# T.E. (Biotechnology) (Semester - I) Examination, 2010 COMPUTATIONAL TECHNIQUES AND BIOSTATISTICS (2008 Course) 

Time : 3 Hours
Max. Marks : 100

## Instructions: 1) Answer any three questions from Section Land any three from Section II.

2) Figures to the right indicate full marks?
3) Make suitable assumptions wherever necessary.
SECTION - I
1. a) Determine the constants "a" and "b" by the Ceast squares method such that $y=a e^{b x} f i t s t h e ~ f o l l o w i n g ~ d a t a . ~$

| $\mathbf{x}$ | 1 | 1.2 | 1.4 | 1.6 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | 40.170 | 73.196 | 133.372 | 243.02 |

b) Find the values of " $a$ ", "b" and "c" sothat $Y=a+b x+c x^{2}$ is the best fit to the data.

| $\mathbf{x}$ | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | 1 | 0 | 3 | 10 | 27 |
|  |  |  |  |  |  |
|  | OR |  |  |  |  |

2. a) The following are the results of an experiment on friction of bearings, the speed being constant Corresponding values of coefficient of friction and temperature are shown in the table. If $\mu$ and $t$ are given by the law find the values of " a " and" b ".

| t | 120 | 110 | 100 | 90 | 80 | 70 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mu$ | 0.0051 | 0.0059 | 0.0071 | 0.0085 | 0.00102 | 0.00124 |

b) Fit a least square geometric curve of the form $y=a x^{b}$ to the data.

| $\mathbf{x}$ | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | 0.5 | 2 | 4.5 | 8 | 12.5 |

3. a) Applying Lagrange's formula and find a polynomial which approximates the, following data.

| $\mathbf{x}$ | -2 | -1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{f}(\mathbf{x})$ | -12 | -8 | 3 | 5 |

b) $\Delta^{2}\left(\mathrm{x}^{3}\right)$. Evaluate It.

> OR
4. a) Given the set of tabulated points $(1,-3),(3,9),(4,30)$ and $(6,132)$. Obtain the value of y when x is 2 using Newton's divided difference formulae.
b) The population of a town in decennial censuswwas as under. Estimate the population for the year 1955 using Newton's interpolation formulae.

| Year | 1921 | 1931 | 1941 | 1951 | 1961 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Population <br> (in thousands) | 46 | 66 | 81 | 93 | 101 |

5. a) The velocities of a car running on a straightrod at intervals of two minutes are given below.

| Time (min.) | 0 | 2 |
| :--- | :--- | :--- |
| Velocity $(\mathbf{k m} / \mathbf{h r})$ | 0 | 22 | | 6 | 8 | 10 | 12 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 27 | 18 | 7 | 0 |

Apply Simpson's $1 / 3^{\text {rd }}$ rule to find the total distance covered by the car. Compare with the actual value
b) Determine the maximum error in evaluating the integral $\int \operatorname{cosxdx}$ from 0 to $\pi / 2$ by trapezoidal rule using four sub intervals.

OR
6. a) A curve is drawn to pass through the points given by the following table. Using Weddle's rufle, estimate the area bounded by the curve, the $x$-axis and the lines $x=1$ and $x=4$.

| $\mathbf{x}$ | 1 | 1.5 | 2 | 2.5 | 3 | 3.5 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ | 2 | 2.4 | 2.7 | 2.8 | 3 | 2.6 | 2.1 |

b) A reservoir discharging water through sluices at a depth "h" below the water surface has a surface area "A" for various values of "h" as given below. If " t " denotes the time in minutes, the rate of fall of the surface is given by $\mathrm{dh} / \mathrm{dt}=-(48 \mathrm{~h} / \mathrm{A})$. Estimate the time taken for the water level to fall from 14 to 10 ft above the sluices.

| h (ft) | 10 | 11 | 12 | 13 | 14 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| A (sq.ft) | 950 | 1070 | 1200 | 1350 | 1530 |

## SECTION - II

7. a) Find the least positive root of the equation $\tan x=x$ to an accuracy of 0,001 by Newton-Raphson method.
b) Find the root of the equation $2 x=\cos x+3$ correct to three decimal places by Bisection method.
OR
8. a) Use the method of Regular falsi to estimate the positive soot of the equation $\mathrm{xe}^{\mathrm{x}}=1$ between 0 and 1 .
b) Find the real root of the non linear equations $x^{2}-y^{2}=3$ and $x^{2}+y^{2}=13$ by Newton-Raphson method.

b) Discuss in short about types of bar diagrams.

OR
10. a) Discuss in detail the methods of Sampling.
b) Discuss in detail on Pictographs and Cartograms with suitable examples.
11. a) A controlled experiment was conducted to test the effectiveness of a new drug. Under this experiment 300 patients were treated with new drug and 200 were not treated with drug. The results of the experiment are as follows. Use Chi square test and comment on the effectiveness of the drug. For degrees of freedom $=2$, the table value at $5 \%$ significance level is 5.49.

| Details | Cured | Condition worsened | No effect |
| :--- | :--- | :--- | :--- |
| Treated with drug | 200 | 40 | 60 |
| Not treated with drug | 120 | 30 | 50 |

b) The following table gives the yearly medical expenditure of 80 hostilities of a college. Calculate arithmetic mean, standard deviation and coefficient of
variation of the above data.

| Expenditure <br> (Rs.) | $78-82$ | $73-77$ | $68-72$ | $63-67$ | $58-62$ | $53-57$ | $48-52$ | $43-47$ | $38-42$ | $33-37$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No of <br> students | 2 | 6 | 7 | 12 | 18 | 13 | 9 | 7 | 4 | 2 |

## OR

12. a) Calculate the median for the following data.

| Weight <br> (gms) | $410-419$ | $420-429$ | $430-439$ | $440-449$ | $450-459$ | $460-469$ | $470-479$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No.of <br> apples | 14 | 20 | 42 | 54 | 45 | 18 | 7 |

b) Two laboratories " A " and " B " carry out independent estimates of fat content in ice cream made by a firm. Asample is taken from each batch, halved and the separated halves sent to two laboratories. The fat content obtained by the laboratories are recorded below. Is there a significant difference between the mean fat content obtained by the two laboratories "A" and "B"? The following " $t$ " extracts are given below.
$\left.\begin{array}{lrrrrrrrrrr}\text { Degrees of freedom } & 6 & 7 & 8 & 9 & 10 & 16 & 18 & 20 & \\ \text { 5\% value of } \mathrm{t} & & 1.45 & 2.36 & 2.31 & 2.26 & 2.23 & 2.12 & 2.10 & 2.09 & \\ \text { Batch No. } & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \text { LabA } & 7 & 8 & 7 & 3 & 8 & 6 & 9 & 4 & 7 & 8 \\ \text { Lab B } & & 7 & 8 & 8 & 4 & 7 & 7 & 9 & 6 & 6\end{array}\right)$

