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# GUJARAT TECHNOLOGICAL UNIVERSITY <br> MBA. Sem-II Remedial Examination December 2010 <br> Subject code: 820007 <br> Subject Name: Research Methodology and operations Research <br> Time: $10.30 \mathrm{am} \mathbf{- 0 1 . 0 0} \mathbf{~ p m}$ 

Date: $\mathbf{2 4 / 1 2 / 2 0 1 0}$

## Total Marks: 70

## Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) Find the graphical solution of the following problem.

Find x and y so as to Minimize $\mathrm{Z}=\mathrm{X}+\mathrm{Y}$ subject to the following constraints; $5 \mathrm{X}+10 \mathrm{Y} \leq 50, \mathrm{X}+\mathrm{Y} \geq 1, \mathrm{Y} \leq 4, \mathrm{X}, \mathrm{Y} \geq 0$. Observe the solution and comment on it. Write the dual of this problem.
(b) State and explain the following important features of 'Explanatory Data Analysis'
(1) Frequency table and Histogram
(2) Stem and Leaf displays
(3) Boxplots
Q. 2 (a) Explain salient features of 'Goal Programming'.

Construct a goal programming problem using the following facts. Show the deviational variables in the constraints.

| Resource type | Product 1 | Product 2 | Available Resource |
| :--- | :--- | :--- | :--- |
| Labor hours | 2 | 4 | 600 |
|  |  |  |  |
| Material 1 | 4 | 5 | 1000 |
| Material 2 | 5 | 4 | 1200 |
| Profit per Unit | Rs. 20 | Rs. 32 |  |

It is known that production of one unit of product 1 , would maintain 0.3 person and one unit of production of product 2 would maintain 0.75 person. The manager has set up two goals (1) profit of Rs. 5400 and (2) A total staff of 108 persons.
(b) Identify the differences between Parametric and non-Parametric tests. in the context of $\chi^{2}$ test, comment on 'Goodness of fit is identified by badness of fit'. It is hypothesized by a researcher that the three cities A, B , and C have selling potential of a product in the ratio 2:3:4. The sales manager of the company gave the actual sales figures 380,640 , and 780 in the respective cities. What test do you suggest? Perform basic steps towards the solution and find the calculated value. (There is no need of searching for 'Table value'.)

## OR

(b) What is a research? State each aspect of a good research and write distinct features or characteristics of that aspect.
Q. 3 (a) Define hypothesis in research terminology. What is a null hypothesis? Give important features on each of the followings.
(1) Descriptive Hypothesis (2) Relational Hypothesis (3) Co relational Hypothesis, and
(4) Explanatory Hypothesis. Explain type-I and type -II errors.
(b) It was claimed that persons crossing certain age group may not like to change their
reading habits. The study of 22 randomly selected persons divided in two equal
groups, the total numbers of books or magazines they read during a span of one year
are as follows.

Average books read

| Group A | Group B |
| :--- | :---: |
| 1500 | 1300 |

Standard Deviation $225 \quad 251$
Do the two groups means differ from each other? (Use $0.05 \%$ level of significance )

OR
Q. 3 (a) Briefly discuss the two important features -(1) Accuracy and (2) Precision of a good sample. Discuss Cluster Sampling and Double Sampling.
(b) Find a simple (linear ) regression using the following data and also graph the relation
you obtain.

| $X$ | $Y$ |
| :---: | :---: |
| 12 | 2000 |
| 16 | 3000 |
| 20 | 4000 |
| 24 | 5000 |

Q. 4 (a) Describe the complete procedure of finding graphical solution of a linear programming problem. What do you understand by 'convex region'? Discuss one special case in the graphical solution of such problem.
(b) What do we mean by 'Duality'? Write some important features of 'Primal \& Dual' problem.
Write the dual of the following problem.
Maximize $10 \mathrm{Y}_{1}+8 \mathrm{Y}_{2}-6 \mathrm{Y}_{3}$ subject to the following constraints.
$3 \mathrm{Y}_{1}+\mathrm{Y}_{2}-2 \mathrm{Y}_{3} \leq 10,-2 \mathrm{Y}_{1}+3 \mathrm{Y}_{2}-\mathrm{Y}_{3} \geq 12, \quad \mathrm{Y}_{1}, \quad \mathrm{Y}_{2}, \quad \mathrm{Y}_{3} \geq 0$

> OR
Q. 4 (a) Write the dual of the following problem. Graph both the Primal and its Dual.

Maximize $\mathrm{Z}=5 \mathrm{X}+7 \mathrm{Y}$, Subject to $\mathrm{X}+\mathrm{Y} \leq 4, ~ 3 \mathrm{X}+8 \mathrm{Y} \leq 26, ~ 10 \mathrm{X}+7 \mathrm{Y} \leq 35$ $\mathrm{X}, \mathrm{Y} \geq 0$
(b) Find an initial basic feasible solution to the following transportation problem. Is it an optimal one ?

| FROM | D1 | D2 | D3 | D4 | AVAILABLE <br> UNITS |
| :--- | :--- | :--- | :--- | :--- | :--- |
| O1 | 5 | 4 | 2 | 1 | 130 |
| O2 | 2 | 3 | 7 | 5 | 100 |
| O3 | 5 | 4 | 5 | 6 | 30 |
| DEMAND | 40 | 50 | 70 | 100 |  |

Q. 5 (a) Solve the following assignment problem. (Assign one machine to one worker so that total time in hours is minimized.)

| Machine Matrix |  |  |  |  |  |  | M1 | M2 | M3 | M4 | M5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Man |  |  |  |  |  |  |  |  |  |  |  |
| A | 3 | 2 | 7 | 4 | 8 |  |  |  |  |  |  |
| B | 5 | 4 | 3 | 8 | 5 |  |  |  |  |  |  |
| C | 3 | 7 | 9 | 1 | 2 |  |  |  |  |  |  |
| D | 4 | 2 | 6 | 5 | 7 |  |  |  |  |  |  |
| E | 2 | 8 | 4 | 6 | 6 |  |  |  |  |  |  |

(b) Explain the basic concepts of Sensitivity Analysis. What are the different factors affecting the given solutions and how do we resolve them? Give a brief comment on each of them.

## OR

Q. 5 (a) What is a travelling salesman's problem?

Stating an upper bound of the solution, solve the problem.
You are required to design a complete route for a salesman who begins from the city ' $A$ ' and he is required to return to the same city ' $A$ '. The distances in miles between the cities are given as follows.

| TRQ <br> FRQ | A | B | C | D | E | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | --- | 25 | 18 | 35 | 50 | 39 |
| B | 21 | --- | 28 | 16 | 30 | 13 |
| C | 22 | 28 | ---- | 14 | 16 | 20 |
| D | 35 | 12 | 14 | ---- | 12 | 12 |
| E | 50 | 30 | 16 | 12 | ----- | 8 |
| F | 39 | 15 | 20 | 12 | 7 | ----- |

(b) What is Simulation? Describe Monte Carlo Simulation. Explain applications of 07 simulation in business environment.

