n^2 y - 2nx + y = 0$ (4)

2 a) $DE \parallel AB$ and
 $FE \parallel DB$ Prove that $DC^2 = CF.AC$ (3)



b). Four horses are tethered at 4 corners of a square field of side 70 metres so that they just cannot reach one another. What is the area left ungrazed by the horses 4

c) Mr. Khan invests Rs. 45000 in a cement company paying a dividend of 9% per annum, when Rs. 100 share sells at Rs. 150. What is his annual Income? He sells 50% of his shares when the price rises to Rs. 200. What is his gain ?

3 a) A hemispherical bowl of internal diameter 36 cm is full of some liquid. This liquid is to be filled in cylindrical bottles of radius 3 cm and height 6 cm. Find the number of bottles needed to empty the bowl 3

b) Bibhu Prasad buys goods worth Rs. 5000. He gets a rebate of 5% on it. A sales tax at the rate of 5% is levied on the discounted price. Find the amount he will have to pay for the goods.: (3)

c) A sum of Rs.4,920 was borrowed at 5% p.a. compound interest. The loan was paid back in 2 equal instalments in two years. Find the value of each instalment. (4)

4 a) If the point C (-1, 2) divides the line segment AB in the ratio 3 : 4, where coordinates of A are (2, 5), find the coordinates of B. \ (3)

b) Given that $2x^3 - x^2 - 2x + 3 = (Ax + B)(x - 1)(x + 2) + C(x - 1) + D$, find the values of A, B, C and D. Hence or otherwise, deduce the remainder when $2x^3 - x^2 - 2x + 3$ is divided by $x^2 + x - 2$ (4)

c) Plot P(3,2) and Q(-3,-2). Draw perpendicular PM and QN on X axis
1. Find image of P at the origin.
2. Name PMQN find its area
3. When M is mapped on reflection to X-axis, Y-axis and , origin ,find coordinates Use graph paper for this question. Take 1 cm = 1 unit on both the axes. (3)

Section – B

(Answer any FOUR questions from this Section)

5 a) The numerator of a fraction is one less than its denominator. If three is added to each of the numerator and denominator, the fraction is increased by $\frac{3}{28}$. Find the fraction? (3)

b) The mean of the following frequency distribution is 62.8. Find the missing x. (3)

11 a) Priya Goswami has a savings bank account in a bank. Her pass book has the following entries:

| Year | Date | Particulars | Debit | Credit | Balance |
|------|----------|-------------|---------|---------|----------|
| 2000 | Feb 10 | By cash | -- | 1000-00 | 1000-00 |
| | Feb 26 | By cheque | -- | 2000-0 | 3000-00 |
| | March | By salary | -- | 5000-00 | 8000-00 |
| | March 10 | By cheque | 2000-00 | - | 6000-00 |
| | March 29 | By cash | 500-0 | - | 5500-00 |
| | April 3 | By salary | -- | 5000-00 | 10500-00 |

If she closes her account on 15th April and the rate of interest is 5% per annum, find the amount received by her. (5)

b) $\frac{8a-5b}{8c-5d} = \frac{8a+5b}{8c+5d}$ prove that $a/b=c/d$

| | |
|---------|----|
| 0-20 | 5 |
| 20-40 | 8 |
| 40-60 | x |
| 60-80 | 12 |
| 80-100 | 7 |
| 100-120 | 8 |

c) A pole 5 m high is fixed on the top of a tower. The angle of elevation of the top of the pole observed from a point A on the ground is 60° and the angle of depression of point A from the top of the tower is 45° . Find the height of the tower. (Take $\sqrt{3}=1.732$) (4)

6 a) Solve $(x-5)^2 + 2(x-5) - 35 = 0$

b) Give an example of reflection on the line $y=x$
 Give an example of reflection on the X axis
 Give an example of reflection on the Y axis (3)

c) Water flows out through a circular pipe whose internal radius is 1 cm, at the rate of 80 cm/second into an empty cylindrical tank, the radius of whose base is 40 cm. By how much will the level of water rise in the tank in half an hour? (4)

7 a) Draw a histogram with the following data of salaries [in thousands] of employees of a Foreign Bank branch in Mumbai

| Salary in thousands | no of employees |
|---------------------|-----------------|
| 0-10 | 50 |
| 11-21 | 300 |
| 22-32 | 250 |
| 33-43 | 400 |
| 44-54 | 550 |
| 55-65 | 440 |
| 66-76 | 260 |

| | |
|----------|-----|
| 77-87 | 350 |
| 88 above | 100 |

b) Using the ruler and compasses only: Using a ruler construct a triangle with $BC=6.4$ cm $CA=5.8$ and $\angle ABC=60^\circ$. Draw its incircle. Record the radius

(5)

8 a) If the equation $(1 + m^2)x^2 + 2mcx + c^2 - a^2 = 0$ has equal roots, prove that $c^2 = a^2(1 + m^2)$.

(5)

8 b) find the value of x, y if

$$\begin{bmatrix} 1 & 2 \\ 3 & 3 \end{bmatrix} \begin{bmatrix} x & 0 \\ 0 & y \end{bmatrix} = \begin{bmatrix} x & 0 \\ 0 & 1 \end{bmatrix}$$

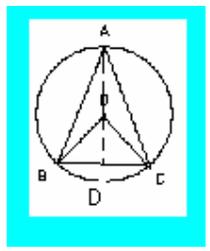
c) Prove that

$$\frac{\sin A}{1 + \cos A} + \frac{1 + \cos A}{\sin A} = 2 \operatorname{cosec} A$$

(3)

9a) BC is a chord of a circle with centre O . A is a point on arc BAC as shown. Prove that $\angle BAC + \angle OBC = 90^\circ$.

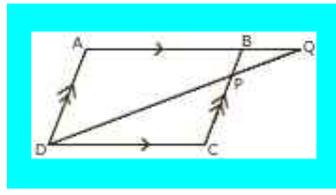
(3)



9 b) In the below figure, alongside $ABCD$ is a parallelogram, P is a point on BC such that $BP : PC = 1 : 2$. DP produced meets AB produced

at Q . Given area of triangle $BPQ = 20 \text{ cm}^2$, calculate:

- (i) Area of triangle CDP ;
- (ii) Area of parallelogram $ABCD$ (4)



c) What will Rs.1500 amount to in three years if it is invested in 20% p.a. compound interest, interest being compounded annually? (3)

10a) Answer yes / no

1. Are any two equilateral triangles similar?
2. If two isosceles triangles have congruent vertex angles, are the triangles similar?
3. If two isosceles triangles have congruent base angles, are the triangles similar?
4. Is it possible for two quadrilaterals to have congruent angles and not be similar?
5. Are all squares similar to one another?
6. Are all circles similar? (3)

b) Mrs. Kaul invests Rs. 56000 in a textile company paying 5% per annum when its Rs. 100 share can be bought for Rs. 140. Find her annual dividend and her percentage income on investment.

10(c) A rocket at Sriharikota launching pad having the shape of a cylinder surmounted by a cone. has the following measurements. The cylinder is of radius 3 m and height 20 m and the cone has the slant height 5 m. Calculate the surface area and volume of the rocket. (4)