

**Sample Paper**  
**Class – X**  
**Subject – Mathematics**

Section – A

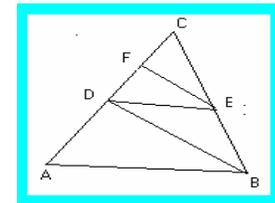
(Answer all the questions from this Section)

1.a) A certain sum gives Rs 1000 as SI and 1050 as CI for 2 years time . If the rate is same , find the sum (3)

b) What are the solutions to  $|x| \geq 2$  ? .  
 Graph on a number line. (3)

c)  $n = \frac{\sqrt{x^2+xy} + \sqrt{x^2-xy}}{\sqrt{x^2+xy} - \sqrt{x^2-xy}}$ , show that  $n^2 y - 2nx + y = 0$  (4)

2 a)  $DE \parallel AB$  and  $FE \parallel DB$  Prove that  $DC^2 = CF.AC$  (3)



b). Four horses are tethered at 4 corners of a square field of side 70 metres so that they just cannot reach one another. What is the area left ungrazed by the horses 4

c) Mr. Khan invests Rs. 45000 in a cement company paying a dividend of 9% per annum, when Rs. 100 share sells at Rs. 150. What is his annual

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Income? He sells 50% of his shares when the price rises to Rs. 200. What is his gain ?

3 a) A hemispherical bowl of internal diameter 36 cm is full of some liquid. This liquid is to be filled in cylindrical bottles of radius 3 cm and height 6 cm. Find the number of bottles needed to empty the bowl (3)

b) Bibhu Prasad buys goods worth Rs. 5000. He gets a rebate of 5% on it. A sales tax at the rate of 5% is levied on the discounted price. Find the amount he will have to pay for the goods.: (3)

c) A sum of Rs.4,920 was borrowed at 5% p.a. compound interest. The loan was paid back in 2 equal instalments in two years. Find the value of each instalment. (4)

4 a) If the point C (-1, 2) divides the line segment AB in the ratio 3 : 4, where coordinates of A are (2, 5), find the coordinates of B. (3)

b) Given that  $2x^3 - x^2 - 2x + 3 = (Ax + B)(x - 1)(x + 2) + C(x - 1) + D$ , find the values of A, B, C and D. Hence or otherwise, deduce the remainder when  $2x^3 - x^2 - 2x + 3$  is divided by  $x^2 + x - 2$  (4)

c) Plot P(3,2) and Q(-3,-2). Draw perpendicular PM and QN on X axis  
1. Find image of P at the origin.

2. Name PMQN find its area

3. When M is mapped on reflection to X-axis, Y-axis and origin, find coordinates Use graph paper for this question. Take 1 cm = 1 unit on both the axes. (3)

### Section – B

(Answer any FOUR questions from this Section)

5 a) The numerator of a fraction is one less than its denominator. If three is added to each of the numerator and denominator, the fraction is increased by  $\frac{3}{28}$ . Find the fraction?  
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6 Are all circles similar ? (3)

b) Mrs. Kaul invests Rs. 56000 in a textile company paying 5% per annum when its Rs. 100 share can be bought for Rs. 140. Find her annual dividend and her percentage income on investment.

10 (c) A rocket at Sriharikota launching pad having the shape of a cylinder surmounted by a cone .has the following measurements The cylinder is of radius 3 m and height 20 m and the cone has the slant height 5 m. Calculate the surface area and volume of the rocket. (4)

11 a) Priya Goswami has a savings bank account in a bank. Her pass book has the following entries:

Year	Date	Particulars	Debit	Credit	Balance
2000	Feb 10	By cash	--	1000-00	1000-00
	Feb 26	By cheque	--	2000-0	3000-00
	March	By salary	--	5000-00	8000-00
	March 10	By cheque	2000-00	-	6000-00
	March 29	By cash	500-0	-	5500-00
	April 3	By salary	--	5000-00	10500-00

If she closes her account on 15th April and the rate of interest is 5% per annum, find the amount received by her. (5)

b)  $8a-5b$        $8a+5b$   
 If  $\frac{8a-5b}{8c-5d} = \frac{8a+5b}{8c+5d}$  prove that  $a/b=c/d$

b) The mean of the following frequency distribution is 62.8. Find the missing x. (3)

0-20	5
20-40	8
40-60	x
60-80	12
80-100	7
100-120	8

c) A pole 5 m high is fixed on the top of a tower. The angle of elevation of the top of the pole observed from a point A on the ground is  $60^\circ$  and the angle of depression of point A from the top of the tower is  $45^\circ$ . Find the height of the tower. (Take  $\sqrt{3}=1.732$ ) (4)

6 a) Solve  $(x-5)^2 + 2(x-5) - 35 = 0$

b) Give an example of reflection on the line  $y=x$   
 Give an example of reflection on the X axis  
 Give an example of reflection on the Y axis (3)

c) Water flows out through a circular pipe whose internal radius is 1 cm, at the rate of 80 cm/second into an empty cylindrical tank, the radius of whose base is 40 cm. By how much will the level of water rise in the tank in half an hour ? (4)

7 a) Draw a histogram with the following data of salaries[ in thousands] of employees of a Foreign Bank branch in Mumbai

Salary in thousands	no of employees
0-10	50
11-21	300

22-32	250
33-43	400
44-54	550
55-65	440
66-76	260
77-87	350

88 above	100
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b) Using the ruler and compasses only: Using a ruler construct a triangle with  $BC=6.4$  cm,  $CA=5.8$  and  $\angle ABC=60^\circ$ . Draw its incircle. Record the radius

(5)

8 a) If the equation  $(1 + m^2)x^2 + 2mcx + c^2 - a^2 = 0$  has equal roots, prove that  $c^2 = a^2(1 + m^2)$ .

(5)

8 b) find the value of  $x, y$  if

$$\begin{bmatrix} 1 & 2 \\ 3 & 3 \end{bmatrix} \begin{bmatrix} x & 0 \\ 0 & y \end{bmatrix} = \begin{bmatrix} x & 0 \\ 0 & 1 \end{bmatrix}$$

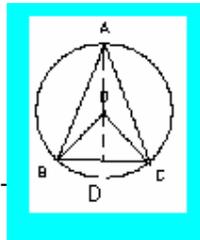
c) Prove that

$$\frac{\sin A}{1 + \cos A} + \frac{1 + \cos A}{\sin A} = 2 \operatorname{cosec} A$$

(3)

9a)  $BC$  is a chord of a circle with centre  $O$ .  $A$  is a point on arc  $BAC$  as shown. Prove that  $\angle BAC + \angle OBC = 90^\circ$ .

(3)

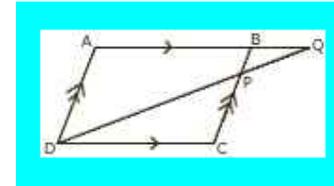


9 b) In the below figure, alongside  $ABCD$  is a parallelogram,  $P$  is a point on  $BC$  such that  $BP : PC = 1 : 2$ .  $DP$  produced meets  $AB$  produced at  $Q$ . Given area of triangle  $BPQ = 20 \text{ cm}^2$ , calculate:

(i) Area of triangle  $CDP$ ;

(ii) Area of parallelogram  $ABCD$

(4)



c) What will Rs.1500 amount to in three years if it is invested in 20% p.a. compound interest, interest being compounded annually? (3)

10a) Answer yes / no

- Are any two equilateral triangles similar?
- If two isosceles triangles have congruent vertex angles, are the triangles similar?
- If two isosceles triangles have congruent base angles, are the triangles similar?
- Is it possible for two quadrilaterals to have congruent angles and not be similar?
- Are all squares similar to one another?