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SATHYABAMA UNIVERSITY

(Established under section 3 of UGC Act, 1956)

Course & Branch: M.E - W-AEL

Title of the Paper: Transforms and Probabilities

Sub. Code:735101 (2008-09)

Date:02/12/2011

Max. Marks:80

Time: 3 Hours

Session:FN

PART - A

 $(6 \times 5 = 30)$

Answer ALL the Questions

- 1. State and prove any two properties of discrete Fourier transform.
- 2. Write the test statistic in testing whether the sample mean deviates significantly from the population mean, using T distribution.
- 3. Define stochastic process and state its classification.
- 4. At a checkout counter customers arrive at an average of 1.5/min. Find the probabilities that
 - (a) at most 4 will arrive in any given minute
 - (b) At least 3 will arrive during an interval of 2 minutes
- 5. State the types of Queuing models with example.
- 6. Bring out the salient features of Binomial, Poisson and exponential distributions with classic examples.

PART - B

 $(5 \times 10 = 50)$

Answer ALL the Questions

7. Write down the algorithm for Decomposition-in-time Fast Fourier Transform.

(or)

8. Give on application of the Z-transform to linear time invariant (*LTI*) systems.

9. State and prove any two properties of the continuous wavelet transform.

(or)

- 10. Find the scaling and wavelet coefficients of the function $y = x^2$, 0 < x < 1 by taking the starting scale as $j_0 = 1$.
- 11. Given a 2^J x 2^J image does a J+1 level pyramid reduce or expand the amount of data require to represent the image? What is the compression or expansion ratio?

(or)

- 12. Using the Haar Wavelet, determine the minimum entropy packet decomposition for the function f(n) = 0.25 for $n = 0,1,2 \dots 15$. Employ the non-normalized Shannon entropy $E[f(n) = \sum f^2(n) \ I_n \ [f^2(n)]$ As the minimization criterion. Draw the optimal tree, labling the
- 13. State and prove the properties of auto-correlation function. (or)

nodes with the computed entropy values.

- 14. Find the auto-correlation function corresponding to the power density spectrum $S_{xx}(w) = \frac{8}{(9+w^2)^2}$. Also find its mean and variance.
- 15. Write detailed notes on (a) Ergodicity, Mean Ergodic processes (b) Variance and Co- vaiance

 Draw sketches and graphs where necessary (or)
- 16. State Wiener Khvichin relations. For a random process, $X(t) = A \cos(W+\theta)$ where A is real constant, W is a random variable with density f(w) and θ is a random variable uniformly distributed over the interval $(-\pi,\pi)$ and independent of w, calculate the power spectral density.