## AIEEE 2010 Physics Held on (25-04-2010)

## PART A - PHYSICS

Directions: Questions number 1-3 are based on the following paragraph.

An initially parallel cylindrical beam travels in a medium of refractive index  $\mu(I) = \mu_0 + \mu_2 I$ , where  $\mu_0$  and  $\mu_2$  are positive constants and I is the intensity of the light beam. The intensity of the beam is decreasing with increasing radius.

- The initial shape of the wavefront of the beam is
  - (1) planar
  - (2) convex
  - (3) concave
  - (4) convex near the axis and concave near the periphery
- 2. The speed of light in the medium is
  - (1) maximum on the axis of the beam
  - (2) minimum on the axis of the beam
  - (3) the same everywhere in the beam
  - (4) directly proportional to the intensity I
- 3. As the beam enters the medium, it will
  - (1) travel as a cylindrical beam
  - (2) diverge
  - (3) converge

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(4) diverge near the axis and converge near the periphery Directions: Questions number 4-5 are based on the following paragraph.

A nucleus of mass  $M+\Delta m$  is at rest and decays into two daughter nuclei of equal mass  $\frac{M}{2}$  each. Speed of light is c.

- 4. The speed of daughter nuclei is
  - (1)  $c \sqrt{\frac{\Delta m}{M + \Delta m}}$
  - (2)  $c \frac{\Delta m}{M + \Delta m}$
  - (3)  $e^{\sqrt{\frac{2\Delta m}{M}}}$ 
    - (4)  $c \sqrt{\frac{\Delta m}{M}}$
- 5. The binding energy per nucleon for the parent nucleus is  $E_1$  and that for the daughter nuclei is  $E_2$ . Then
  - (1)  $E_1 = 2E_2$
  - (2)  $E_2 = 2E_1$
  - $(3)\quad \mathrm{E}_1 > \mathrm{E}_2$
  - (4)  $E_2 > E_1$

 $\Omega$ 

Directions: Questions number 6-7 contain 8.

Statement-1 and Statement-2. Of the four choices given after the statements, choose the one that best describes the two statements.

6. Statement-1: When ultraviolet light is incident on a photocell, its stopping potential is V<sub>0</sub> and the maximum kinetic energy of the photoelectrons is K<sub>max</sub>. When the ultraviolet light is replaced by X-rays, both V<sub>0</sub> and K<sub>max</sub> increase.

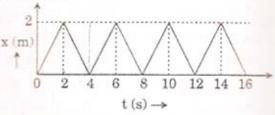
Statement-2: Photoelectrons are emitted with speeds ranging from zero to a maximum value because of the range of frequencies present in the incident light.

- (1) Statement-1 is true, Statement-2 is 9. false.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1.
- (3) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1.
- (4) Statement-1 is false, Statement-2 is true.
- Statement-1: Two particles moving in the same direction do not lose. all their energy in a completely inelastic collision.

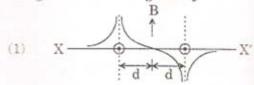
Statement-2: Principle of conservation of momentum holds true for all kinds of collisions.

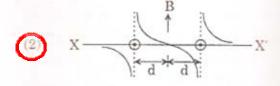
- (N Statement-1 is true, Statement-2 is false.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1.
- (3) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1.
- (4) Statement-1 is false, Statement-2 is true.

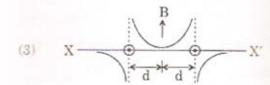
8. The figure shows the position - time (x-1) graph of one-dimensional motion of a body of mass 0.4 kg. The magnitude of each impulse is

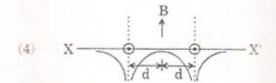


- (1) 0.2 Ns
- (2) 0.4 Ns
- (3) 0.8 Ns (4) 1.6 Ns
- 2. Two long parallel wires are at a distance 2 apart. They carry steady equal currents flowing out of the plane of the paper as shown. The variation of the magnetic field 3 along the line XX' is given by

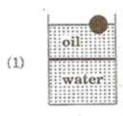


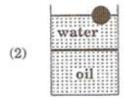


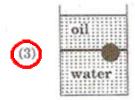


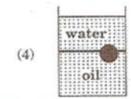


10. A ball is made of a material of density  $\rho$  where  $\rho_{\rm oil} < \rho < \rho_{\rm water}$  with  $\rho_{\rm oil}$  and  $\rho_{\rm water}$  representing the densities of oil and water, respectively. The oil and water are immiscible. If the above ball is in equilibrium in a mixture of this oil and water, which of the following pictures represents its equilibrium position?

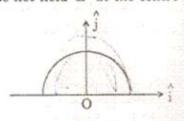


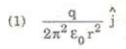






A thin semi-circular ring of radius r has a positive charge q distributed uniformly over
 it. The net field E at the centre O is





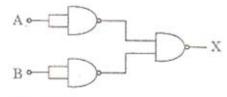
$$(2) \quad \frac{q}{4\pi^2 \varepsilon_0 r^2} \hat{j}$$

$$(3) - \frac{q}{4\pi^2 \epsilon_0 r^2} \hat{j}$$

$$(4) - \frac{q}{2\pi^2 \varepsilon_0 r^2} j$$

- 12. A diatomic ideal gas is used in a Carnot engine as the working substance. If during the adiabatic expansion part of the cycle the volume of the gas increases from V to 32 V, the efficiency of the engine is
  - (1) 0.25
  - (2) 0-5
  - (3) 0·75 (4) 0·99
  - . The respective numb
- The respective number of significant figures for the numbers 23-023, 0-0203 and 2-1 x 10<sup>-3</sup> are
  - (1) 4, 4, 2
  - (2) 5, 1, 2
  - (3) 5, 1, 5
  - (4) 5, 5, 2

The combination of gates shown below 17. yields

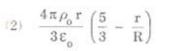


- (1) NAND gate
- (2) OR gate
- (3) NOT gate
- (4) XOR gate
- 15. If a source of power 4 kW produces 10<sup>20</sup> photons/second, the radiation belongs to a part of the spectrum called
  - (1) y-rays
  - (2) X-rays
  - (3) ultraviolet ravs
  - (4) microwaves
- 16. A radioactive nucleus (initial mass number A and atomic number Z) emits 3  $\alpha$ -particles and 2 positrons. The ratio of number of neutrons to that of protons in the final nucleus will be
  - (1)  $\frac{A-Z-4}{Z-2}$
  - (2)  $\frac{A-Z-8}{Z-4}$
  - $(3) \quad \frac{A-Z-4}{Z-8}$
  - (4)  $\frac{A-Z-12}{Z-4}$

17. Let there be a spherically symmetric charge distribution with charge density varying as  $\rho(r) = \rho_0 \left(\frac{5}{4} - \frac{r}{R}\right)$  upto r = R, and  $\rho(r) = 0$  for r > R, where r is the distance from

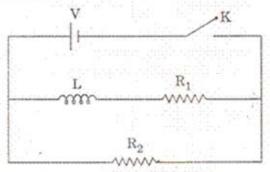
for r > R, where r is the distance from the origin. The electric field at a distance r (r < R) from the origin is given by

 $(1) \quad \frac{\rho_o\,r}{3\epsilon_o}\left(\frac{5}{4}\,-\,\frac{r}{R}\right)$ 



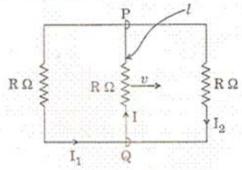
- $\frac{\rho_{\rm o}\, \rm r}{4\,\epsilon_{\rm o}} \left(\frac{5}{3} \frac{\rm r}{\rm R}\right)$
- $(4) \quad \frac{4\,\rho_o\,r}{3\,\epsilon_o}\left(\frac{5}{4}\,-\,\frac{r}{R}\right)$
- 18. In a series LCR circuit R = 200 Ω and the voltage and the frequency of the main supply is 220 V and 50 Hz respectively. On taking out the capacitance from the circuit the current lags behind the voltage by 30°. On taking out the inductor from the circuit the current leads the voltage by 30°. The power dissipated in the LCR circuit is
  - (1) 242 W
    - (2) 305 W
    - (3) 210 W
  - (4) Zero W

19. In the circuit shown below, the key K is closed at t = 0. The current through the battery is



- (1)  $\frac{V(R_1 + R_2)}{R_1 R_2}$  at t = 0 and  $\frac{V}{R_2}$  at  $t = \infty$
- (2)  $\frac{VR_1R_2}{\sqrt{R_1^2+R_2^2}}$  at t=0 and  $\frac{V}{R_2}$  at  $t=\infty$
- (3)  $\frac{V}{R_2}$  at t = 0 and  $\frac{V(R_1 + R_2)}{R_1 R_2}$  at  $t = \infty$
- (4)  $\frac{V}{R_2}$  at t = 0 and  $\frac{VR_1R_2}{\sqrt{R_1^2 + R_2^2}}$  at  $t = \infty$
- 20. A particle is moving with velocity  $\overrightarrow{v} = K(y\hat{i} + x\hat{j})$ , where K is a constant. The general equation for its path is
  - (1)  $y^2 = x^2 + constant$
  - (2)  $y = x^2 + constant$
  - (3)  $y^2 = x + constant$
  - (4) xy = constant

- Let C be the capacitance of a capacitor discharging through a resistor R. Suppose  $t_1$  is the time taken for the energy stored in the capacitor to reduce to half its initial value and  $t_2$  is the time taken for the charge to reduce to one-fourth its initial value. Then the ratio  $t_1/t_2$  will be
- (1) 2
- (2) 1
- (3)  $\frac{1}{2}$
- $\frac{1}{4}$
- A rectangular loop has a sliding connector PQ of length *l* and resistance R Ω and it is moving with a speed *v* as shown. The set-up is placed in a uniform magnetic field going into the plane of the paper. The three currents I<sub>1</sub>, I<sub>2</sub> and I are



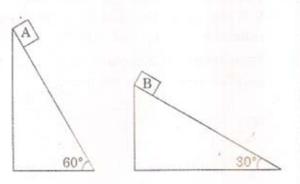
- (1)  $I_1 = I_2 = \frac{Blv}{6R}$ ,  $I = \frac{Blv}{3R}$
- (2)  $I_1 = -I_2 = \frac{Blv}{R}$ ,  $I = \frac{2Blv}{R}$
- (3)  $I_1 = I_2 = \frac{Blv}{3R}$ ,  $I = \frac{2Blv}{3R}$
- (4)  $I_1 = I_2 = I = \frac{B l v}{R}$

23. The equation of a wave on a string of linear mass density 0.04 kg m<sup>-1</sup> is given by

$$y = 0.02(m) \sin \left[ 2\pi \left( \frac{t}{0.04(s)} - \frac{x}{0.50(m)} \right) \right].$$

The tension in the string is

- (1) 6·25 N
- (2) 4·0 N
- (3) 12·5 N
- (4) 0.5 N
- 24. Two fixed frictionless inclined planes making an angle 30° and 60° with the vertical are shown in the figure. Two blocks A and B are placed on the two planes. What is the relative vertical acceleration of A with respect to B?



- (1) 4.9 ms<sup>-2</sup> in vertical direction
- (2) 4.9 ms<sup>-2</sup> in horizontal direction
- (3) 9.8 ms<sup>-2</sup> in vertical direction
- (4) Zero

25. For a particle in uniform circular motion, the acceleration a at a point P (R, θ) on the circle of radius R is (Here θ is measured from the x-axis)

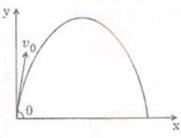
$$(1) \quad \frac{v^2}{R} \stackrel{\wedge}{i} + \frac{v^2}{R} \stackrel{\circ}{j}$$

(2) 
$$-\frac{v^2}{R}\cos\theta \hat{i} + \frac{v^2}{R}\sin\theta \hat{j}$$

(3) 
$$-\frac{v^2}{R} \sin \theta \hat{i} + \frac{v^2}{R} \cos \theta \hat{j}$$

$$(4) - \frac{v^2}{R} \cos \theta \hat{i} - \frac{v^2}{R} \sin \theta \hat{j}$$

26. A small particle of mass m is projected at an angle 0 with the x-axis with an initial velocity  $v_0$  in the x-y plane as shown in the figure. At a time  $t < \frac{v_0 \sin \theta}{g}$ , the angular momentum of the particle is



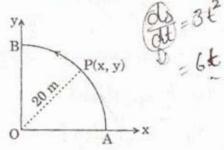
- (1)  $\frac{1}{2} \operatorname{mg} v_0 t^2 \cos \theta$
- (2)  $\text{mg } v_0 t^2 \cos \theta \hat{j}$
- (3) mg  $v_0$  t cos 0  $\hat{k}$
- (4)  $-\frac{1}{2} \operatorname{mg} v_0 t^2 \cos \theta \hat{k}$

where î, ĵ and k are unit vectors along x, y and z-axis respectively.

Two identical charged spheres are suspended by strings of equal lengths. The strings make an angle of 30° with each other. When suspended in a liquid of density 0.8 g cm<sup>-3</sup>, the angle remains the same. If density of the material of the sphere is 1.6 g cm<sup>-3</sup>, the dielectric constant of the liquid is

- (1)
- (2) 4
- (3) 3
- (4) 2

28. A point P moves in counter-clockwise direction on a circular path as shown in the figure. The movement of 'P' is such that it sweeps out a length  $s = t^3 + 5$ , where s is in metres and t is in seconds. The radius of the path is 20 m. The acceleration of 'P' when t = 2 s is nearly



- (1) 14 m/s<sup>2</sup>
- (2) 13 m/s<sup>2</sup>
- (3) 12 m/s<sup>2</sup>
- (4) 7-2 m/s<sup>2</sup>

9. The potential energy function for the force between two atoms in a diatomic molecule is approximately given by  $U(x) = \frac{a}{x^{12}} - \frac{b}{x^6}$ , where a and b are constants and x is the distance between the atoms. If the dissociation energy of the molecule is  $D = [U(x = \infty) - U_{at equilibrium}]$ , D is

- $(1) \quad \frac{b^2}{6a}$
- $(2) \quad \frac{b^2}{2a}$
- $(3) \quad \frac{b^2}{12a}$
- $(4) \frac{b^2}{4a}$

Two conductors have the same resistance at 0 °C but their temperature coefficients of resistance are  $\alpha_1$  and  $\alpha_2$ . The respective temperature coefficients of their series and parallel combinations are nearly

- (1)  $\frac{\alpha_1 + \alpha_2}{2}$ ,  $\frac{\alpha_1 + \alpha_2}{2}$
- $(2) \quad \frac{\alpha_1 + \alpha_2}{2}, \quad \alpha_1 + \alpha_2$
- (3)  $\alpha_1 + \alpha_2, \frac{\alpha_1 + \alpha_2}{2}$
- $(4) \quad \alpha_1 \,+\, \alpha_2, \quad \frac{\alpha_1\,\alpha_2}{\alpha_1 \,+\, \alpha_2}$

# AIEEE 2010 Chemistry - (25-04-2010)

#### PART B — CHEMISTRY

In aqueous solution the ionization constants for carbonic acid are

> $K_1 = 4.2 \times 10^{-7}$  and  $K_2 = 4.8 \times 10^{-11}$ . Select the correct statement for a saturated 0.034 M solution of the carbonic acid.

- The concentration of H<sup>+</sup> is double that
- (2) The concentration of CO<sub>3</sub><sup>2-</sup> is 0.034 M.
- (3) The concentration of CO<sub>3</sub><sup>2-</sup> is greater than that of HCO<sub>3</sub><sup>-</sup>.
- The concentrations of H+ and HCOare approximately equal.
- Solubility product of silver bromide is  $5.0 \times 10^{-13}$ . The quantity of potassium bromide (molar mass taken as 120 g mol-1) to be added to 1 litre of 0.05 M solution of silver nitrate to start the precipitation of AgBr is
  - (1)  $5.0 \times 10^{-8}$  g
  - (2)  $1.2 \times 10^{-10}$  g

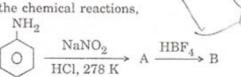


- (3) 1·2 × 10<sup>-9</sup> g
- . (4)  $6.2 \times 10^{-5}$  g
- 33. The correct sequence which shows decreasing order of the ionic radii of the elements is

(1) 
$$O^{2-} > F^- > Na^+ > Mg^{2+} > Al^{3+}$$

- (2)  $Al^{3+} > Mg^{2+} > Na^{+} > F^{-} > O^{2-}$
- (3)  $Na^+ > Mg^{2+} > Al^{3+} > O^{2-} > F^-$
- (4)  $Na^+ > F^- > Mg^{2+} > O^{2-} > Al^{3+}$

34. In the chemical reactions,



the compounds 'A' and 'B' respectively are

- (1) nitrobenzene and chlorobenzene
- (2) nitrobenzene and fluorobenzene
- (3) phenol and benzene
- benzene diazonium chloride fluorobenzene
- 350 If 10-4 dm3 of Water is introduced into a 1.0 dm3 flask at 300 K, how many moles of water are in the vapour phase when equilibrium is established?

(Given: Vapour pressure of H2O at 300 K is 3170 Pa;  $R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$ 

- (1)  $1.27 \times 10^{-3}$  mol
- (2)  $5.56 \times 10^{-3}$  mol
- (3)  $1.53 \times 10^{-2}$  mol
- (4)  $4.46 \times 10^{-2}$  mol
- From amongst the following alcohols the one that would react fastest with conc. HCl and anhydrous ZnCl2, is
  - (1) 1-Butanol
  - (2) 2-Butanol
  - (3) 2-Methylpropan-2-ol
  - (4) 2-Methylpropanol
- 37(3) If sodium sulphate is considered to be completely dissociated into cations and anions in aqueous solution, the change in freezing point of water (\$\Delta T\_f\$), when 0.01 mol of sodium sulphate is dissolved in 1 kg of water, is  $(K_f = 1.86 \text{ K kg mol}^{-1})$ 
  - (1) 0·0186 K
  - 0.0372 K
  - 0.0558 K
  - 0.0744 K
- 1.36 100

- 38. Three reactions involving H<sub>2</sub>PO<sub>4</sub> are given below:
  - (i)  $H_3PO_4 + H_2O \rightarrow H_3O^+ + H_2PO_4^-$
  - (ii)  $H_2PO_4^- + H_2O \rightarrow HPO_4^{2-} + H_3O^+$
  - (iii)  $H_2PO_4^- + OH^- \rightarrow H_3PO_4 + O^{2-}$

In which of the above does  $H_2PO_4^-$  act as an acid?

- (1) (i) only
- (2) (ii) only
  - (3) (i) and (ii)
- (4) (iii) only
- The main product of the following reaction is

 $C_6H_5CH_2CH(OH)CH(CH_3)_2 \xrightarrow{conc. H_2SO_4} ?$ 

(1) 
$$H_5C_6CH_2CH_2 \longrightarrow C = CH_2$$

(2) 
$$H_5C_6$$
  $C = C < H_{CH(CH_3)_2}$ 

$$(3) \qquad \begin{matrix} \mathrm{C_6H_5CH_2} \\ \mathrm{H} \end{matrix} \mathbf{C} = \mathbf{C} \diagdown \begin{matrix} \mathrm{CH_3} \\ \mathrm{CH_3} \end{matrix}$$

(4) 
$$C_6H_5 > C = C < CH(CH_3)_2$$

- The energy required to break one mole of Cl-Cl bonds in Cl<sub>2</sub> is 242 kJ mol<sup>-1</sup>. The longest wavelength of light capable of breaking a single Cl-Cl bond is
  - $(c = 3 \times 10^8 \text{ ms}^{-1} \text{ and } N_A = 6.02 \times 10^{23} \text{ mol}^{-1})$ 
    - (1) 494 nm
    - (2) 594 nm
    - (3) 640 nm
    - (4) 700 nm

29.5 mg of an organic compound containing nitrogen was digested according to Kjeldahl's method and the evolved ammonia was absorbed in 20 mL of 0.1 M HCl solution. The excess of the acid required 15 mL of 0.1 M NaOH solution for complete neutralization. The percentage of nitrogen in the compound is

- (1) 29.5
- (2) 59.0
- (3) 47.4
- (4) 23.7

Ionisation energy of He<sup>+</sup> is  $19.6 \times 10^{-18} \text{ J atom}^{-1}$ . The energy of the first stationary state (n = 1) of Li<sup>2+</sup> is

- (1)  $8.82 \times 10^{-17} \text{ J atom}^{-1}$
- (2)  $4.41 \times 10^{-16} \text{ J atom}^{-1}$
- (3) -4·41 × 10<sup>-17</sup> J atom<sup>-1</sup>
- (4)  $-2.2 \times 10^{-15} \text{ J atom}^{-1}$

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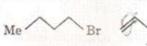
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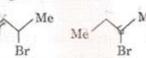
- 43. On mixing, heptane and octane form an ideal solution. At 373 K, the vapour pressures of the two liquid components (heptane and octane) are 105 kPa and 45 kPa respectively. Vapour pressure of the solution obtained by mixing 25.0 g of heptane and 35 g of octane will be (molar mass of heptane = 100 g mol<sup>-1</sup> and of octane = 114 g mol<sup>-1</sup>)
  - (1) 144.5 kPa
  - (2) 72·0 kPa
  - (3) 36·1 kPa
  - (4) 96·2 kPa
- 44. Which one of the following has an optical isomer?
  - (1)  $[Zn(en)_2]^{2+}$
  - (2)  $[Zn(en)(NH_3)_2]^{2+}$
  - (3) [Co(en)<sub>3</sub>]<sup>3+</sup>
  - (4)  $[Co(H_2O)_4(en)]^{3+}$

(en = ethylenediamine)

45. Consider the following bromides:

(3)











The correct order of S<sub>N</sub>1 reactivity is

- (1) A > B > C
- (2) B > C > A
  - (3) B > A > C
  - (4) C > B > A

- 46. One mole of a symmetrical alkene on ozonolysis gives two moles of an aldehyde having a molecular mass of 44 u. The alkene is
  - (1) ethene
  - (2) propene
  - (3) 1-butene
  - (4) 2-butene
- 47. Consider the reaction:

The rate equation for this reaction is rate =  $k [Cl_2] [H_2S]$ 

Which of these mechanisms is/are consistent with this rate equation?

- A.  $Cl_2 + H_2S \rightarrow H^+ + Cl^- + Cl^+ + HS^-$  (slow)  $Cl^+ + HS^- \rightarrow H^+ + Cl^- + S$  (fast)
- B.  $H_2S \Leftrightarrow H^+ + HS^-$  (fast equilibrium)  $Cl_2 + HS^- \rightarrow 2 Cl^- + H^+ + S \text{ (slow)}$
- (1) A only
- (2) B only
- (3) Both A and B

4) Neither A nor B

0.0001

48. The Gibbs energy for the decomposition of 51. Al<sub>2</sub>O<sub>3</sub> at 500 °C is as follows:

$$\frac{2}{3}~\mathrm{Al_2O_3} \rightarrow \frac{4}{3}~\mathrm{Al} + \mathrm{O_2}, \Delta_{\mathrm{r}}\mathrm{G} = +~966~\mathrm{kJ}~\mathrm{mol}^{-1}$$

The potential difference needed for electrolytic reduction of Al<sub>2</sub>O<sub>3</sub> at 500 °C is at least

- (1) 5.0 V
- (2) 4.5 V
- (3) 3·0 V
- (4) 2·5 V
- 49. The correct order of increasing basicity of the given conjugate bases (R = CH<sub>3</sub>) is

(1) 
$$RCO\overline{O} < HC = \overline{C} < \overline{N}H_2 < \overline{R}$$

- (2)  $RCO\overline{O} < HC = \overline{C} < \overline{R} < \overline{N}H_2$
- (3)  $\overline{R} < HC = \overline{C} < RCO\overline{O} < \overline{N}H_2$
- (4)  $RCO\overline{O} < \overline{N}H_2 < HC = \overline{C} < \overline{R}$
- of an ionic substance is 508 pm. If the radius of the cation is 110 pm, the radius of the anion is
  - (1) 144 pm
  - √(2) 288 pm
    - (3) 398 pm
    - (4) 618 pm

- Out of the following, the alkene that exhibits optical isomerism is
  - (1) 2-methyl-2-pentene
  - (2) 3-methyl-2-pentene
  - (3) 4-methyl-1-pentene
  - (4) 3-methyl-1-pentene
- 52. For a particular reversible reaction at temperature T,  $\Delta H$  and  $\Delta S$  were found to be both +ve. If  $T_e$  is the temperature at equilibrium, the reaction would be spontaneous when
  - (1)  $T = T_e$
  - (2)  $T_c > T$
  - (3)  $T > T_e$
  - (4) Te is 5 times T
- 53. Percentages of free space in cubic close packed structure and in body centered packed structure are respectively
  - (1) 48% and 26%
  - (2) 30% and 26%
  - (3) 26% and 32%
  - (4) 32% and 48%

- 54. intermolecular forces e.g. hydrogen bonding,
  - (1)natural rubber
  - (2) teflon
  - (3)nylon 6,6
  - (4) polystyrene
- 55. At 25 °C, the solubility product of Mg(OH), is 1.0 × 10<sup>-11</sup>. At which pH, will Mg<sup>2+</sup> ions start precipitating in the form of Mg(OH), from a solution of 0.001 M Mg2+ ions?
  - (1) 8
  - (2)
  - 10
  - (4) 11
- The correct order of E M2+/M negative sign for the four successive elements Cr, Mn. Fe and Co is
  - Cr > Mn > Fe > Co
    - (2) Mn > Cr > Fe > Co
    - (3) Cr > Fe > Mn > Co
    - (4) Fe > Mn > Cr > Co
- Biuret test is not given by
  - (1) proteins
  - carbohydrates
  - (3) polypeptides
  - (4) urea

- polymer containing strong 58. The time for half life period of a certain reaction A ----- Products is 1 hour. When the initial concentration of the reactant 'A', is 2.0 mol L-1, how much time does it take for its concentration to come from 0:50 to \$25 mol L-1 if it is a zero order reaction?

  - 4 h
  - 0.5 h
  - 0.25 h
  - A solution containing 2.675 g of  $CoCl_3$ . 6 NH<sub>3</sub> (molar mass = 267.5 g mol<sup>-1</sup>) is passed through a cation exchanger. The chloride ions obtained in solution were treated with excess of AgNO3 to give 4.78 g of AgCl (molar mass = 143.5 g mol-1). The formula of the complex is (At. mass of Ag = 108 u)
    - (1) [CoCl(NH<sub>3</sub>)<sub>5</sub>] Cl<sub>2</sub>
    - [Co(NH3)6] Cl3
    - (3) [CoCl<sub>2</sub>(NH<sub>2</sub>)<sub>4</sub>] CI
    - (4) [CoCl<sub>3</sub>(NH<sub>2</sub>)<sub>3</sub>]
  - The standard enthalpy of formation of NH3 is -46.0 kJ mol-1. If the enthalpy of formation of H2 from its atoms is -436 kJ mol<sup>-1</sup> and that of N<sub>2</sub> is - 712 kJ mol-1, the average bond enthalpy of N-H bond in NH3 is
    - 1102 kJ mol-1
    - 964 kJ mol<sup>-1</sup>
    - + 352 kJ mol-1
    - (4) + 1056 kJ mol-14

### AIEEE 2010 Mathematics Paper Held On (25-04-2010)

#### PART C - MATHEMATICS

- 61. Consider the following relations:

  - $S = \{(\frac{m}{n}, \frac{p}{q}) \mid m, n, p \text{ and } q \text{ are integers} \}$ such that  $n, q \neq 0$  and  $qm = pn\}$ .

Then

- (1) R is an equivalence relation but S is not an equivalence relation
- (2) neither R nor S is an equivalence relation
- (3) S is an equivalence relation but R is not an equivalence relation
- (4) R and S both are equivalence relations
- 62. The number of complex numbers z such that |z-1| = |z+1| = |z-i| equals
  - (1) 0
  - (2)
    - (3) 2
    - (4) 00
- 63. If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 x + 1 = 0$ , then  $\alpha^{2009} + \beta^{2009} =$ 
  - (1) -2
  - (2) -1
  - (3)
    - (4) 2

64. Consider the system of linear equations:

$$x_1 + 2x_2 + x_3 = 3$$

$$2x_1 + 3x_2 + x_3 = 3$$

$$3x_1 + 5x_2 + 2x_3 = 1$$

The system has

- (1) infinite number of solutions
- (2) exactly 3 solutions
- (3) a unique solution
- (4) no solution
- 65. There are two urns. Urn A has 3 distinct red balls and urn B has 9 distinct blue balls. From each urn two balls are taken out at random and then transferred to the other. The number of ways in which this can be done is
  - (1) 3
  - (2) 36
  - (3) 66
  - (4) 108
- 66. Let  $f: (-1, 1) \rightarrow \mathbb{R}$  be a differentiable function with f(0) = -1 and f'(0) = 1. Let  $g(x) = [f(2f(x) + 2)]^2$ . Then g'(0) =
  - (1) 4
    - (20) -4
    - (3) 0
    - (4) -2

67 Let  $f: \mathbb{R} \to \mathbb{R}$  be a positive increasing 70. function with  $\lim_{x\to\infty} \frac{f(3x)}{f(x)} = 1$ .

Then  $\lim_{x \to \infty} \frac{f(2x)}{f(x)}$ 

- (1) 1
- (2)  $\frac{2}{3}$
- (3) 3 2
- (4) 3

68. Let p(x) be a function defined on R such that p'(x) = p'(1-x), for all  $x \in [0, 1]$ , p(0) = 1 and p(1) = 41. Then  $\int_{0}^{1} p(x) dx$  equals

- (1)  $\sqrt{41}$
- (2) 21
- (3) 41 (4) 42
- 69. A person is to count 4500 currency notes. Let  $a_n$  denote the number of notes he counts in the  $n^{th}$  minute. If  $a_1 = a_2 = ... = a_{10} = 150$  and  $a_{10}$ ,  $a_{11}$ , ... are in an AP with common difference -2, then the time taken by him to count all notes is
  - (1) 24 minutes
  - (2) 34 minutes
    - (3) 125 minutes
    - (4) 135 minutes

- 70. The equation of the tangent to the curve  $y = x + \frac{4}{x^2}$ , that is parallel to the x-axis, is
  - (1) y = 0
  - (2) y = 1
  - (3) y = 2
  - (4) y = 3
- 71. The area bounded by the curves  $y = \cos x$  and  $y = \sin x$  between the ordinates x = 0 and  $x = \frac{3\pi}{2}$  is
  - (1)  $4\sqrt{2} 2$ 
    - (2)  $4\sqrt{2} + 2$
    - (3) 4/20-1
    - (d) 4 /2 + 1
- 72. Solution of the differential equation  $\cos x \, dy = y (\sin x y) \, dx, \ 0 < x < \frac{\pi}{2} \quad is$ 
  - (1)  $\sec x = (\tan x + e) y$ 
    - (2)  $y \sec x = \tan x + c$
    - (3)  $y \tan x = \sec x + c$
    - (4)  $\tan x = (\sec x + c) y$

- 73. Let  $\vec{a} = \hat{j} \hat{k}$  and  $\vec{c} = \hat{i} \hat{j} \hat{k}$ . Then the vector  $\vec{b}$  satisfying  $\vec{a} \times \vec{b} + \vec{c} = \vec{0}$  76. The line L given by  $\frac{x}{5} + \frac{y}{b} = 1$  passes through the point (13, 32). The line K is and  $\overrightarrow{a}$ ,  $\overrightarrow{b} = 3$  is
  - (1)  $-\hat{i} + \hat{j} 2\hat{k}$ 
    - (2)  $2\hat{i} \hat{j} + 2\hat{k}$
    - (3)  $\hat{i} \hat{j} 2\hat{k}$
    - (4)  $\hat{i} + \hat{j} 2\hat{k}$
- 74. If the vectors  $\vec{a} = \hat{i} \hat{j} + 2\hat{k}$ ,  $\stackrel{\rightarrow}{b}=2\,\hat{i}+4\,\hat{j}+\hat{k}$  and  $\stackrel{\rightarrow}{c}=\lambda\,\hat{i}+\hat{j}+\mu\,\hat{k}$  are mutually orthogonal, then  $(\lambda,\,\mu)=$ 
  - (1) (-3, 2)
    - (2) (2, -3)
    - (3) (-2,3)
    - (4) (3, -2)
- 75. If two tangents drawn from a point P to the parabola  $y^2 = 4x$  are at right angles, then the locus of P is
  - (1) x = 1
  - (2) 2x + 1 = 0
  - - (4) 2x 1 = 0

- through the point (13, 32). The line K is parallel to L and has the equation  $\frac{x}{c} + \frac{y}{3} = 1$ . Then the distance between L and K is



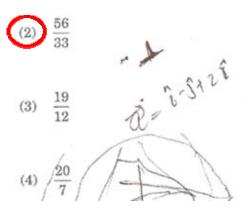
- A line AB in three-dimensional space makes angles 45° and 120° with the positive x-axis and the positive y-axis respectively. If AB makes an acute angle 0 with the positive z-axis, then  $\theta$  equals
  - (1) 30°

  - (4)

- 78. Let S be a non-empty subset of R. Consider 80. the following statement:
  - P: There is a rational number  $x \in S$  such that x > 0.

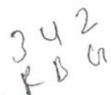
Which of the following statements is the negation of the statement P?

- There is a rational number x ∈ S such that x ≤ 0.
  - (2) There is no rational number x ∈ S such that x ≤ 0.
  - (3) Every rational number x ∈ S satisfies x ≤ 0.
  - (4)  $x \in S$  and  $x \le 0 \Rightarrow x$  is not rational.
- 79. Let  $\cos{(\alpha + \beta)} = \frac{4}{5}$  and let  $\sin{(\alpha \beta)} = \frac{5}{13}$ , where  $0 \le \alpha$ ,  $\beta \le \frac{\pi}{4}$ . Then  $\tan{2\alpha} =$ 
  - (1)  $\frac{25}{16}$  Cos 60



- 80. The circle  $x^2 + y^2 = 4x + 8y + 5$  intersects the line 3x 4y = m at two distinct points if
  - (1) −85 < m < −35
  - (2) -35 < m < 15
  - (3) 15 < m < 65
  - (4) 35 < m < 85
- 81. For two data sets, each of size 5, the variances are given to be 4 and 5 and the corresponding means are given to be 2 and 4, respectively. The variance of the combined data set is
  - (1)  $\frac{5}{2}$
  - (2)  $\frac{11}{2}$ 
    - (3) 6
    - (4)  $\frac{13}{2}$
- 82. An urn contains nine balls of which three are red, four are blue and two are green. Three balls are drawn at random without replacement from the urn. The probability that the three balls have different colours is
  - (1)  $\frac{1}{3}$
  - (2)  $\frac{2}{7}$ 
    - (3)  $\frac{1}{21}$
    - (4)  $\frac{2}{23}$





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- 83. For a regular polygon, let r and R be the Directions: Questions number 86 to 90 are radii of the inscribed and the circumscribed circles. A false statement among the following is
  - (1) There is a regular polygon with

$$\frac{r}{R} = \frac{1}{2}$$

(2) There is a regular polygon with

$$\frac{r}{R} = \frac{1}{\sqrt{2}}$$

(3) There is a regular polygon with

$$\frac{r}{R} = \frac{2}{3}$$

(4) There is a regular polygon with

$$\frac{\mathbf{r}}{\mathbf{R}} = \frac{\sqrt{3}}{2}$$

- 84 The number of 3 × 3 non-singular matrices, with four entries as 1 and all other entries as 0, is
  - (1) less than 4
  - (2) 5
  - (3) 6
  - (4) at least 7
- 85. Let  $f: \mathbb{R} \to \mathbb{R}$  be defined by

$$f(x) = \begin{cases} k-2x, & \text{if } x \leq -1 \\ \\ 2x+3, & \text{if } x > -1 \end{cases}.$$

If f has a local minimum at x = -1, then a possible value of k is

- (1) 1

Assertion - Reason type questions. Each of these questions contains two statements.

Statement-1: (Assertion) and

Statement-2: (Reason).

Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select the correct choice.

- Four numbers are chosen at random (without replacement) from the set {1, 2, 3, ..., 20}.
  - Statement-1: The probability that the chosen numbers arranged in some order will form an AP is  $\frac{1}{85}$ .
  - Statement-2: If the four chosen numbers form an AP, then the set of all possible values common difference is  $\{\pm 1, \pm 2, \pm 3, \pm 4, \pm 5\}.$
  - (1) Statement-1 is true, Statement-2 is true; Statement-2 is a explanation for Statement-1.
  - (2) Statement-1 js true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1.
  - (3) Statement-1 is true, Statement-2 is false.
  - Statement-1 is false, Statement-2 is true.

87. Let 
$$S_1 = \sum_{j=1}^{10} j(j-1)^{10}C_j$$
,  $S_2 = \sum_{j=1}^{10} j^{10}C_j$  and  $S_3 = \sum_{j=1}^{10} j^{2}^{10}C_j$ .

Statement-1:  $S_3 = 55 \times 2^9$ .

Statement-2:  $S_1 = 90 \times 2^8$  and  $S_2 = 10 \times 2^8$ .

- Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1.
- (3) Statement-1 is true, Statement-2 is false.
- (4) Statement-1 is false, Statement-2 is true.
- 88. Statement-1: The point A(3, 1, 6) is the mirror image of the point B(1, 3, 4) in the plane x-y+z=5.

Statement-2: The plane x - y + z = 5bisects the line segment joining A(3, 1, 6) and B(1, 3, 4).

- Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1.
  - (3) Statement-1 is true, Statement-2 is false.
  - (4) Statement-1 is false, Statement-2 is true.

89. Let f: R → R be a continuous function defined by

$$f(x) = \frac{1}{e^x + 2e^{-x}}$$
.

Statement-1:  $f(c) = \frac{1}{3}$ , for some  $c \in \mathbb{R}$ .

Statement-2:  $0 < f(x) \le \frac{1}{2\sqrt{2}}$ , for all  $x \in \mathbb{R}$ .

- Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is **not** a correct explanation for Statement-1.
  - (3) Statement-1 is true, Statement-2 is false.
- (4) Statement-1 is false, Statement-2 is true.
- 90. Let A be a 2 × 2 matrix with non-zero entries and let A<sup>2</sup> = I, where I is 2 × 2 identity matrix. Define Tr(A) = sum of diagonal elements of A and | A | = determinant of matrix A.

Statement-1: Tr(A) = 0.

Statement-2: |A| = 1.

- Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1.
- (3) Statement-1 is true, Statement-2 is false.
- (4) Statement-1 is false, Statement-2 is true.