RITSAT-PILANI ENGINEERING ENTRANCE

A-PDFsMerger-DFMQ Purchas

Mathematics

through the int	of a parabola which passes ersection of a straight line or circle $x^2 + y^2 + 4y = 0$ is ;	equations	homogeneous system of $px + y + z = 0$, $x + qy + z = z = 0$, where $p, q, r \neq 1$, h
(a) $y^2 = 4x$	(b) $y^2 = x$	non-zero	solution, then the val
(c) $v^2 = 2x$	(d) none of these		1 1

- 2. The point (4, -3) with respect to the ellipse $4x^2 + 5y^2 = 1$ is:
 - (a) lies on the curve
 - (b) is inside the curve
 - (c) is outside the curve (d) is focus of the curve
- 3. If $\vec{a} = \hat{i} + 2\hat{i} 3\hat{k}$ and $\vec{b} = 3\hat{i} \hat{i} + 2\hat{k}$ then the angle between the vectors a + b and a - b is:

(a) 60° (b)90° (c) 45° (d) 55°

4. Let S be a set containing n elements and we select two subsets A and B of S at random, then the probability that $A \cup B = S$ and $A \cap B = \emptyset$. ic .

(b) n2 (a) 2" (c) 1/n (d) 1/2" $\sin^2 \theta$, $\sin^2 \theta$ $1 + \sin^2 \theta$

 $\cos^2 \theta = 0$. 5. $\cos^2 \theta$ 1 + $\cos^2 \theta$ 1 + 4 sin 40

then sin 40 equals to:

(a) 1/2 (d) -1 (c) - 1/2

6. The value of the constant α and β such that $\alpha x - \beta = 0$ are respectively :

(b) (-1, 1) (a) (1, 1) (d) (0, 1)

1-p 1-a 1-r 15: (b) 0

(d) 1 8. A point (α, β) lies on a circle $x^2 + y^2 = 1$, then

locus of the point $(3\alpha + 2\beta)$ is a/an: (a) straight line (b) ellinse

(c) parabola (d) none of these 9. If θ is an acute angle and $\sin \frac{\theta}{2} = \sqrt{\frac{x-1}{2x}}$, then

tan 0 is equal to: (b) $\sqrt{x^2 - 1}$ (a) $x^2 - 1$ (c) $\sqrt{x^2+1}$

10. The value of

is equal to:

(a) n

11. $\int_0^{2n\pi} \left\{ |\sin x| - \left| \frac{1}{2} \sin x \right| \right\} dx$ equals:

(b) 2n (c) -2n(d) none of the above

12. Range of the function f(x) =

(b) (-1, 1) (a) (-1, 0) (d) (1, 1) (c) [0, 1]

	1 Hour Source Laber-506
13. If $\sin^{-1}(1-x) - 2\sin^{-1}x = \pi/2$, then x is equals:	(a) -4 (c) 1 (b) 0 (d) 4
(a) (0, -1/2) (b) (1/2, 0) (c) (0) (d) (-1, 0) 14. sin A, sin B, cos A are in GP. Roots of x ² + 2 x cot B + 1 = 0 are always:	24. The number of solutions for the equations $ z-1 = z-2 = z-i $ is: (a) one solution (b) 3 solutions (c) 2 solutions (d) no solution
(a) real (b) imaginary (c) greater than 1 (d) equal 15. If $\int_{\log 2}^{\pi} \frac{du}{(e^{w}-1)^{3/2}} = \frac{\pi}{6}$, then e^{w} is equal to :	25. Let A and B are two events and $P(A') = 0$ $P(B) = 0.4$, $P(A \cap B') = 0.5$ then $P(A \cup B') = 0$ (a) 0.5 (b) 0.8 (c) 1 (d) 0.1
(a) 1 (c) 4 (b) 2 (d) -1	26. (10101101) ₂ = (
 Total number of books is 2n + 1. One is allowed to select a minimum of the one book and a maximum of n books. If total number of 	27. Given function $f(x) = \left(\frac{e^{2x} - 1}{e^{2x} + 1}\right)$ is:
selections if 63, then value of n is: (a) 3 (b) 6	(a) increasing (b) decreasing (c) even (d) none of these
(c) 2 (d) none of these 17. $x^2 = xy$ is a relation which is:	28. The solution of $x^2 + y^2 - 2xy \frac{dy}{dx} = 0$ is: (a) $x^2 - y^2 = cx$ (b) $x^2 + y^2 = cx$
(a) symmetric (b) reflexive (c) transitive (d) none of these	(c) $2(x^2 - y^2) = cx$ (d) none of these 29. $f(x) = ax^2 + bx + c$ and $g(x) = gx^2 + gx$ where
18. Let the determinant of a 3×3 matrix A be 6, then B is a matrix defined by $B = 5$ A^2 . Then determinant of B is : (a) 180 (b) 100 (c) 80 (d) none of these	29. $f(x) = ax^2 + bx + c$ and $g(x) = px^2 + qx$ as $g(1) = f(1)$, $g(2) - f(2) = 1$, $g(3) - f(3) = 0$ then $g(4) - f(4)$ is: (a) 0 (b) 5 (c) 6 (d) none of these
19. Let $f(x) = \begin{cases} 1 & \forall x < 0 \\ 1 + \sin x & \forall 0 \le x \le \pi/2 \end{cases}$	30. If the vectors $\alpha \hat{\mathbf{i}} + \hat{\mathbf{j}} + \hat{\mathbf{k}}$, $\hat{\mathbf{i}} + \beta \hat{\mathbf{j}} + \hat{\mathbf{k}}$ $\hat{\mathbf{i}} + \hat{\mathbf{j}} + \lambda \hat{\mathbf{k}} (\alpha, \beta, \gamma \neq 1)$ are coplanar, then
then what is the value of $f'(x)$ at $x = 0$? (a) 1 (b) -1 (c) ∞ (d) does not exist	value of $\frac{1}{1-\alpha} + \frac{1}{1-\beta} + \frac{1}{1-\gamma}$ is:
 (c) ∞ (d) does not exist 20. The length intercepted by the curve y² = 4x on 	(a) -1 (b) 0 (c) 1 (d) 1/2
the line satisfying $dy/dx = 1$ and passing through point $(0, 1)$, is given by: (a) 1 (b) 2 (c) 0 (d) none of these	 31. The circumcentre of a triangle formed by a line xy + 2x + 2y + 4 = 0 and x + y + 2 = 0 and x - 1 = 0. (a) (-1, -1) (b) (0, -1) (c) (1,1) (d) (-1, 0)

32. The number of common tangents to di $x^2 + y^2 + 2x + 8y - 23 = 0$ and $x^2 + y^2 - 4x - 10y + 9 = 0$, is: (b) 3 (a) 1

(d) none of these

33. If $\frac{x}{\alpha} + \frac{y}{\beta} = 1$ touches the circle $x^2 + y^2 = 1$ then point (1/a, 1/B) lies on a/an: (a) straight line (b) circle (c) parabola (d) ellipse

(c) 2

(d) 2 23. The largest value of $2x^3 - 3x^2 - 12x + 5$ for -25x 54 occurs at x is equal to :

(b) 1/2

21. Area bounded by curve $y = x^2$ and $y = 2 - x^2$

 $4\theta (\tan \theta - 2\theta \tan \theta)$ is:

(b) 3/8 sq units

(d) none of these

is: (a) 8/3 sq units

(c) 3/2 sq units

22. lim 0→0 (1 − cos 20)

(a) 1/√2

(c) 1

- 24. The point of intersection of the line 2x - y + 3z - 1 = 0 is: (a) (10, -10, 3) (b) (10, 10, -3) (c) (-10, 10, 3)
- (d) none of these as. The tangents from a point $(2\sqrt{2}, 1)$ to the hyperbola $16x^2 - 25y^2 = 400$ include an angle equal to:
 - (2) =/2 (b) =/4 (c) x (d) =/2
- 36. Let α, β, γ and δ are four positive real number such that their product is unity, then the least value of $(1 + \alpha)(1 + \beta)(1 + \gamma)(1 + \delta)$ is: (a) 6
- 37. Value of $\sum_{i=1}^{6} \left(\frac{2k\pi}{7}\right) i \cos\left(\frac{2k\pi}{7}\right)$ is equal to:
 - (a) -1(d) none of these
- 38. The degree of the differential equation
 - $y(x) = 1 + \frac{dy}{dx} + \frac{1}{1 \cdot 2} \left(\frac{dy}{dx}\right)^2 + \frac{1}{1 \cdot 2 \cdot 3} \left(\frac{dy}{dx}\right)^3 + \dots$
 - (a) 2
 - (d) none of these
- 39. Let $P(x_1, y_1)$ and $Q(x_2, y_2)$ are two points such that their abscissa x, and x, are the roots of the equation $x^2 + 2x - 3 = 0$ while the ordinate y_1 and y2 are the roots of the equation $v^2 + 4v - 12 = 0$. The centre of the circle with PO as diameter is:
 - (b) (1.2) (a)(-1, -2)(c) (1, -2)
- 40. The equation of plane passing through a
- (d) (-1, 2)
 - point A (2, -1, 3) and parallel to the vectors $\vec{a} = (3, 0, -1)$ and $\vec{b} = (-3, 2, 2)$ is:

- (a) 2x 3y + 6z 25 = 0(b) 2x - 3y + 6z + 25 = 0 (c) 3x - 2y + 6z - 25 = 0
- (d) 3x 2y + 6z + 25 = 0
- 41. The equation of a straight line drawn through the focus of the parabola $y^2 = -4x$ at an angle of 120° to the x-axis is: (a) $y + \sqrt{3}(x-1) = 0$
 - (b) $y \sqrt{3}(x-1) = 0$ (c) $y + \sqrt{3}(x+1) = 0$ (d) $y - \sqrt{3}(x+1) = 0$
- 42. Let $x = \alpha + \beta$, $y = \alpha \omega + \beta \omega^2$, $z = \alpha \omega^2 + \beta \omega$, ω is an imaginary cube root of unity. Product of xyz
 - (a) $a^2 + a^2$ (b) $\alpha^2 - \beta^2$ (c) $\alpha^3 + \beta^3$ (d) a3 - 82
- 43. If $r = \lceil 2b + \cos^2 (2b + \pi/4) \rceil^{1/2}$, then what is the value of the derivative of dr/do at 0 = 1/4?
 - (a) $2\left(\frac{1}{\pi+1}\right)^{1/2}$ (b) $2\left(\frac{2}{\pi+1}\right)^{1/2}$ (c) $\left(\frac{2}{z+1}\right)^{1/2}$ (d) $2\left(\frac{2}{z+1}\right)^{1/2}$
- 44. If a vector α lie in the plane of β and γ, then which is correct?
 - (a) $\begin{bmatrix} \alpha & \beta & \gamma \end{bmatrix} = 0$ (b) $\begin{bmatrix} \alpha & \beta & \gamma \end{bmatrix} = 1$ (b) [By a] = 1 (c) [\alpha \beta \vi] = 3
- 45. If $\vec{q} = 2\hat{i} + 3\hat{i} \hat{k}$, $\vec{\beta} = -\hat{i} + 2\hat{i} 4\hat{k}$ $y = \hat{i} + \hat{i} + \hat{k}$, then what is the value of
 - $(\vec{\alpha} \times \vec{\beta}) \cdot (\vec{\alpha} \times \vec{\gamma})$?
 - (a) 47 (b) 74
 - (c) -74
 - (d) none of the above

Physics

- 46. If M is the mass of the earth and R its radius, the ratio of the gravitational acceleration and the gravitational constants is:
 - (a) $\frac{R^2}{M}$
 - (c) MR2

- 47. A student unable to answer a question on Newton's laws of motion attempts to pull himself up by tugging on his hair. He will not
 - (a) as the force exerted is small (b) the frictional force while gripping, is small

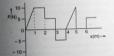
- (c) Newton's law of inertia is not applicable to 54. In the given circuit, the voltmeter recon-The resistance of the voltmeter in ohme (d) as the force applied is internal to the 48. Which one of the following is not a unit of (a) Nm-1 (b) Nm-2 (c) dyne cm-2 (d) mega pascal 49. A piece of blue glass heated to a high (a) 200 (b) 100 temperature and a piece of red glass at room
 - temperature, are taken inside a dimly lit room. then: (a) the blue piece will look blue and red will body depends upon : look as usual
 - (h) red looks brighter red and blue looks ordinary blue (c) blue shines like brighter red compared to
 - the red piece (d) both the pieces will look equally red
- 50. A 5.0 A current is setup in an external circuit by a 6.0 V storage battery for 6.0 min. The chemical energy of the battery is reduced by:
 - (a) 1.08 × 104 J
 - (b) 1.08 ×10⁻⁴ J (c) 1.8 ×104 J
 - (d) 1.8 × 10-4 J
- 51. The current in a simple series circuit is 5.0 A. When an additional resistance of 2.0 Ω is inserted, the current drops to 4.0 A. The original resistance of the circuit in ohms was : (a) 1.25 (b) 8
 - (c) 10 (d) 20
- 52. Two resistances are connected in two gaps of a metre bridge. The balance point is 20 cm from the zero end. A resistance of 15 \O is connected in series with the smaller of the two. The null point shifts to 40 cm. The value of the smaller resistance in ohms is :
 - (a) 3 (b) 6 (c) 9 (d) 12
- 53. By using only two resistance coils-singly, in series or in parallel one should be able to obtain resistances of 3, 4, 12 and 16 Ω . The separate resistances of the coil are :
 - (b) 4 and 12
 - (d) 16 and 3

(c) 90G

- (c) 10 (d) 50 55. The wavelength of the radiation em
 - (a) the nature of the surface (b) the area of the surface
 - (c) the temperature of the surface (d) all of the above factors
- 56. Which mirror is to be used to obtain an
- beam of light from a small lamp? (a) Plane mirror
 - (b) Convex mirror
 - (c) Concave mirror
- (d) Any one of the above 57. Which of the following is a wrong states
 - (a) D = 1/f where f is the focal length as called the refractive power of a len (b) Power is expressed in a diopter when
 - in metres (c) Power is expressed in diopter and do depend on the system of unit u
 - measure f (d) D is positive for convergent less
- negative for divergent lens 58. An electric field of 1500 V/m and a m field of 0.40 Wb/m2 act on a moving of
 - The minimum uniform speed along as line the electron could have is: (a) 1.6×10^{15} m/s (b) 6×10^{-16} m/s
 - (d) 3.75×10³m³ (c) 3.75 × 103 m/s
- 59. In an ammeter 10% of main current is through the galvanometer. If the resident the galvanometer is G, then the resistance, in ohms is:
 - (a) 9G

o. Among the following properties describing	65. Infrared
diamagnetism identify the property that is wrongly stated:	(a) Wil
(a) Diamagnetic material do not have permanent magnetic moment	(b) Wil (c) Wil
(b) Diamagnetism is explained in terms of	(d) The

- (c) Diamagnetic materials have a small
- positive susceptibility (d) The magnetic moment of individual
- electrons neutralize each other
- 61. The induction coil works on the principle of :
 - (a) self-induction
 - (b) mutual induction (c) Ampere's rule
 - (d) Fleming's right hand rule
- 62. The square root of the product of inductance and capacitance has the dimension of (b) mass (a) length
- (d) no dimension (c) time 63. The relationship between the force F and nosition x of a body is as shown in figure. The work done in displacing the body from x = 1 mto $x = 5 \,\mathrm{m}$ will be :



- (a) 30 J
- (b) 15 J
- (c) 25 J
- (d) 20 J
- 64. From the top of a tower of two stones, whose masses are in the ratio 1: 2 are thrown on straight up with an initial speed u and the second straight down with the same speed u. Then neglecting air resistance:
 - (a) the heavier stone hits the ground with a higher speed
 - (b) the lighter stone hits the ground with a higher speed (c) both the stones will have the same speed
 - when they hit the ground (d) the speed cannot be determined with the given data

- radiation was discovered in 1800 by : iam Wollaston
 - liam Herschel
 - helm Roentgen omas Younz
 - ele on the trough of a wave at any instant will come to the mean position after a time : (T = time period)
 - (a) T/2 (b) T/4 (c) T
- (d) 2T
- 67. The disc of a siren containing 60 holes rotates at a constant speed of 360 rpm. The emitted
 - sound is in unison with a tuning fork of frequency: (a) 10 Hz (b) 360 H₂
 - (c) 216 Hz (d) 60 Hz
- 68. The ratio of velocity of sound in hydrogen and oxygen at STP is -
 - (a) 16:1 (b) 8:1
- (c) 4:1 (d) 2:1 69. In an experiment with sonometer a tuning fork
 - of frequency 256 Hz resonates with a length of 25 cm and another tuning fork resonates with a length of 16 cm. Tension of the string remaining constant the frequency of the second
 - tuning fork is: (a) 163.84 Hz
 - (b) 400 Hz (c) 320 Hz
 - (d) 204.8 Hz
- 70. The wave theory of light, in its original form, was first postulated by:
 - (a) Isaac Newton
 - (b) Christian Huygens
 - (c) Thomas Young (d) Augustin Jean Fresnel
- 71. If a liquid does not wet glass, its angle of contact is: (b) acute
 - (a) zero (d) right angle
- (c) obtuse 72. Electron of mass m and charge q is travelling
 - with a speed v along a circular path of radius r at right angles to a uniform magnetic field of intensity B. If the speed of the electron is doubled and the magnetic field is halved the resulting path would have a radius:
 - (b) 4r
 - (a) 2r (d) r/2 (c) r/4

- Two coherent light beams of intensity I and 4I are superposed. The maximum and minimum possible intensities in the resulting beam are : (b) 91 and 31
 - (d) 5 I and 3 I
- 74. The electron in a hydrogen atom makes a transition form $n = n_1$ to $n = n_2$ state. The time period of the electron in the initial state (n_z) is eight times that in the final state(n2). The possible values of n, and n, are :
 - (a) $n_1 = 8$, $n_2 = 1$
 - (b) $n_0 = 4$, $n_0 = 2$ (c) $n_1 = 2 n_2 = 4$
 - (d) $n_1 = 1, n_2 = 8$
- 75. If the forward voltage in a diode is increased. the width of the depletion region : (a) increases
 - (b) decreases
- 76. Two nucleons are at a separation of one Fermi. Protons have a charge of + 1.6 × 10-19 C. The net nuclear force between them is F_1 , if both are neutrons, Fa if both are protons and Fa if one is proton and the other is neutron. Then :
 - (a) F, = F, > F,
 - (b) F₁ = F₂ = F₃
- (d) F, > F, > F. 77. The potential to which a conductor is raised, depends on .
 - (a) the amount of charge
 - (b) geometry and size of the conductor
 - (c) both (a) and (b) (d) only on (a)
- 78. The work done in carrying a charge q once round a circle of radius r with a charge Q at the

 - (d) none of the above
- 79. An air filled parallel plate condenser has a canacity of 2pF. The separation of the plates is

- doubled and the interspace between the planis filled with wax. If the capacity is increased 6 pF, the dielectric constant of wax is : (b) 3 (a) 2
- (d) 6 (c) 4 80. The energy that should be added to an electronic to reduce its de-Broglie wavelength from 1 no
 - to 0.5 nm is : (a) four times the initial energy
 - (b) equal to the initial energy
 - (c) twice the initial energy
 - (d) thrice the initial energy
- 81. Mean life of a radioactive sample is 100 s. The its half-life (in minutes) is: (a) 0.693
 - (d) 1.155 (c) 10⁻⁴
- 82. Consider two nuclei of the same radioaction nuclide. One of the nuclei was created in supernova explosion 5 billion years ago. The probability of decay during the next time is (a) different for each nuclei
 - (b) nuclei created in explosion decays first
 - (c) nuclei created in the reactor decays fire
- (d) independent of the time of creation 83. Bohr's atom model assumes:
 - (a) the nucleus is of infinite mas and is at ree
 - (b) electrons in a quantized orbit will not radiate energy
 - (c) mass of electron remains constant (d) all the above conditions
- 84. Identify the wrong statement in the following Coulomb's law correctly described the electric force that .
 - (a) binds the electrons of an atom to in nucleus
 - (b) binds the protons and neutrons in the nucleus of an atom
 - (c) binds atoms together to form molecules
- (d) binds atoms and molecules to form solids 85. When unpolarised light beam is incident from
 - air onto glass (n = 1.5) at the polarising angle-(a) reflected beam is polarised 100 percent
 - (b) reflected and refracted beams are partially polarised
 - (c) the reason for (a) is that almost all the light is reflected
 - (d) all of the above

as. Which of the following silver salts is insoluble in water?

(a) AeClO. (b) Ag-SO. (c) AgF (d) AgNO,

ay. Suitable reasents A and B for the following reactions are:

(a) Br, Br,

(b) Br., NBS (d) NBS, Br.

- (c) NBS NBS 88. KF combines with HF to form KHF. The compound contains the species:
 - (a) K' F and H' (b) K+ . F and HF (c) K* and (HF-)" (d) (KHF) and F-
- A. A will have configuration :

(b)

(c) both (a) and (b) (d) none of these 90. Among the following sets of quantum numbers. Which one is incorrect for 4d electron?

(b) 4, 2, 1, 0 (a) 4, 3, 2, + (d) 4, 2, 1, -1

- (c) 4, 2, -2, + 1 91. Raffinose is:
 - (a) trisaccharide
 - (b) monosaccharide
 - (c) disaccharide (d) none of the above
- 92. The molecular electronic configuration of Be2
 - (a) gls2g*1s2g2s2g*2n2
 - (b) KKg2s2 (c) ols20*15202520*242
 - (d) none of the above

- 93. Which of the following is deliquescent? (a) ZnCl. (b) Hg-Cl-(c) HgCl. (d) CdCl.
- 94. The velocity of electron in first orbit of H-atom. as compared to the velocity of light is : (a) 10th

(d) 1000th (d) same

(a) meso diol (b) racemic diol

- (c) both (a) and (b) (d) none of the above
- 96. In which of the following reactions is K < K?
- (a) 1₂ (g) ⇒ 2l(g) (b) 2BrCl(g) → Cl, (g) + Br, (g)
 - (c) $CO(g) + 3H_1(g) \Longrightarrow CH_4(g) + H_4O(g)$ (d) All of the above
- 97. For the reaction (at 1240 K and 1 atm.) $CaCO_{\gamma}(s) \longrightarrow CaO(s) + CO_{\gamma}(g)$
- $\Delta H = 176 \text{ kJ/mol}$: ΔE will be: (a) 160 kJ (b) 165.6 kJ (c) 186.4 kJ (d) 180 kJ
- 98. Following compound is treated with NBS

-CH-CH==CH2 + NBS -> A

Compound formed A is :

CHCH = CH,

CH - CHCH, Br

CH_CH=CH

99. The standard reduction potential of the reation, $H_0 \sim \epsilon \longrightarrow \frac{1}{2}H_2 + 0$ Hat 298 K is: (a) $E^* = \frac{RT}{F} \ln K_*$ (b) $E^* = -\frac{RT}{F} \ln [P_{H_2}]^{1/2}$ (OH') (c) $E^* = -\frac{RT}{F} \ln \frac{[P_{H_2}]^{1/2}}{[H']}$	(a) T ₁₁₂ − T ₁₁₂ (b) T ₁₁₂ − T ₁₂₂ (c) T ₁₁₂ − T ₁₁₂ (d) T ₁₁₂ − √TT ₁₁₂ 108. In P _{O 112} , the: (a) second bond in P _O − 0 is formed by p _T − q bonding (b) P _O − 0 bond is formed by p _T − q bonding (c) P _O − 0 bond is formed by d _T − q bonding (d) P _O − 0 bond is formed by d _T − q bonding (d) P _O − 0 bond is formed by d _T − q bonding
(d) $E^{\circ} = -\frac{RT}{F} \ln K_{+}$ 00. Glycerol is oxidised by bismuth nitrate to produce: (a) oxalic acid (b) mesooxalic acid	(d) P=O bond is formed by diff-diff-3er back bonding 109. Grignard reagent reacts with HCHO to produce: (a) secondary alcohol (b) anhydride (c) and acid
(c) glyceric acid (d) glyoxalic acid 101. Unit of frequency factor (A) is: (a) mol/L (b) mol/L×5 (c) depends upon order (d) it does not have any unit	(d) primary alcohol 110. Dacron is polymer of : (a) glycol and formaldehyde (b) glycol and phenol (c) glycol and phthalic acid
102. The change in pressure will not affect the equilibrium constant for: (a) N ₂ + 3H ₂ ≠ 2NH ₃ (b) PCl ₃ ≠ PCl ₃ + Cl ₂ (c) H ₃ + 1 ₂ ≠ 2HI (d) all of the above	(d) glycol and terephthalic acid 111. The product obtained by heating diethyl ether with HI is: (a) C₂H₃I (b) C₂H₃OH (c) C₂H₃OH + C₂H₃I
103. The volume strength of 1.5 N H ₂ O ₂ solution is : (a) 4.5 (b) 8.4 (c) 4.2 (d) 2.4 104. Bicyclo (1, 1, 0) butane is :	 (d) C₂H₅—C₂H₅ 112. For the gaseous reaction involving the complete combustion of isobutane: (a) ΔH = ΔE (b) ΔH > ΔE (c) ΔH < ΔE (d) none of these
(a) (b) (d) (d)	113. Natural rubber is a polymer of : (a) styrene (b) isoprene (c) ethylene (d) butadiene 114. Charles' law is represented mathematically as:
105. How many hydrogen bonds are present between pair of thymine and adenine in DNA? (a) 1-hydrogen bond (b) 2-hydrogen bonds (c) 3-hydrogen bonds (d) No bonds occur	(a) $V_t = KV_0 t$ (b) $V_t = \frac{KV_0}{t}$ (c) $V_t = V_0 \left(1 + \frac{273}{t}\right)$ (d) $V_t = V_0 \left(1 + \frac{t}{273}\right)$ 115. Cyanohydrin of which of the following forms
106. Graham's law deals with the relation between: (a) pressure and volume (b) density and rate of diffusion (c) rate of diffusion and volume (d) rate of diffusion and viscosity	lactic acid: (a) HCHO (b) CH ₂ CHO (c) CH ₂ CH ₂ CHO (d) CH ₂ COCH ₂ 116. Dinitrogen pentoxide (N ₂ O ₃), a colordes solid, is prepared by: (a) heating NH ₄ NO ₂ with an excess of oxyges
107. The rms speed of hydrogen is \$\sqrt{7}\$ times the rms speed of nitrogen. If T is the temperature of the gas, then:	(b) dehydrating HNO ₃ with CaO (c) dehydrating HNO ₃ with P _i O ₁₀ (d) heating a mixture of HNO ₂ and Ca(NO ₃)

111

12

1:

1:

1:

12

- 117. Which gas has the highest partial pressure in atmosphere?
 - (a) CO₂ (b) H₂O (b) O₂ (d) N₂
- 118. Acetone and acetaldehyde can be distinguished by:
 - (a) Molisch test (b)Tollen's test
- 119. Incorrect statement for pyrophosphorus acid
 - (a) contains P in +5 oxidation state
 (b) it is dibasic acid
 - (e) it is dibasic acid
 (e) it is strongly reducing in nature
- (d) it contains one P—O—P bond

 120. Which of the following compounds is not an
- "interpseudohalogen"?
 (a) Cl₂N₃ (b) BrCN
 - c) CICN (d) ICN

- 121. The oxidation number of oxygen in hydrogen peroxide is:
 (a) +1 (b) -1
 - (a) +1 (b) -1 (c) +2 (d) -2
- 122. Isopropyl bromide on Wurtz reaction gives:
 (a) hexane
 (b) propane
 - (c) 2, 3-dimethyl butane (d) neo-hexane
- 123. Tetraethyl lead is a:
- (a) solvent (b) petroleum additive
 (c) oxidising agent (d) fire extinguisher

 124. Solvay process is used for the manufacture of:
- 125. Milk of magnesia is used as:

 (a) antichlor (b) antacid
 (c) antiseptic (d) food preservative

English

Directions: Choose the correct meanings of Phrases/Idioms, out of the four responses given under each.

- 126. To meet one's Waterloo:

 (a) To meet a strong adversary
 - (b) To met with humiliation
 - (e) To die fighting
 - (d) To meet one's final defeat
- 127. Through thick and thin :
 - (a) Big and small (b) Large object
 - (c) Under all conditions
- (d) Thin and fat 128. An axe to grind:
 - (a) Difficult iob
 - (b) Hard labour (c) Private ends to serve
 - (d) Punishment
- 129. His wit's end :
 - (b) Confused
 - (c) Comedy
 (d) Very intelligent
 Directions: Find out the part which contains
 - an error in the following sentences. If there is no error, the answer is (d).

- 130. It is not advisable to take heavy luggages

 (a) (b)

 while on journey these days.

 (d)

 No error.

 (d)
- 131. Mr. Bose
 (a)
 accompanied by his wife and children
 - were present there. No error. (d)
- 132. You must pay respect to those who has
- (a)
 respect for you.
 (c)
 No error.
 (d)

 Directions: Choose the word that is most
 - nearly opposite in meaning to the word given incapital letters at the question place.
- 133. DREARY:
 (a) Drab
 (b) Dangerous
 (d) Bright
 - (c) Beautiful
- 134. GREGARIOUS: (a) Antisocial
 - (a) Antisocial (b) Horrendous
 - (c) Similar (d) Glorious

135. MISERLY (b) Spendthrift (d) Generous (c) Liberal Directions : Choose the word that is most nearly the same in meaning to the word given in capital letters at the question place.

136. DILIGENT (a) Industrious

(b) Energetic (d) Inteligent (c) Modest 137. RENOUNCE:

(a) Reform (b) Revoke (d) Resign (c) Retain

138. PROLIFIC: (b) Competent (a) Plenty (c) Predominant (d) Fertile

sentence R: having heard of the palmist

139. P. I decided to call on him Q: at the earliest opportunity

> S : before I came into town (a) RSPO (b) PORS (c) SOPR (d) OPRS

Directions : In each of the following queuis-

four parts of a sentence are given as P. Q. R.

S. Put them in proper order to produce the corre

140. P: when a chemical substance O: the food poisoning occurred

R: in the food preparations S: was mistaken for salt and used

(a) ROPS (b) SROP (c) OPSR (d) PSRO

Reasoning

141. Victory is related to Happiness in the same way as Failure is related to :

(a) Defeat (b) Anger

(d) Sadness (c) Frustration 142. In the following question, four groups of letters

are given. Three of them are alike in a certain way while one is different. Select the one which is different.

(a) RSXY (c) MNST (b) NOUV (d) DEJK

143. Complete the pattern in fig (x) by selecting one of the figures from the four alternatives:





144. In the following question, a statement/ group of statements is given followed by some conclusions. Choose the conclusion which logically follows from the given statement.

Statements:

1. Only students can participate in the race.

2. Some participants in the race are females. 3. All female participants in the race are insite for coaching

Conclusions :

(a) All participants in the race are invited for coaching.

(b) All participants in the race are males.

(c) All students are invited for coaching. (d) All participants in the race are students.

145. Consider the figures X and Y showing a rectangular sheet of paper folded in fig. X and punched in fig. Y. From amongst the answer figures a, b, c and d, select the figure, which wil most closely resemble the unfolded position of fig. Y.



146. Which one of the given sets of figures follow the following rule.

(c)

Rule: "Sectors get converted to triangles of by one".



Direction: In the following question find out which of the figures (a), (b), (c) and (d) can be formed from the pieces given in (X).

147. (X)

Direction: Find the missing character from among the given alternatives.



(a) 25

(b) 37 (c) 41 (d) 47 149. What terms will fill the blank spaces? Z, X, V, T, R, (....), (....)

(a) O. K (b) N. M (c) K. S (d) P. N

Direction : In the following question, choose the set of figures which follows the given rule.

150. Rule : Closed figures become more and more open and open figures become more and more closed





ATHEMATICS

■ MA	MEIRIN	AIICS												•	144
33.	(c) (b) (c) (b) (b)	2. 10. 18. 26. 34.	(c) (d) (a) (b) (b)	3. 11. 19. 27. 35.	(b) (b) (d) (a) (a)	4. 12. 20. 28. 36. 44.	(d) (c) (c) (a) (b) (a)	5. 13. 21. 29. 37. 45.	(c) (a) (d) (d) (d)	6. 14. 22. 30. 38.	(a) (d) (c)	7. 15. 23. 31. 39.	(d) (c) (d) (a) (a)	24. 32.	(b) (a) (c) (a)

78. (d)

- PH	YSICS						-		(a)	51.	(b)	52.	(c)	53.	(d)
46. 54. 62. 70.	(b)	47. 55. 63. 71.	(c)	64. 72.	(c)	73.	(c) (c) (b) (a)	50. 58. 66. 74. 82.	(c) (b) (b) (d)	59.	(b)	60. 68. 76. 84.	(c) (b) (b)	61. 69. 77. 85.	

86. 94. 102. 110. 118.	(b) (d) (d)	87. 95. 103. 111. 119.	(b) (c)	88. 96. 104. 112. 120.	(c) (a) (c) (b) (a)	89: 97. 105. 113. 121.	(b) (b) (b) (b) (b)	90. 98. 106. 114. 122.	(b) (b) (d) (c)	91. 99. 107. 115. 123.	(a) (a) (c) (b) (b)	92. 100. 108. 116. 124.	(a)	101.	
- EN	GLISH	1													
	(d)	127.	(c)	128.	(c)	129.	(b)	130.	(b)	131.	(c)	132.	(b)	133.	

REASONING

149

HINTS & SOLUTIONS

144. (d) 145. (d) 146. (b)

Mathematics

150

1. Given equation of line is x + y = 0and equation of circle is $x^2 + y^2 + 4y = 0$...(ii) On solving Eqs. (i) and (ii). $x^2 + (-x)^2 + 4(-x) = 0$ $2x^2 - 4x = 0$ 2x(x-2)=0x = 0, 2 and y = 0, -2Now taking option (c) ie $v^2 = 2x$ at poing $(0,0) \Rightarrow 0 = 0$ and at point (2, -2) \Rightarrow $(-2)^2 = 2(2) \Rightarrow 4 = 4$.. option (c) is the correct answer. 2. Given equation of ellipse is $4x^2 + 5y^2 = 1$ $S = 4x^2 + 5y^2 - 1 = 0$...(i) At point (4, -3) $S = 4(4)^2 + 5(-3)^2 - 1$ = 108 > 0 Therefore the given point lies outside the

3. Given that $\vec{a} = \vec{i} + 2\vec{j} - 3\vec{k} \text{ and } \vec{b} = 3\vec{i} - \vec{j} + 2\vec{k}$ Now, $\vec{a} \cdot \vec{b} = \vec{i} + 2\vec{j} - 3\vec{k} + 3\vec{i} - \vec{j} + 2\vec{k}$ $= 4\vec{i} - \vec{j} - \vec{k}$ and $\vec{a} - \vec{b} = (\vec{i} + 2\vec{j} - 3\vec{k}) - (3\vec{i} - \vec{j} + 2\vec{k})$ $= -2\vec{i} + 3\vec{j} - 5\vec{k}$

147. (a)

 $\begin{aligned} &= -2 + 3j - 5k \\ &\text{Let } \theta \text{ be the angle between } \vec{\mathbf{a}} + \vec{\mathbf{b}} \text{ and } \vec{\mathbf{a}} - \vec{\mathbf{b}} \end{aligned}$ $& \cos \theta = \frac{(\vec{\mathbf{a}} + \vec{\mathbf{b}}) \cdot (\vec{\mathbf{a}} - \vec{\mathbf{b}})}{|\vec{\mathbf{a}} - \vec{\mathbf{b}}|} = \frac{(\vec{\mathbf{a}} + \hat{\mathbf{j}} - \hat{\mathbf{k}}) \cdot (-2\hat{\mathbf{a}} + 3\hat{\mathbf{j}} - 5\hat{\mathbf{k}})}{|\vec{\mathbf{a}} - \vec{\mathbf{b}}| \cdot |\vec{\mathbf{a}} - 2\hat{\mathbf{a}} + 3\hat{\mathbf{j}} - 5\hat{\mathbf{k}}|} = \frac{(\vec{\mathbf{a}} + \hat{\mathbf{j}} - \hat{\mathbf{k}}) \cdot (-2\hat{\mathbf{a}} + 3\hat{\mathbf{j}} - 5\hat{\mathbf{k}})}{|\vec{\mathbf{a}} - \hat{\mathbf{a}}| \cdot |\vec{\mathbf{a}} - 2\hat{\mathbf{a}} - 2\hat{\mathbf{k}}|} = \frac{-8 + 3 + 5}{\sqrt{16 + 1 + 1} \sqrt{4 + 9 + 25}} = 0$

4. Let A and B be two subsets of S. There are following cases to make a subset of S, under the given condition i.e. A ∪ B = S and A ∩ B = Case I: If set A has no element. The number of ways of selection of 0 element from set S is Vernage.

Case II: If set A has one element. The number of ways of selection of one element from set S is

Case III : If set A has two elements. The number of ways of selection of two element from set S is "Ca.

Case (n) : If set A has n elements. The number of ways of selection of n elements from set .. Total set of A = "C0 + "C1 + "C2 + ... + "Ca

$$= 2^n$$
Total set of A and B = $2^n \times 2^n - 2^{2n}$

Total set of A and
$$B = 2^n \times 2^n = 2^n$$

$$\therefore \text{ Required probability} = \frac{2^n}{2^{2n}} = \frac{1}{2^n}$$

5. Let
$$A = \begin{bmatrix} 1 + \sin^2 \theta & \sin^2 \theta & \sin^2 \theta \\ \cos^2 \theta & 1 + \cos^2 \theta & \cos^2 \theta \end{bmatrix} = 0$$

Applying
$$R_1 \rightarrow R_1 + R_2$$

$$2$$

$$\Rightarrow \cos^2 \theta \qquad 1 + \cos^2 \theta \qquad \cos^2 \theta = 0$$

$$4 \sin 4\theta \qquad 4 \sin 4\theta \qquad 1 + 4 \sin 4\theta$$

Applying
$$C_1 \to C_1 - 2C_3$$
, $C_2 \to C_2 - 2C_3$
0 1

$$\Rightarrow -\cos^2 \theta \qquad 1 - \cos^2 \theta \qquad \cos^2 \theta = 0$$

$$-2 - 4 \sin 4\theta \qquad -2 - 4 \sin 4\theta \qquad 1 + 4 \sin 4\theta$$

 $[\cos^2 \theta (2 + 4 \sin 4\theta) + (1 - \cos^2 \theta) (2 + 4 \sin 4\theta)] = 0$ \Rightarrow [2cos² θ + 4 cos² θ sin 4θ + 2 + 4 sin 4θ $-2\cos^2 \theta - 4\cos^2 \theta \sin 4\theta = 0$

$$2 + 4 \sin 4\theta = 0$$

$$\sin 4\theta = -\frac{1}{2}$$

6. Given that,

$$\lim_{x \to \infty} \left(\frac{x^2 + 1}{x + 1} - \alpha x - \beta \right) = 0$$

$$\Rightarrow \lim_{x \to \infty} \left(\frac{x^2 + 1 - \alpha (x^2 + x) - \beta (x + 1)}{x + 1} \right) = 0$$

$$\Rightarrow \lim_{x \to \infty} \left(\begin{array}{c} x + 1 \\ \text{Using L-Hospital's rule, we get} \\ \lim_{x \to \infty} \left(\frac{2x - \alpha (2x + 1) - \beta(1)}{1} \right) = 0 \end{array} \right)$$

If this limit is zero, then the function $2x - \alpha (2x + 1) - \beta = 0$ x(2-2a)-(a+0)=0Equating the coefficient of x and constant terms, we get

 $2 - 2\alpha = 0$ and $\alpha + \beta = 0$

 $\alpha = 1$, $\beta = -1$ 7. Given equations are

px + y + z = 0, x + qy + z = 0, x + y + rz = 0Since the system have a non-zero solution,

Applying $C_2 \rightarrow C_2 - C_3$ $C_3 \rightarrow C_3 - C_2$ $p \quad 1 - p \quad 0$ and

$$\Rightarrow (1-p)(1-q)(1-r)\begin{vmatrix} \frac{p}{1-p} & 1 & 0 \\ \frac{1}{1-a} & -1 & 1 \\ 0 & 1 & 1 \end{vmatrix} = 0$$

$$\Rightarrow \frac{(1-p)(1-q)(1-r)}{\left[\frac{1}{1-r} \quad 0 \quad -1\right]}$$

$$\Rightarrow \frac{(1-p)(1-q)(1-r)}{\left[\frac{p}{1-r}(1)-\left(-\frac{1}{1-q} - \frac{1}{1-r}\right)\right]} = 0$$

Since,
$$p, q, r \neq 1$$

$$\therefore \frac{p}{1-p} + \frac{1}{1-q} + \frac{1}{1-r} = 0$$

$$\Rightarrow \frac{1-p}{1-p} - 1 + \frac{1}{1-q} + \frac{1}{1-r} = 0$$

$$\Rightarrow \frac{1-p}{1-p} + \frac{1-q}{1-q} + \frac{1}{1-r} = 1$$

8. Given that (α, β) lies on the circle $x^2 + y^2 = 1$ $\alpha^2 + \beta^2 = 1$

or it can be rewritten as
$$\frac{1}{9} (9\alpha^2 + 4 + 12\alpha) + \beta^2 = 1 + \frac{1}{9} (4 + 12\alpha)$$

$$\Rightarrow \frac{1}{9} (3\alpha^2 + 2)^2 + \beta^2 = 1 + \frac{4}{9} (1 + 3\alpha + 1) - \frac{4}{9}$$

$$\Rightarrow \frac{1}{9} (3\alpha + 2)^2 + \beta^2 = \frac{5}{9} + \frac{4}{9} (3\alpha + 2)$$
The locus of $(3\alpha + 2, \beta)$ is
$$\frac{1}{9} x^2 + y^2 = \frac{5}{9} + \frac{4}{9} x$$

 $x^2 - 4x + 9x^2 - 5 = 0$ On comparing this equation with $ax^2 + 2hxy + by^2 + 2ex + 2fy + c = 0$ a = 1, b = 9, h = 0, g = -2, f = 0, c = -5

Now. $\Delta = abc + 2feh - af^2 - be^2 - ch^2$

=1×9×(-5)+2(0)-1(0)2-9(-2)2-0 -- 45 - 36 - - 81 - 0 Now. $h^2 - ab = 0 - 9(1) = -9 < 0$

 $\Delta \neq 0$ and $h^2 < ab$. Hence, it is an ellipse.

9. Given that

 $\sin \frac{\theta}{2} = \sqrt{\frac{x-1}{2\pi}}$

$$\tan \theta = \frac{2\tan \frac{\theta}{2}}{1 - \tan^2 \frac{\theta}{2}}$$

$$= \frac{2\sqrt{\frac{x-1}{x+1}}}{1 - \frac{x-1}{x+1}} - \frac{2\sqrt{\frac{x-1}{x+1}}}{\frac{x-1}{x+1}}$$

$$f(\theta) = \begin{bmatrix} \sin^2 \theta \\ \int_0^{\sin^2 \theta} \sin^{-1} \sqrt{\phi} \ d\phi + \int_0^{\cos^2 \theta} \cos^{-1} \sqrt{\phi} \ d\phi \end{bmatrix}$$

 $f'(\theta) = \frac{d}{d\theta} \sin^2 \theta \left[\sin^{-1} \sqrt{\sin^2 \theta} \right]$

+
$$\frac{d}{d\theta}\cos^2\theta \left[\cos^{-1}\sqrt{\cos^2\theta}\right]$$

= $(2\sin\theta\cos\theta)\theta - (2\sin\theta\cos\theta)\theta$

 $f(\theta) = constant = a (say)$

$$f(\theta) = \text{constant} = a \text{ (say)}$$

$$f\left(\frac{\pi}{4}\right) = a$$

$$\Rightarrow \int_{0}^{1/2} \sin^{-1} \sqrt{\phi} \, d\phi + \int_{0}^{1/2} \cos^{-1} \sqrt{\phi} \, d\phi = a$$

$$\Rightarrow \int_{0}^{1/2} (\sin^{-1} \sqrt{\phi} + \cos^{-1} \sqrt{\phi}) \, d\phi = a$$

$$\frac{\pi}{2} [\phi]_0^{1/2} = \alpha$$

$$\frac{\pi}{4} = a$$

11. Let
$$I = \int_{0}^{2\pi\pi} \left\{ \left| \sin x \right| - \left| \frac{1}{2} \sin x \right| \right\} dx$$

$$= \int_{0}^{2n\pi} \left\{ |\sin x| - \frac{1}{2} |\sin x| \right\} dx$$

$$= \int_{0}^{2\pi x} \frac{1}{2} |\sin x| dx$$

$$= \int_{0}^{2\pi} \frac{1}{2} |\sin x| dx$$

$$= \frac{1}{2} \left[\int_{0}^{2\pi} |\sin x| \, dx + \int_{2\pi}^{4\pi} |\sin x| \, dx + \dots \right]^{2\pi\pi}$$

Now,
$$I_1 = \int_{1}^{2\pi} |\sin x| dx$$

$$I_1 = \int_0^{\pi} \sin x \, dx - \int_0^{2\pi} \sin x \, dx$$

= $[-\cos x]_0^{\pi} + [\cos x]_n^{2\pi} = -[-1-1] + [+1+1]$
= $2 + 2$

$$I = \frac{1}{2} [4 + 4 + 4 + ... n \text{ times}]$$

$$= \frac{1}{2} (4n) = 2n$$

12. Given that
$$f(x) = \frac{x^2}{x^2 + 1}$$

Since, it is an even function therefore its valu is always greater than equal to 0 and we know

$$x^2 < x^2 + 1$$
 or $\frac{x^2}{x^2 + 1} < 1$

: Required range is [0, 1). 13. Given $\sin^{-1}(1-x) + 2\sin^{-1}x = \frac{\pi}{2}$

$$\Rightarrow \sin^{-1}(1-x) = \frac{\pi}{2} + 2\sin^{-1}(x)$$

$$\Rightarrow (1-x) = \sin\left(\frac{\pi}{2} + 2\sin^{-1}x\right)$$

$$\Rightarrow (1-x) = \cos(2\sin^{-1}x)$$

But $x = \frac{1}{2}$ does not satisfy the given equation, So $x = \{0\}$ is the answer.

So, $x = \{0\}$ is the answer. 14. Since $\sin A$, $\sin B$ and $\cos A$ are in GP

i. Since $\sin A$, $\sin B$ and $\cos A$ are in GP $\sin^2 B = \sin A \cos A \qquad ...(i)$ $x^2 + 2x \cot B + 1 = 0 \qquad \text{(given)}$

Now, $b^2 - 4ac = 4 \cot^2 B - 4$ = $\frac{4 \cos^2 B - 4 \sin^2 B}{\sin^2 B} = \frac{4 (1 - \sin^2 B) - 4 \sin^2 B}{\sin^2 B}$

[from (i)]

 $\sin^2 B$ $4[1-2\sin A\cos A]$

 $\sin^2 B$ $= 4 \left(\frac{\sin A - \cos A}{\sin B} \right)^2 > 0$

:. Roots are always real.

15. Let $I = \int_{-\infty}^{\infty} \frac{du}{(e^{u} - 1)^{3/2}}$

or $I = \int_{\log 2}^{x} \frac{e^{u}}{e^{u} (e^{u} - 1)^{1/2}} du$

 $\begin{aligned} & \text{Let } e^{t} - 1 = t^{2} \Rightarrow e^{t} \ du = 2t \ dt \\ & = \int_{1}^{\sqrt{e^{t}} - 1} \frac{2t}{(t^{2} + 1)t} \ dt = 2 \int_{1}^{\infty} \frac{dt}{(1 + t^{2})} \\ & = [\tan^{-1} t]_{1}^{(e^{t} - 1)} = 2 \tan^{-1} \sqrt{e^{t}} - 1 - \tan^{-1} 1] \\ & \Rightarrow 2 \left[\tan^{-1} \sqrt{e^{t}} - 1 - \frac{\pi}{4} \right] = \frac{\pi}{6}. \end{aligned}$

 $\Rightarrow \tan^{-1} \sqrt{e^x - 1} = \frac{\pi}{12} + \frac{\pi}{4} = \frac{\pi}{3}$ $\Rightarrow \sqrt{e^x - 1} = \tan\left(\frac{\pi}{3}\right)$

 $\sqrt{e^x - 1} = \sqrt{3}$

16. Since $(1+x)^{2n+1} = C_0 + C_1 x + \dots + C_n x^n + C_{n+1} x^{n+1} + \dots + x^{2n+1}$

 $= 2(C_0 + C_1 + \dots + C_n x^n)$

 $(1+1)^{2n+1} = 2(C_0 + C_1 + ... + C_n)$ $\Rightarrow 2^{2n} = (C_1 + C_2 + ... + C_n)$

 $\begin{array}{ll} \Rightarrow & 2^{2n} - (C_0 + C_1 + ... + C_n) \\ \Rightarrow & 2^{2n} - 1 = C_1 + C_2 + ... + C_n \\ \Rightarrow & 2^{2n} - 1 = 63 \end{array}$

 $\Rightarrow 2^{2n} = 64 \Rightarrow 2^{2n} = 2^6$ $\Rightarrow 2n = 6 \Rightarrow n = 3$

17. Given that

 $x^{2} = xy$ Let $x, y \in \mathbb{R}$ $xBy = x^{2} = xy$ and $yRx = y^{2} = yx$ Now, $x^{2}y^{2} = xy^{2}x$ $x^{2} = xx$

.. It is transitive.

18. Given that $\det(A) = 6$...(Now, $B = 5A^2$

⇒ $det(B) = det(5 A^2)$ = $5 det(A^2) = 5 det(A)^2$ = $5 (6)^2$ (fr

⇒ det (B) = 180

19. Given that $f(x) = \begin{cases} 1 & \forall x < 0 \\ 1 + \sin x & \forall 0 \le x \le \pi/2 \end{cases}$

At x = 0 $LHD = \lim_{h \to 0} \frac{f(0 - h) - f(0)}{-h}$ $= \lim_{h \to 0} \frac{1 - 1}{-h} = 0$ $RHD = \lim_{h \to 0} \frac{f(0 + h) - f(0)}{h}$ $= \lim_{h \to 0} \frac{1 + \sin(0 + h) - 1}{h}$

 $= \lim_{h \to 0} \frac{\sin h}{h} = 1$ LHD \neq RHD

.. f'(x) does not exist at x = 0. 20. Given curve is $y^2 = 4x$

Let the equation of line by y = mx + cSince $\frac{dy}{dx} = m = 1$ and this line is passing through the point (0, 1).

 $1 = 1 (0) + c \Rightarrow c = 1$ y = x + 1

...(ii)

...(i)

Solving Eqs. (i) and (ii), we get $(x+1)^2 = 4x$ $(x-1)^2 = 0$

x=1 and y=2

This shows that line touch the curve at one point. So length of intercept is zero.

21. Given curves are

$$y = x^2 \qquad \dots$$
and
$$y = 2 - x^2$$

or $x^2 = -(y-2)$

or $x^2 = -(y-2)$...(If On solving Eqs. (i) and (ii), we get

and y = 1, 1

$$y = x^2$$
 $A(1, 1)$
 $y = 2 - x^2$

: Required area = Area of curve OABCO

= 2 Area of curve OABO = $2 \int_{1}^{1} y \, dx$ = $2 \int_{0}^{1} [(2 - x^{2}) - (x^{2})] \, dx$ = $2 \int_{0}^{1} (2 - 2x^{2}) \, dx$ = $4 \int_{0}^{1} x - \frac{x^{3}}{3} \int_{0}^{1} x^{3} dx$

 $=4\left[x-\frac{x^3}{3}\right]_0^1$ $=4\left[1-\frac{1}{3}\right]$

8 sq units

 $\lim_{\theta \to 0} \frac{4\theta (\tan \theta - 2\theta \tan \theta)}{1 - \cos 2\theta}$

 $\frac{4(\theta \tan \theta - 2\theta^2 \tan \theta)}{1 - \cos 2\theta}$

Using L' Hospital's rule $\frac{4 (0 \sec^2 \theta + \tan \theta - 4\theta \tan \theta - 2\theta^2 \sec^2 \theta)}{2 \sin 2\theta}$

Again using L' Hospital's rule $4 (\sec^2 \theta + 2\theta \sec^2 \theta \tan \theta + \sec^2 \theta - 4 \tan \theta)$ $= \lim_{n \to \infty} \frac{-4\theta \sec^2 \theta - 4\theta \sec^2 \theta - 4\theta^2 \sec^2 \theta}{4\cos^2 \theta}$

 $-\frac{4(1+0+1)}{4} = 2$

 $\frac{-}{4} = 2$ 23. Let $f(x) = 2x^3 - 3x^2 - 12x + 5$

23. Let $f(x) = 2x^3 - 3x^2 - 12x + 5$ $f'(x) = 6x^2 - 6x - 12$

Put f'(x) = 0, for maxima or minima.

 $6x^2 - 6x - 12 = 0$

 $\Rightarrow x^2 - x - 2 = 0$

 $\Rightarrow x^2 - 2x + x - 2 = 0$ $\Rightarrow (x - 2)(x + 1) = 0$

 $\Rightarrow (x-2)(x+1)=0$ $\Rightarrow x=-1,2$

Now, f''(x) = 12x - 6f''(-1) = -12 - 6 = -18 < 0

f(x) is maximum at x = -1.But x = 4

f(x) = 37. The largest value of f(x) is at x = 4

24. Let z = x + iy

|z-1| = |z-2| = |z-i| $\Rightarrow |(x-1)+iy| = |(x-2)+iy|$ = |(x+i(y-1)| $\Rightarrow x^2 - 2x + 1 + y^2 = x^2 + 4 - 4x + y^2$

 $= x^2 + y^2 + 1 - 2y$ Taking 1st and IInd term

 $\Rightarrow -2x + 1 = 4 - 4x$ $\Rightarrow 2x = 3$

Taking IInd and IIIrd term

⇒ 4 - 4x = 1 - 2y

 $\Rightarrow 4x - 2y = 3$ Taking Ist and IIIrd term

 $\Rightarrow -2x + 1 = 1 - 2y$ $\Rightarrow 2x - 2y = 0$

⇒ 3

From (i) $x = \frac{3}{2}$ On putting value of x in Eq. (iii), we set

On putting value of x in Eq. (iii), we $y = \frac{3}{2}$

On putting the value of x and y in Eq. (get $4\left(\frac{3}{2}\right) - 2\left(\frac{3}{2}\right) = 3$

⇒ 3 =
∴ One solution exist.

25. Given that, P(A') = 0.3 P(B) = 0.4 $P(A \cap B') = 0.5$ $P(B^*) = 1 - P(B) = 1 - 0.4 = 0.6$ P(A) = 1 - P(A') = 1 - 0.3 = 0.7 $P(A \cup B') = P(A) + P(B') - P(A \cap B')$ = 0.7 + 0.6 - 0.5 = 0.8

26. (10101101).

$$=1 \times 2^{7} + 0 \times 2^{6} + 1 \times 2^{5} + 0 \times 2^{4} + 1 \times 2^{3} + 1 \times 2^{4} + 1 \times 2^{3} + 1 \times 2^{4} + 1 \times 2^{3} + 1 \times 2^{4} + 1 \times$$

27. Given that
$$f(x) = \frac{e^{2x} - 1}{e^{2x} + 1}$$

On differentiating w.r.t. x, we get
$$f'(x) = \frac{2(e^{2x} + 1)(e^{2x}) - 2(e^{2x} - 1)(e^{2x})}{(e^{2x} + 1)^2} = \frac{2(e^{2x} + e^{2x})}{(e^{2x} + 1)^2} > 0$$

Function is an increasing

28. Given equation is

$$x^{2} + y^{2} - 2xy \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{x^{2} + y^{2}}{2xy} \qquad \dots$$

This is a homogeneous equation

we put y = vx and $\frac{dy}{dx} = v + x \frac{dv}{dx}$

The Eq. (i) is reduces to

$$v + x \frac{dv}{dx} = \frac{x^{2}(1 + v^{2})}{2x^{2}v}$$

$$x \frac{dv}{dx} = \frac{1 + v^{2}}{2v} - v = \frac{1 - v^{2}}{2v}$$

$$-\frac{2v}{x^{2}} dv = -\frac{dx}{x^{2}}$$

On integrating both sides, we get $\log(1-v^2) = -\log x + \log c$

 $\Rightarrow \log(x^2 - y^2) - 2\log x = -\log x + \log c$ $\log (x^2 - y^2) = \log xc$

$$\Rightarrow \qquad x^2 - y^2 = xc$$

29. : $f(x) = ax^2 + bx + c$ $g(x) = px^2 + qx$

> p+q=a+b+c ...(i) z(2) - f(2) = 1

4p + 2a - 4a - 2b - c = 1

...(ii)

also g(3)-f(3)=4 9p+3q-9a-3b-5-4 From Eqs. (i) and (ii) 2p = 2q - c + 1Now, g (4) - f (4)

-16p+4q-16q-4b-c =12p+4(p+q)-16q-4b-c=6-3e30. Since the given vectors $\alpha \hat{i} + \hat{j} + \hat{k} \hat{i} + \beta \hat{j} + \hat{k}$

and
$$\hat{i} + \hat{j} + \gamma \hat{k}$$
 are coplanar, then
$$\begin{vmatrix} \alpha & 1 & 1 \\ 1 & \beta & 1 = 0 \end{vmatrix} = 0$$

... (iii)

$$\begin{vmatrix} 1 & \beta & 1 \\ 1 & 1 & \gamma \end{vmatrix} = 0$$
Applying $C_2 \rightarrow C_3 = C_3 =$

$$\Rightarrow (1-\alpha)(1-\beta)(1-\gamma)\begin{vmatrix} 1-\alpha & 1 & 1 \\ \frac{1}{1-\beta} & -1 & 1 \\ \frac{1}{1-\gamma} & 0 & -1 \end{vmatrix} = 0$$

$$\Rightarrow \frac{(1-\alpha)(1-\beta)(1-\gamma)}{\left[\frac{\alpha}{1-\alpha}(1)-1\left(-\frac{1}{1-\beta}-\frac{1}{1-\gamma}\right)\right]=0}$$

$$\begin{bmatrix} 1-\alpha & 1 & 1-\beta & 1-\gamma \end{bmatrix}$$
Bur $\alpha \neq 1, \beta \neq 1$ and $\gamma \neq 1$

$$\vdots \frac{1}{(1-\alpha)} - 1 + \frac{1}{1-\beta} + \frac{1}{1-\gamma} = 0$$

$$\Rightarrow \frac{1}{1-\alpha} + \frac{1}{1-\beta} + \frac{1}{1-\beta} = 1$$

31. Given equation of lines are

$$xy + 2x + 2y + 4 = 0$$

or $(x + 2)(y + 2) = 0$
or $x + 2 = 0, y + 2 = 0$
and $x + y + 2 = 0$



...(16)

These three lines makes an right triangle CAB right angled at A.

The circumcentre of a triangle is the mid point of BC i.e. (-1,-1).

32. The centre and radius of the first circle $x^2 + y^2 + 2x + 8y - 23 = 0$ are $C_1(-1, -4)$ and $n = \sqrt{40}$

Similarly, the centre and radius of second circle $x^2 + y^2 - 4x - 10y + 9 = 0$ are $G_2(2, 5)$ and

Now, C, C = 1(2+1)2+(5+4)2 $=\sqrt{9+81}=\sqrt{90}$

 $r_1 + r_2 = \sqrt{40} + \sqrt{20}$ $r_1 - r_2 = \sqrt{40} - \sqrt{20}$

Here, $r_1 - r_2 < C_1 C_2 < r_1 + r_2$

 $x^2 + y^2 = a^2$

Two common tangents can be drawn.

33. Since the line $\frac{x}{a} + \frac{y}{a} = 1$ touches the circle

The perpendicular distance from centre (0, 0) to the tangent = radius of the circle

(b) to the tangent = radius
$$\Rightarrow \frac{-1}{\sqrt{\frac{1}{\alpha^2} + \frac{1}{\beta^2}}} = a$$

$$\Rightarrow \frac{1}{a^2} = \frac{1}{a^2} + \frac{1}{\beta^2}$$
The locus of $\left(\frac{1}{\alpha}, \frac{1}{\beta}\right)$ is
$$\frac{1}{a^2} = \frac{1}{x^2} + \frac{1}{y^2}$$

.. It represents a circle.

34. Given equation of line is
$$\frac{x-1}{3} = \frac{y+2}{4} = \frac{z-3}{2} = k$$
 (say)

Any point on the line is (3k+1, 4k-2-2k+3)

If the given line intersect the plane 2x - y + 3z - 1 = 0, then any point on the line lies in the plane.

: 2(3k+1)-(4k-2)+3(-2k+3)-1=0 $-4k + 12 = 0 \implies k = 3$

Point is (9 + 1, 12 - 2, -6 + 3) i.e., (10, 10, -3)

35. Equation of director circle of given hyperbola $\frac{x^2}{25} - \frac{y^2}{16} = 1$ is $x^2 + y^2 = 25 - 16$

 $x^2 + y^2 = 0$ This circle passes through $(2\sqrt{2}, 1)$ and we know that director circle is the locus of point of

intersection of perpendicular tangents drawn to a hyperbola. Thus the angle between the tangents is $\pi/2$.

36. Given that, it is given

As, we know A.M. > G.M. $1 + \alpha \ge 2\sqrt{\alpha}$ Similarly, $1 + \beta \ge 2\sqrt{\beta}$

Multiplying Eqs. (ii), (iii), (iv) and (v), we $(1 + \alpha)(1 + \beta)(1 + \gamma)(1 + \delta) \ge 16\sqrt{\alpha\beta\gamma\delta}$ $\Rightarrow (1 + \alpha)(1 + \beta)(1 + \gamma)(1 + \delta) = 16$

37. Given that

$$\begin{split} &\sum_{k=1}^{6} \left(\sin \left(\frac{2k\pi}{T} \right) - i \cos \left(\frac{2k\pi}{T} \right) \right) \\ &= -i \sum_{k=1}^{6} \cos \left(\frac{2k\pi}{T} \right) + i \sin \left(\frac{2k\pi}{T} \right) \\ &= -i \sum_{k=1}^{6} \left(\frac{2\pi}{T} \right)^{k} \\ &= -i \sum_{k=1}^{6} \left(\frac{2\pi}{T} \right)^{k} \\ &= -i \left(3 + r^{2} + \dots + r^{6} \right) \\ &= -i r \frac{(1 - r^{2})}{1 - r} = \frac{-(r - 1)}{1 - r} \\ &= \frac{-i (r - 1)}{1 - r} = i \quad \left\{ y \cdot r^{2} + e^{2k} \right\}. \end{split}$$

38. Given that

$$y(x) = 1 + \frac{dy}{dx} = \frac{1}{1 \cdot 2} \left(\frac{dy}{dx}\right)^2 + \frac{1}{1 \cdot 2 \cdot 3} \left(\frac{dy}{dx}\right)^3$$

or $y(x) = 1 + \frac{1}{1!} \left(\frac{dy}{dx}\right) + \frac{1}{2!} \left(\frac{dy}{dx}\right)^2 + \frac{1}{2!} \left(\frac{dy}{dx}\right)^3$.

 $y(x) = e^{dy/dx}$

Taking log on both sides, we get $\log y(x) = \frac{dy}{dx}$

.. The degree of this equation is 1.

39. Given
$$x_1$$
, x_2 are the roots of the equation
$$x^2 + 2x - 3 = 0$$
$$\Rightarrow x^2 + 3x - x - 3 = 0$$

x(x+3)-1(x+3)=0

(x-1)(x+3)=0 $x_1 = -3 \quad x_2 = 1$

and y1, y2 are the roots of the equation

 $y^2 + 4y - 12 = 0$

⇒
$$y^2 + 6y - 2y - 12 = 0$$

⇒ $y(y' + 6) - 2$ ($y + 6) = 0$
⇒ $(y - 2)(y + 6) = 0$
⇒ $y_1 = -2(y + 6) = 0$
⇒ $y_1 = -6$, $y_2 = 2$
⇒ Points are $P(-3 - 6)$ and $Q(1, 2)$.
Since, P and Q are the end points of a diameter.

40. The equation of any plane through (2, -1, 3) is a(x-2)+b(y+1)+c(z-3)=0 ...(i) where a, b and c are direction ratios, Since Eq. (i) is parallel to a and b

$$3a + 0b - c = 0$$
 ...(ii)
 $-3a + 2b - 2c = 0$...(iii)

Solving Eqs. (iii) and (iii), we get
$$\frac{a}{2} = -\frac{b}{6-2} = \frac{c}{6} = k$$
 (say)

$$\Rightarrow \qquad a=2k, b=-3k, c=6k$$

Putting the values of a, b and c in Eq. (i), we get 2k(x-2) - 3k(y+1) + 6k(z-3) = 0 $\Rightarrow 2x - 3y + 6z - 25 = 0$

which is a required equation of a plane.

41. Equation of parabola is

 $y^2 = -4x$

: focus is (-1, 0).

The equation of line passing through (-1, 0) is

y - 0 = m(x + 1) ...(i) Since, the line makes an angle $\theta = 120^{\circ}$

 $m = \tan \theta = \tan 120^{\circ}$

 $m = -\sqrt{3}$ On putting the value of m in Eq. (i), we get $y = -\sqrt{3}(x+1)$

42. Given that

Now, $xy = (\alpha + \beta)(\alpha +$

$$\begin{bmatrix} 1 + \omega + \omega^2 = 0 \\ \text{and } \omega^3 = 1 \end{bmatrix}$$

 $= (\alpha + \beta) (\alpha^2 - \alpha \beta + \beta^2)$ $= \alpha^3 + \beta^3$

43. Given that

$$r = \left[2\phi + \cos^2\left(2\phi + \frac{\pi}{4}\right)\right]^{3/2}$$
On differentiating w.r.t ϕ , we get

On differentiating w.r.t ϕ , we get $\frac{dr}{d\phi} = \frac{\left[2 - 2\cos\left(2\phi + \frac{\pi}{4}\right)\sin\left(2\phi + \frac{\pi}{4}\right) \cdot 2\right]}{2\sqrt{2\phi + \cos^2\left(2\phi + \frac{\pi}{4}\right)}}$

$$\frac{\left[1-\sin\left(4\phi+\frac{\pi}{2}\right)\right]}{\sqrt{2\phi+\cos^2\left(2\phi+\frac{\pi}{4}\right)}}$$

$$\Rightarrow \left(\frac{dr}{d\phi}\right)_{\phi = \pi/4} = \frac{\left[1 - \sin\left(\pi + \frac{\pi}{2}\right)\right]}{\sqrt{2 \cdot \frac{\pi}{4} + \cos^2\left(\frac{\pi}{2} + \frac{\pi}{4}\right)}}$$

$$= \frac{1 + 1}{\sqrt{\frac{\pi}{2} + \frac{1}{2}}} = 2\sqrt{\frac{2}{1 + \pi}}$$

44. Since, α lie in the plane of β and γ . It means that all three vectors are coplanar. $[\alpha \beta \gamma] = 0$

45. Given that

$$\vec{\alpha} = 2\hat{\mathbf{i}} + 3\hat{\mathbf{j}} - \hat{\mathbf{k}}, \vec{\beta} = -\hat{\mathbf{i}} + 2\hat{\mathbf{j}} - 4\hat{\mathbf{k}}$$

and $\vec{\mathbf{v}} = \hat{\mathbf{i}} + \hat{\mathbf{i}} + \hat{\mathbf{k}}$

Now,

$$\vec{\alpha} \times \vec{\beta} = \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 2 & 3 & -1 \\ -1 & 2 & -4 \end{vmatrix}$$

$$= \hat{\mathbf{i}} (-12 + 2) - \hat{\mathbf{j}} (-8 - 1) + \hat{\mathbf{k}} (4 + 3)$$

= -10\hat{\hat{i}} + 9\hat{\hat{j}} + 7\hat{\hat{k}}

and
$$(\overrightarrow{\alpha} \times \overrightarrow{\gamma}) = \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 2 & 3 & -1 \\ 1 & 1 & 1 \end{vmatrix}$$

$$= \hat{\mathbf{i}} (3+1) - \hat{\mathbf{j}} (2+1) + \hat{\mathbf{k}} (2-3)$$

$$= -4\hat{\mathbf{i}} - 3\hat{\mathbf{j}} - \hat{\mathbf{k}}$$

Now, $(\vec{\alpha} \times \vec{\beta}) \cdot (\vec{\alpha} \times \vec{\gamma})$

$$= (-10\hat{\mathbf{i}} + 9\hat{\mathbf{j}} + 7\hat{\mathbf{k}}) \cdot (4\hat{\mathbf{i}} - 3\hat{\mathbf{j}} - \hat{\mathbf{k}})$$
$$= -40 - 27 - 7$$

46. Gravitational acceleration is given by

$$g = \frac{GM}{R^2}$$
where G = gravitational constant
$$\frac{g}{R} = \frac{M}{R^2}$$

- 47. In this case the internal force is applied on the system, so he will not succeed. According to Newton's law the state of a body can only be changed if some external force is applied on it.
- 48. $y = \frac{\text{stress}}{\text{errain}} = N/m^2 \text{ or pascal}$ (in SI system)

and
$$y = \frac{\text{dyne}}{\text{cm}^2}$$
 (in CGS System)

Thus, Nm⁻¹ is not the unit of Young's modulus.

- 49. According to Stefan's law the energy emitted by a body per second is directly proportional to the fourth power of the temperature of the body. Here, the temperature of blue glass is more than that of red glass, so it will look brighter.
- 50. Chemical energy reduced

51. Let the original resistance is $R \Omega$.

$$V = I R$$

$$V = 5 \times R = 5 R$$

...(i)

When 2Ω resistance is inserted, then total resistance = $(R + 2)\Omega$ V = I'(R + 2) = 4(R + 2) (iii)

$$V = I'(R + 2) = 4(R + 2)$$
 ...(ii)
From Eqs. (i) and (II), we get
 $SR = 4(R + 2)$

$$R = 8\Omega$$

= $100 + \frac{75}{4} = \frac{475}{4}\Omega$
= 118.75Ω

52. Let S be the large and R be the smaller resistance.
From formula for metro bridge.

From formula for metre bridge
$$S = \left(\frac{100 - l}{l}\right)R$$

$$= \frac{100 - 20}{20}R = 4R$$

Again,

$$S = \left(\frac{100 - l}{100}\right)(R + 15)$$

$$= \frac{100 - 40}{40}(R + 15)$$

$$= \frac{3}{2}(R + 15)$$

$$4R = \frac{3}{2}(R + 15)$$

 $\frac{8R}{3} - R = 15 \implies \frac{5R}{3} = 15$

 $R = 9\Omega$ 53. If we take $R_1 = 4\Omega R_2 = 12\Omega$,

53. If we take $R_1 = 4\Omega R_2 = 12t$ then in series resistance $R = R_1 + R_2$

=
$$4 + 12$$

= 16Ω
In parallel, resistance $R = \frac{4 \times 12}{160} = 3\Omega$

So, $R_1 = 4\Omega$ and $R_2 = 12\Omega$

54. Let the resistance of voltmeter is GΩ.
∴ Total resistance of the circuit

 $R = \left(\frac{G \times 100}{G + 100} + 50\right)\Omega$

Total current
$$i = \frac{V}{R}$$

$$= \frac{10}{\left(\frac{G \times 100}{G + 100} + 50\right)}$$

Voltage across 100Ω resistance = $i \left(\frac{G \times 100}{G + 100} \right) = \frac{10}{\left(\frac{G \times 100}{G + 100} + 50 \right)} \times \left(\frac{G \times 100}{G + 100} \right)$

Reading of voltmeter = 5 V $Voltage across 100 \Omega = 5 V$ $\therefore 5 = \frac{10}{\left(\frac{G \times 100}{G + 100} + 50\right)} \times \left(\frac{G \times 100}{G + 100}\right)$

On solving $G = 100 \Omega$. 55. According to Wien's law $\lambda \propto \frac{1}{2}$

EDGE

i.e., it depends on the temperature of surface.

56. It lamp is placed at the focus of concave mirror, then we get parallel beam of light



58. Here, E = 1500V/m, B = 0.4 Wb/m² Minimum speed of electron along the

straight line
$$v = \frac{E}{B}$$

$$= \frac{1500}{0.4}$$

59. Shunt resistance

$$S = \frac{I_g G}{I - I_g}$$

$$= \frac{0.1 G}{1 - 0.1}$$

$$= \frac{G}{9}$$

- Diamagnetic materials have negative susceptibility. Thus, (c) is wrongly stated.
- The induction coil works on the principle of mutual induction.

62. We know
$$f = \frac{1}{2\pi\sqrt{LC}}$$

or $\sqrt{LC} = \frac{1}{2\pi f} = \text{time}.$

Thus, \sqrt{LC} has the dimension of time.

63. Work done = area enclosed by F-x graph.



= area of ABNM + area of CDEN - area of EFGH + area of HU = $1 \times 10 + 1 \times 5 - 1 \times 5 + \frac{1}{2} \times 1 \times 10$

64. Both the stones will have the same speed when they hit the ground.

66. The time taken by the particle to come to mean position from the trough = T/2.

Speed = 360 rev/min = $\frac{360}{60}$ rev/s

68. Velocity of sourd $v = \sqrt{\frac{\gamma RT}{M}}$ $\frac{v_H}{M} = \sqrt{\frac{M_O}{M}}$

$$\frac{v_H}{v_O} = \sqrt{\frac{M_O}{M_B}}$$

$$= \sqrt{\frac{16}{1}}$$

$$= 4:1$$

For sonometer n = 1/l

$$\therefore \frac{n_1}{n_2} = \frac{l_2}{l_1} \Rightarrow \frac{256}{n_2} = \frac{16}{25}$$

$$n_2 = \frac{256 \times 25}{16}$$

$$= 400 \text{ Hz}$$

 Wave theory of light was first proposed by Christian Huygens.
 For the liquids, which do not wet the class, the

 For the liquids, which do not wet the glass, the liquid meniscus is convex upward, so angle of contact is obtuse.

72. Radius of path of electron
$$r = \frac{mv}{Bq}$$

m and q remain unchanged. So, $\frac{r_1}{r_2} = \frac{v_1}{v_2} \cdot \frac{B_2}{B_1}$

73. As
$$I \propto a^2$$
 or $a \propto \sqrt{I}$
 $\therefore \frac{a_1}{a_2} = \sqrt{\frac{I}{4I}}$

$$\frac{a_1}{a_2} = \frac{1}{2}$$

$$\frac{I_{max}}{I_{min}} = \left(\frac{a_1 + a_2}{a_1 - a_2}\right)^2$$

$$= \left(\frac{1 + 2}{1 - a_2}\right)^2 = \frac{9}{1}$$

$$I_{\max} = 9I, I_{\min} = I$$

74. In a hydrogen atom the time period is given by

$$\frac{T_1}{T_2} = \left(\frac{n_1}{n_2}\right)^2 \Rightarrow \frac{8}{1} = \left(\frac{n_1}{n_2}\right)^3$$

$$\frac{n_1}{n_2} = \frac{2}{1}$$

 $n_1 = 4$ and $n_2 = 2$ Thus.

- 75. On increasing the forward bias voltage, the harrier energy decreases. This results in the flow of majority charge carriers. Hence, width of depletion region decreases.
- 76. Nuclear forces are charge independent so, $F_1 = F_2 = F_2$

79. Potential
$$V = \frac{Q}{C} \implies V = \frac{Q}{\frac{A \, \varepsilon_0}{d}}$$

Hence, potential depends on the amount of charge, area or geometry and size of the conductor.

78. The potential at each point on the circular path will be equal.

So, work done =
$$q \times \text{potential difference}$$

= $q \times 0$

79. Capacitance with air

$$C = \frac{A\varepsilon_c}{d}$$

Reasoning

- 141. (c) Second is the result of the first
- 142. (b) In all other groups, the first second and third letters are respectively moved one, five and one step forward to obtain second, third and fourth letters respectively.
- 143, Clearly, fig. (d) when placed in the blank space of fig (x) will complete the pattern, as shown below. Hence, the answer is (d).



When interspace between the plates is filled with wax, then

or
$$C' = \frac{KAr_{c_0}}{2d}$$

$$C' = \left(\frac{Ar_{c_0}}{d}\right) \frac{K}{2}$$
or $C' = C \frac{K}{2}$

$$6 = 2 \cdot \frac{K}{2} \implies K = 6$$

80. de-Broglie wavelength

$$\begin{array}{ccc} \lambda = \frac{h}{\sqrt{2mE}} \\ \therefore & \frac{\lambda_1}{\lambda_2} = \sqrt{\frac{E_2}{E_1}} & \Rightarrow & \frac{1 \times 10^{-9}}{0.5 \times 10^{-9}} = \sqrt{\frac{E_2}{E_1}} \\ \Rightarrow & 2 = \sqrt{\frac{E_2}{E_1}} & \Rightarrow & \frac{E_3}{E_1} = 4 \\ \therefore & E_1 = 4E. \end{array}$$

 $E_2 = 4E_1$ $E_2 = 4E_1$ $E_2 = 4E_1 = 4E_1 = 3E_1$

81. Half-life
$$T/2 = \frac{T}{1.44} = \frac{100}{1.44} \text{ s}$$

= $\frac{69.44 \text{ s}}{60} \approx 1.155 \text{ min}$

- 82. Radioactive decay does not depend upon the time of creation
- 84. Coulomb's law is appliable for charged particles, it is not responsible to bind the protons and neutrons in the nucleus of an atom.
- 85. If unpolarised light is incident at polarising angle, then reflected light is completely, i.e. 100% polarised.

145. In fig. X, the right half of the rectangular paper sheet is folded over the left half. In fig. Y. 100 semicircles are punched into the folded paper. When the paper is unfolded, the semicircles in the two halves will join to form circles. Thus two circles will appear in the unfolded position of fig. Y.

Hence, fig. (d) is the correct answer