12/31/11 **ALCCS** 

## **ALCCS**

Code: CS42 Subject: OPERATIONS RESEARCH AND SYSTEM SIMULATION Time: 3 Hours Max. Marks: 100

**MARCH 2010** 

**NOTE:** 

- Question 1 is compulsory and carries 28 marks. Answer any FOUR questions from the rest. Marks are indicated against each question.
- Parts of a question should be answered at the same place.
- All calculations should be up to three places of decimals.
- **Q.1** a. Discuss how revised simplex method can be used to improve computational efficiency of solving a linear programming problem.
  - b. Discuss the economic interpretation of the dual problem.
  - c. Differentiate between unbounded solution and infeasible solution in the context of solution to linear programming problem.
  - d. Explain what is an unbalanced transportation problem.
  - e. Discuss four applications of integer programming.
  - Discuss degeneracy in linear programming problem?
  - g. Discuss the role of Operations Research in decision making.

 $(7 \times 4)$ 

- a. What is the standard form of linear programming problem and how do you obtain it? Also discuss special cases that **Q.2** arise in application of simplex method. (9)
  - b. Use penalty method to solve the following linear programming problem:

Maximize z=

 $2x_1+x_2+x_3$ 

Subject to 
$$4x_1+6x_2+3x_3 \le 8$$
,  $3x_1-6x_2-4x_3 \le 1$ ,  $2x_1+3x_2-5x_3 \ge 4$ 

and  $x_1, x_2, x_3 \le 0$ .

(9)

- a. What are various algorithms for finding initial basic solution for a transportation problem? Discuss Q.3them. (9)
  - b. Determine the basic feasible solution, if exists, to the following transportation Approximation method.

problem using Vogel's

|               | Distribution Centres |    |   |    |   |    |        |  |
|---------------|----------------------|----|---|----|---|----|--------|--|
| Sources       | D1                   | D2 |   | D3 |   | D4 | Supply |  |
| S1            | 2                    | 3  |   | 11 |   | 7  | 6      |  |
| S2            | 1                    | 0  |   | 6  |   | 1  | 1      |  |
| S3            | 5                    | 8  |   | 15 |   | 9  | 10     |  |
| Requirement 7 |                      | 5  | 3 |    | 2 |    |        |  |
|               |                      |    |   |    |   |    | (9)    |  |

a. What are various algorithms for solving an Integer Linear programming problem? Discuss branch and bound method in **Q.4** detail. (9)

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b. Using the cutting plane method, solve the following Integer Linear Programming Problem

Maximize 
$$z = 7x_1 + 10x_2$$
  
Subject to  $-x_1 + 3x_2 \le 6$ ,  $7x_1 + x_2 \le 35$ ,  $x_1$ ,  $x_2$  are non-negative integers. (9)

Q.5 a. Discuss in detail the various parameters for designing and evaluating a simulation based experiments.(9)

b. A student has to take examination in three courses x, y, z. He has three days available for study. He feels that it would be best to devote a whole day to study the same course so that he may study a course for one day, two days or three days or not at all. His estimates of grades he may get by studying are as follows.

| Study days/courses | X | У | Z |
|--------------------|---|---|---|
| 0                  | 1 | 2 | 1 |
| 1                  | 2 | 2 | 2 |
| 2                  | 2 | 4 | 4 |
| 3                  | 4 | 5 | 4 |

How should the student plan to study so that the grades obtained are maximized?

(9)

Q.6 a. Discuss Hungarian Assignment algorithm in detail. (9)

b. A department has five employees with five jobs to be performed. The time (in hrs) each man will take to perform each job is given by the following cost matrix:

|      |   |    | Employees |     |    |    |  |  |
|------|---|----|-----------|-----|----|----|--|--|
|      |   | I  | $\Pi$     | III | IV | V  |  |  |
| Jobs | A | 10 | 5         | 13  | 15 | 16 |  |  |
|      | В | 3  | 9         | 18  | 13 | 6  |  |  |
|      | C | 10 | 7         | 2   | 2  | 2  |  |  |
|      | D | 7  | 11        | 9   | 7  | 12 |  |  |
|      | Е | 7  | 9         | 10  | 4  | 12 |  |  |

How should jobs be allocated one per employee so that total the man-hours can be maximized?

(9)

- Q.7 Write a short note on any **THREE** of the following:
  - (i) GPSS.
  - (ii) Degeneracy in Transportation Problem.
  - (iii) Sensitivity and Parametric Analysis.
  - (iv) Monte Carlo Method.

(6+6+6)