

VIII. (a) The open loop transfer function of a unity feedback control system is $G(s) = \frac{k}{S(1+0.5s)}$. It is required that the velocity error constant should be at least 15 and that the phase margin is atleast 40° . Design a compensator for the same. (12)

(b) Explain lead and lag-lead compensation networks. (8)

IX. (a) What are the advantages and disadvantages of state variable approach compared to conventional approach? (8)

(b) The driving function $r(t)$ and the response function $c(t)$ of a single input single output system are related by

$$a_3 \frac{d^3 c}{dt^3} + a_2 \frac{d^2 c}{dt^2} + a_1 \frac{dc}{dt} + a_0 c(t) = b_0 r(t)$$

Form a state variable model of the system. (12)

OR

X. Write short notes on:

- (i) AC Servo motor
- (ii) Hydraulic Controllers
- (iii) Stepper Motors
- (iv) Magnetic Amplifier (20)

EB/CS/EI/EC 605 CONTROL SYSTEMS

ENGINEERING

(1999 Admissions)

Time: 3 Hours

Maximum Marks: 100

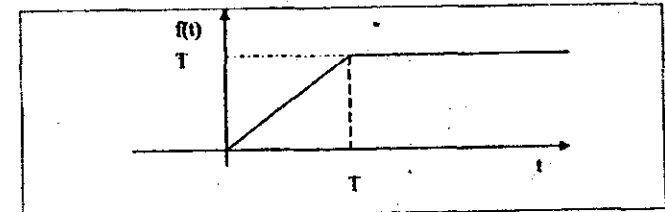
I. (a) Obtain the Laplace transform of the function defined by
 $f(t) = 0$ for $t < 0$
 $f(t) = t^2 e^{-at}$ for $t > 0$ (6)

(b) Determine the Inverse Laplace transform for the function
 $F(s) = 1 / s(s^2 + w^2)$ (6)

(c) Solve the following differential equation
 $\ddot{x} + 2\xi w_n \dot{x} + w_n^2 x = 0$ where $x(0) = a$; $\dot{x}(0) = b$
 where a and b are constants. (8)

OR

II. (a) Obtain the Laplace transform of the function $f(t)$ shown in the figure below: (6)



(b) Find the Inverse Laplace transform for the function

$$F(s) = \frac{(s+1)}{s(s^2+s+1)} \quad (6)$$

(c) Solve the following differential equation $2\ddot{x} + 7\dot{x} + 3x = 0$;
 $x(0) = 3$; $\dot{x}(0) = 0$. (8)

(Turn over)

- III. (a) Derive expressions for peak overshoot M_p and peak time t_p of the time response of a second order system subjected to a unit step input. (10)
- (b) A unity feedback control system has open loop transfer function $G(s) = K/s(s+1)$. Find the value of K for damping coefficient of 0.5. For this value of K determine peak time, maximum overshoot and settling time for unit step input. (10)

OR

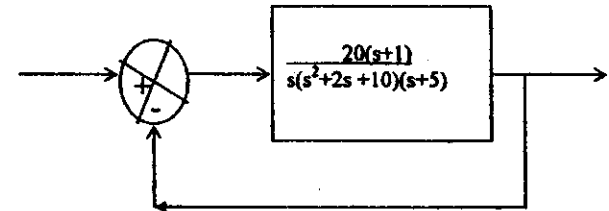
- IV. (a) The characteristic equation of a servo system is given by $a_0s^4 + a_1s^3 + a_2s^2 + a_3s + a_4 = 0$. Determine the condition which must be satisfied by the coefficients of the characteristic equation for the system to be stable. (10)
- (b) Measurements conducted on a servomechanism show the system response to be $c(t) = 1 + 0.2e^{-60t} - 1.2e^{-10t}$ when subjected to a unit step input.
- Obtain the expression for the closed-loop transfer function.
 - Determine the undamped natural frequency and damping ratio of the system. (10)

- V. (a) Sketch the root locus plot for a unity feedback system with $G(s) = \frac{K}{s(s+1)(s^2+4s+13)}$. Obtain the range of K for stability. (10)
- (b) The forward path transfer function $G(s)$ of a unity feedback system is $G(s) = \frac{K}{s(1+0.01s)(1+0.05s)}$. Draw the Bode plot and determine the gain margin and phase margin for $K = 50$. (10)

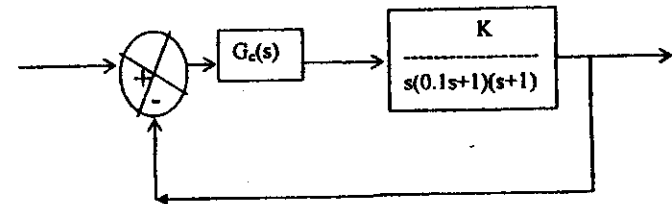
OR

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- VI. (a) Draw a Nyquist locus for the unity feedback control system with the open loop transfer function $G(s) = \frac{K(1-s)}{(s+1)}$. Using the Nyquist stability criterion, determine the stability of the closed loop system. (10)
- (b) Consider the system shown in figure below. Draw a Bode diagram of the open-loop transfer function $G(s)$. Determine the gain and phase margins. (10)



- VII. (a) For a closed loop system shown in figure, design a lead compensator $G_c(s)$ such that the phase margin is 45° , gain margin is not less than 8dB and the velocity error constant K_v is 4.0 sec^{-1} . (12)



- (b) How are the compensation networks used to modify the system characteristics? Explain using an example. (8)

OR

Contd.....4.