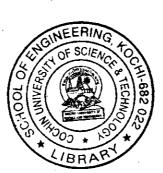
# MODULE-V

- IX a) Define level of significance, Type I error, Type II error.
  - b) The mean of a sample of size 20 from a normal population  $N(\mu, 8)$  was found to be 81.2. Find a 90% confidence interval for  $\mu$ .
  - c) Three specimens of high quality concrete had compressive strength 357, 359, 413 (in kg/cm²) and for three specimens of ordinary concrete and the values were 346, 358, 302.

    Test for quality of the population means  $\mu_1 = \mu_2$  against the alternative  $\mu_1 > \mu_2$ . (8)

#### OR

- X a) Define null hypothesis and alternative hypothesis. A random sample of size 18 is taken from a normal distribution  $N(\mu, \sigma^2)$ . Test the hypothesis  $H_o: \sigma^2 = 0.36$  against  $H_1: \sigma^2 > 0.36$  at  $\alpha = 0.05$  given the sample variance  $s^2 = 0.68$ . (12)
  - b) Two independent random samples of size  $n_1 = 10$ ,  $n_2 = 7$  where observed to have sample variance  $s_1^2 = 16$ ,  $s_2^2 = 3$  Using  $\alpha = 0.10$ , test  $H_o: \sigma_1^2 = \sigma_2^2$  against  $H_i: \sigma_1^2 \neq \sigma_2^2$ .



BTS-C023 ME

# B. Tech. Degree III Semester Examination January 2002

M

## IT/CS/EC/CE/ME/SE/EI/EB/EE 301 ENGINEERINGMATHEMATICS-III

Time: 3 Hours

b)

(6)

Max. Marks: 100

### **MODULE-I**

a) Obtain the Fourier series of

$$f(x) = \begin{cases} -x & -\pi < x \le 0 \\ x & 0 \le x \le \pi, \ f(x+2\pi) = f(x) \end{cases}$$

Deduce 
$$\sum_{n=1}^{\infty} \frac{1}{(2n-1)^2} = \frac{\pi^2}{8}$$
 (10)

b) Find the Fourier transform of

$$f(x) = \begin{cases} 1 & \text{for } |x| < 1 \\ 0 & \text{for } |x| > 1 \end{cases}$$

Hence evaluate 
$$\int_{0}^{\infty} \frac{\sin x}{x} dx$$
 (10)

a) Represent the following function in the Fourier integral form

$$f(x) = \begin{cases} x^2 & 0 < x < \mathbf{i} \\ o & x > 1 \end{cases} \tag{10}$$

Define gamma function and prove that

$$\Gamma(n) \Gamma\left(n + \frac{1}{2}\right) = \frac{\sqrt{\pi}}{2^{2n-1}} \Gamma(2n)$$
 (10)

(P.T.O)

VI

VII

b)

### MODULE-II

III a) Prove that 
$$\int_{0}^{1} x J_{n}(\alpha x) J_{n}(\beta x) dx = \begin{cases} o & \alpha \neq \beta \\ \frac{1}{2} \left[ J_{n+1}^{(\alpha)} \right]^{2}, \alpha = \beta \end{cases}$$

where 
$$\alpha, \beta$$
 are roots of  $J_n(x) = 0$  (12)

b) Express 
$$J_5(x)$$
 in terms of  $J_o(x)$  and  $J_1(x)$  (8)

OR

N a) Prove that 
$$nP_n(x) = xP_n^1(x) - P_{n-1}^1(x)$$
 (10)

b) Show that 
$$(1-2xt+t^2)^{-\frac{1}{2}} = \sum_{n=0}^{\infty} t^n P_n(x)$$
 (10)

#### MODULE-III

V a) (i) Solve 
$$(z-y)p+(x-z)q=y-x$$

(ii) Solve 
$$\sqrt{p} + \sqrt{q} = x + y$$
 (10)

b) A tightly stretched string with fixed end points x = 0 and  $x = \ell$  is initially in a position given by  $y(x,0) = y_o \sin^3\left(\frac{\pi x}{\ell}\right).$  If it is released from rest from this position, find the displacement y at any time and at any distance from the end x = 0. (10)

#### **UK**

Using the method of separation of variables solve the Laplace's equation  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0.$  (8)

An infinitely long plane uniform plate is bounded by two parallel edges x = 0 and  $x = \ell$ , and an end at right angles to them. The breadth of this edge y = 0 is  $\ell$  and is maintained at a temperature f(x). All the other three edges are at temperature zero. Find the steady state temperature at any interior point of the plate. (12)

#### MODULE-IV

a) The following is the probability density function of a random variable X.

$$x = 0$$
 1 3 7 13  
 $P(X=x) = \frac{1}{8}$   $\alpha = \frac{1}{6}$   $\frac{1}{4}$   $\beta$ 

Find  $\alpha$  and  $\beta$  if  $P(X^2 = 4X - 3) = \frac{1}{2}$  (7)

- b) Obtain the mean and variance of the binomial distribution. (7)
- c) Suppose that X has a Poisson distribution.

If 
$$P(X = 2) = \frac{2}{3}P(X = 1)$$
. Find  $P(X = 3)$  (6)

#### OR

II a) In a test on 2000 electric bulbs, it was found that the life of a particular make was normally distributed with an average life of 2040 hrs. and S.D. 60 hrs. Estimate the no. of bulbs likely to burn for

- (i) More than 2150 hrs. (ii) More than 1920 hrs. but less than 2160 hrs. (10)
- b) Find the equation of the regression line of y on x and x on y given the following data.

Contd....4