

2011 CA

Test Paper Code: CA

Time: 3 Hours

Max. Marks: 300

**INSTRUCTIONS****A. General:**

1. This Booklet is your Question Paper. It contains **20** pages and has 100 questions.
2. The Question Booklet **Code** is printed on the right-hand top corner of this page.
3. The Question Booklet contains blank spaces for your rough work. No additional sheets will be provided for rough work.
4. **Clip board, log tables, slide rule, calculator, cellular phone or any other electronic gadget in any form are NOT allowed.**
5. Write your **Name** and **Registration Number** in the space provided at the bottom.
6. All answers are to be marked only on the machine gradable Objective Response Sheet (**ORS**) provided along with this booklet, as per the instructions therein.
7. The Question Booklet along with the Objective Response Sheet (**ORS**) must be handed over to the Invigilator before leaving the examination hall.
8. Refer to **Special Instruction/Useful Data** on reverse of this sheet.

**B. Filling-in the ORS:**

9. Write your Registration Number in the boxes provided on the upper left-hand-side of the **ORS** and darken the appropriate bubble under each digit of your Registration Number using a **HB pencil**.
10. Ensure that the **code** on the **Question Booklet** and the **code** on the **ORS** are the same. If the codes do not match, report to the Invigilator immediately.
11. On the lower-left-hand-side of the **ORS**, write your Name, Registration Number, and Name of the Test Centre and put your signature in the appropriate box with ball-point pen. Do not write these anywhere else.

**C. Marking of Answers on the ORS:**

12. Each question has **4 choices** for its answer: (A), (B), (C) and (D). Only **ONE** of them is the correct answer.
13. On the right-hand-side of **ORS**, for each question number, darken with a **HB Pencil** ONLY one bubble corresponding to what you consider to be the most appropriate answer, from among the four choices.
14. There will be **negative marking** for wrong answers.

**MARKING SCHEME:**

- (a) For each correct answer, you will be awarded **3 (Three)** marks.
- (b) For each wrong answer, you will be awarded **-1 (Negative one)** mark.
- (c) Multiple answers to a question will be treated as a wrong answer.
- (d) For each un-attempted question, you will be awarded **0 (Zero)** mark.

<b>Name</b>							
<b>Registration Number</b>							

**Special Instructions/ Useful Data**

**N** denotes the set of natural numbers  $\{1, 2, 3, \dots\}$

**Q** denotes the set of rational numbers

**R** denotes the set of real numbers

$A \setminus B = \{x \in A \mid x \notin B\}$ , for two sets  $A, B$

$f'$  denotes the first derivative of  $f$

$f''$  denotes the second derivative of  $f$

$f_x = \frac{\partial f}{\partial x}$  denotes the partial derivative of  $f$  with respect to  $x$

$f_{xx}, f_{xy}, f_{yx}, f_{yy}$  denote the usual second order partial derivatives of  $f$

$\nabla f$  denotes the gradient of  $f$

$P(X = n)$  denotes the probability of  $X = n$

$\bar{x}$  denotes the complement of a Boolean variable  $x$

LPP denotes Linear Programming Problem

$\max f$  denotes maximum of  $f$

$\min f$  denotes minimum of  $f$

For all C programs, assume that all standard library functions are accessible.

Q.1 Consider the following C program

```
#include <stdio.h>
int main() {
    int x = 01234;
    printf("%d", x);
    return 0;
}
```

The output of the program will be

- (A) 01234                      (B) 1234                      (C) 567                      (D) 668

Q.2 Consider the following C function

```
float f(float a, int m) {
    float x;
    if (m == 0) return 1;
    x = f(a, m/2);
    if (m%2 == 1) return x * x * a;
    else return x * x;
}
```

What will be the return value of the function  $f(2, 3)$ ?

- (A) 20.0                      (B) 16.0                      (C) 12.0                      (D) 8.0

Q.3 When a computer is switched on, the BIOS is loaded from

- (A) Hard Disk                      (B) RAM                      (C) ROM                      (D) CD-ROM

Q.4 In a computer, TFT is related to

- (A) Memory                      (B) Monitor                      (C) Input Device                      (D) Serial Port

Q.5 Consider the following lists:

**List I**

1. Pen drive
2. Hard disk
3. CD-ROM
4. Floppy

**List II**

- P. Optical Memory
- Q. Flash Memory
- R. Magnetic Memory
- S. Volatile Memory

The correct match is

- (A) 1 → P, 2 → R, 3 → P, 4 → S                      (B) 1 → Q, 2 → R, 3 → P, 4 → R  
(C) 1 → S, 2 → P, 3 → R, 4 → Q                      (D) 1 → Q, 2 → R, 3 → S, 4 → R

Q.6 Consider the following C program

```
#include <stdio.h>
int main(){
    int x = 5;
    int y = 2;
    while (x) {
        y += 2 * x;
        printf("%d", x);
        x--;
    }
    printf("%d", y);
    return 0;
}
```

What is printed when the above program is executed?

- (A) 5432132                      (B) 432132                      (C) 5432129                      (D) 432130

Q.7 If the speed of a computer is 2 GHz, then which one of the following statements must be TRUE?

- (A) Its processor performs  $2 \times 10^9$  operations per second  
 (B) Its clock cycles  $2 \times 10^9$  times per second  
 (C) Its RAM stores  $2 \times 10^9$  bytes per second  
 (D) Its printer prints  $2 \times 10^9$  characters per second

Q.8 Consider the following lists:

- |               |                      |
|---------------|----------------------|
| <b>List I</b> | <b>List II</b>       |
| 1. Linux      | P. Text File Editor  |
| 2. Mozilla    | Q. Image File Format |
| 3. Notepad    | R. Operating System  |
| 4. JPEG       | S. Web Browser       |

The correct match is

- (A) 1 → R, 2 → S, 3 → P, 4 → Q                      (B) 1 → S, 2 → R, 3 → Q, 4 → P  
 (C) 1 → R, 2 → P, 3 → S, 4 → Q                      (D) 1 → Q, 2 → S, 3 → P, 4 → R

Q.9 If  $y = x \cos x$  is a solution of an  $n$ -th order linear differential equation

$$\frac{d^n y}{dx^n} + a_1 \frac{d^{n-1} y}{dx^{n-1}} + \dots + a_{n-1} \frac{dy}{dx} + a_n y = 0$$

with real constant coefficients, then the least possible value of  $n$  is

- (A) 1                                      (B) 2                                      (C) 3                                      (D) 4

Q.10 The general solution of the differential equation

$$\frac{dy}{dx} = (1+y^2)(e^{-x^2} - 2x \tan^{-1}y)$$

is

- (A)  $e^{x^2} \tan^{-1}y = x + c$  (B)  $e^{-x^2} \tan y = x + c$   
 (C)  $e^x \tan y = x^2 + c$  (D)  $e^{-x} \tan^{-1}y = x^3 + c$

Q.11 If  $g(x, y)dx + (x+y)dy = 0$  is an exact differential equation and if  $g(x, 0) = x^2$ , then the general solution of the differential equation is

- (A)  $2x^3 + 2xy + y^2 = c$  (B)  $2x^3 + 6xy + 3y^2 = c$   
 (C)  $2x + 2xy + y^2 = c$  (D)  $x^2 + xy + y^2 = c$

Q.12 The value of  $\int_0^1 \frac{dx}{\sqrt{x(1-x)}}$  is

- (A) 0 (B)  $\frac{\pi}{2}$  (C)  $\pi$  (D)  $2\pi$

Q.13 Let  $f(x) = \int_0^x (t-1)(t^2-5t+6)dt$  for all  $x \in \mathbf{R}$ . Then

- (A)  $f$  is continuous but not differentiable on  $\mathbf{R}$   
 (B)  $f'$  is bounded on  $\mathbf{R}$   
 (C)  $f'$  has exactly three zeroes  
 (D)  $f$  is continuous and bounded on  $\mathbf{R}$

Q.14 If  $f(x, y) = \frac{1}{x^2} \tan^{-1} \frac{x}{\sqrt{x^2+y^2}} + \frac{x^{10}}{y^{12}} e^{\frac{x^2}{y^2}}$  for  $x > 1, y > \frac{\pi}{2}$ ,

then  $x \frac{\partial f}{\partial x} + y \frac{\partial f}{\partial y} + 1000f$  equals

- (A)  $998f$  (B)  $999f$  (C)  $1000f$  (D)  $1002f$

Q.15 The general solution of the differential equation

$$\frac{d^2y}{dx^2} = \left( \frac{dy}{dx} \right)^2$$

is

- (A)  $x = c_1 e^{-y} + c_2 e^y$  (B)  $x = c_1 e^y + c_2$  (C)  $x = c_1 e^{-y} + c_2$  (D)  $x = c_1 e^y + c_2 y$

Q.16 Let  $f(x, y) = \begin{cases} xy \frac{x^4 - y^4}{x^4 + y^4} & \text{if } (x, y) \neq (0, 0), \\ 0 & \text{if } (x, y) = (0, 0). \end{cases}$

Which of the following is TRUE?

- (A)  $f_{xy}(0, 0) \neq f_{yx}(0, 0)$
- (B)  $f_{xy}(x, y) = f_{yx}(x, y)$  for all  $(x, y)$
- (C)  $f_x(x, 0)$  does not exist for any real  $x$
- (D)  $\lim_{(x, y) \rightarrow (0, 0)} f(x, y) = 1$

Q.17 The value of  $\int_{1/2}^2 \frac{1}{x} \sin\left(x - \frac{1}{x}\right) dx$  is

- (A) 1
- (B)  $\frac{\pi}{2}$
- (C) 0
- (D)  $\sin\left(\frac{3}{2}\right)$

Q.18 The area included between the curves  $x^2 + y^2 = a^2$  and  $b^2x^2 + a^2y^2 = a^2b^2$  ( $a > 0, b > 0$ ), is

- (A)  $\frac{\pi a}{2} |a - b|$
- (B)  $\pi |a^2 - 3ab + b^2|$
- (C)  $\pi a |a - b|$
- (D)  $\pi |a^2 - b^2|$

Q.19 Changing the order of integration of  $\int_1^2 \int_0^x f(x, y) dy dx$  gives

- (A)  $\int_0^1 \int_1^2 f(x, y) dx dy + \int_0^1 \int_0^1 f(x, y) dx dy$
- (B)  $\int_0^1 \int_1^2 f(x, y) dx dy + \int_1^2 \int_1^2 f(x, y) dx dy$
- (C)  $\int_0^1 \int_{y/2}^y f(x, y) dx dy + \int_1^2 \int_y^{2y} f(x, y) dx dy$
- (D)  $\int_0^1 \int_y^1 f(x, y) dx dy + \int_1^2 \int_1^y f(x, y) dx dy$

Q.20 The volume of the closed region bounded by the surfaces  $x^2 + y^2 = 2x$ ,  $z = -1$  and  $z = 1$  is

- (A) 0
- (B)  $\frac{\pi}{2}$
- (C)  $2\pi$
- (D)  $\pi$

Q.21 Let  $f(x) = \begin{cases} x+1 & \text{if } x < 0, \\ (x-1)^2 & \text{if } x \geq 0. \end{cases}$

Which one of the following is TRUE?

- (A)  $f$  is differentiable on  $\mathbf{R}$
- (B)  $f$  has neither a local maximum nor a local minimum in  $\mathbf{R}$
- (C)  $f$  is bounded on  $\mathbf{R}$
- (D)  $f$  is not differentiable at  $x = 0$  but has a local maximum at  $x = 0$

Q.22 If  $p_{ij} = 1$  for  $1 \leq i, j \leq m$ , then the characteristic equation of the matrix  $P = (p_{ij})$  is

- (A)  $\lambda^m - \lambda^{m-1} + 1 = 0$
- (B)  $\lambda^m - m = 0$
- (C)  $\lambda^m - m\lambda^{m-1} = 0$
- (D)  $\lambda^m + 1 = 0$

Q.23 If  $P = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$ , then  $P^{50}$  equals

- |  |  |
|--|--|
| <p>(A) <math>\begin{bmatrix} 1 &amp; 100 &amp; 500 \\ 0 &amp; 1 &amp; 100 \\ 0 &amp; 0 &amp; 1 \end{bmatrix}</math></p> <p>(C) <math>\begin{bmatrix} 50 &amp; 100 &amp; 150 \\ 0 &amp; 50 &amp; 100 \\ 0 &amp; 0 &amp; 50 \end{bmatrix}</math></p> | <p>(B) <math>\begin{bmatrix} 1 &amp; 50 &amp; 100 \\ 0 &amp; 1 &amp; 50 \\ 0 &amp; 0 &amp; 1 \end{bmatrix}</math></p> <p>(D) <math>\begin{bmatrix} 1 &amp; 50 &amp; 1275 \\ 0 &amp; 1 &amp; 50 \\ 0 &amp; 0 &amp; 1 \end{bmatrix}</math></p> |
|--|--|

Q.24 The dimension of the subspace

$$W = \{(x, y, z, w) \in \mathbf{R}^4 \mid x + y + z + w = 0, \quad x + y + 2z = 0, \quad x + 3y = 0\}$$

is

- (A) 1
- (B) 2
- (C) 3
- (D) 4

Q.25 Let  $P$  be a matrix of size  $3 \times 3$  with eigenvalues 1, 2 and 3. Then  $P$  is

- (A) neither invertible nor diagonalizable
- (B) both invertible and diagonalizable
- (C) invertible but not diagonalizable
- (D) not invertible but diagonalizable

Q.26 The integral  $\int_{-1}^1 |x| dx$  is computed by the trapezoidal rule with step length  $h = 0.01$ . The absolute error in the computed value is

- (A) 0
- (B) 0.0001
- (C) 0.0025
- (D) 0.005

Q.27 An iteration scheme generates a sequence  $\{x_n\}$ . For some  $\alpha, c \in \mathbf{R}$ ,  $\{x_n\}$  satisfies  $|\alpha - x_{n+1}| \leq c |\alpha - x_n|$  for all  $n \geq 0$ . Which one of the following conditions on  $c$  ensures the convergence of  $\{x_n\}$ ?

- (A)  $c = 1$                       (B)  $c > 1$                       (C)  $c > 0$                       (D)  $0 < c < 1$

Q.28 The integral  $\int_0^1 f(x) dx$  is approximated by the formula

$$\int_0^1 f(x) dx \approx \alpha_1 f(0) + \alpha_2 f(1) + \alpha_3 f'(0) + \alpha_4 f'(1).$$

This approximation is exact for all the polynomials of degree  $\leq 3$ . Then  $(\alpha_3, \alpha_4)$  is

- (A)  $\left(\frac{1}{6}, -\frac{1}{6}\right)$               (B)  $\left(\frac{1}{12}, \frac{1}{12}\right)$               (C)  $\left(\frac{1}{12}, -\frac{1}{12}\right)$               (D)  $\left(\frac{1}{6}, \frac{1}{6}\right)$

Q.29 An approximate value of  $\sqrt{3}$  is computed by the formula  $x_{n+1} = x_n - \frac{1}{4}(x_n^2 - 3)$ . If  $x_0 = 1.75$ , the value of  $x_1$  correct to three decimal places is

- (A) 1.734                      (B) 1.733                      (C) 1.732                      (D) 1.731

Q.30 Consider the following table:

$x$	1	2	3
$y$	-10	-6	0

The roots of the corresponding interpolating quadratic polynomial are

- (A) -4, 3                      (B) 3, 4                      (C) -2, 4                      (D) -1, 3

Q.31 The optimal solution of the LPP

$$\max f = 2x + 3y + 20$$

subject to

$$\begin{aligned} x + y &\leq 1, \\ 2x + 5y &\leq 3, \\ x \geq 0, \quad y &\geq 0, \end{aligned}$$

is

- (A)  $\left(\frac{1}{3}, \frac{2}{3}\right)$               (B)  $\left(\frac{2}{3}, \frac{1}{3}\right)$               (C)  $\left(0, \frac{3}{5}\right)$               (D)  $\left(\frac{3}{2}, 0\right)$



Q.32 The number of optimal solutions of the LPP  

$$\max f = 2x + 3y$$
 subject to  

$$4x + 6y \leq 5,$$

$$2x + 2y \geq 1,$$

$$x \geq 0, \quad y \geq 0,$$

is

- (A) zero (B) one  
 (C) two (D) infinite

Q.33 The value of  $x$  in the sequence 2, 4, 10, 28, 82,  $x, \dots$  is

- (A) 102 (B) 168 (C) 252 (D) 244

Q.34 Consider the following segment of a C program

```
int x = 2;
if (x = 3) printf("%d", x++);
else printf("%d", --x);
```

The output of the program segment will be

- (A) 0 (B) 2 (C) 3 (D) 4

Q.35 Four different weights  $W_1, W_2, W_3, W_4$  can take only integral values. They can be used on one or both the pans of a balance to weigh objects having all possible integral weights from unit weight to  $W$ , where,  $W = W_1 + W_2 + W_3 + W_4$ . The vector  $(W_1, W_2, W_3, W_4)$  which maximizes  $W$  is

- (A) (1, 2, 5, 10) (B) (1, 3, 9, 27) (C) (1, 2, 4, 8) (D) (1, 3, 15, 25)

Q.36 In a C program, variables  $x$  and  $y$  are declared to be of type `int`. Consider the following four statements

```
S1: y = x & 1;      S2: y = x % 2;
S3: y = x / 2;     S4: y = x << 1;
```

Which of the statements will result in the same value of  $y$  for every value of  $x$ ?

- (A) S3 and S4 (B) S1 and S3 (C) S1 and S2 (D) S2 and S4

Q.37 IBM stands for

- (A) Indian Business Machine  
 (B) International Business Manufacturer  
 (C) Indian Business Manufacturer  
 (D) International Business Machine

Q.38 Consider the following fragment of a C program

```
int x = 20;
int y = 25;
int z = x ^ y;
```

where ^ denotes bit-wise XOR operation. Then the value assigned to z will be

- (A) 20                      (B) 25                      (C) 23                      (D) 13

Q.39 An ASCII code contains

- (A) 8 bits                      (B) 4 bits                      (C) 7 bits                      (D) 6 bits

Q.40 Who among the following developed Linux ?

- (A) Bill Gates                      (B) Sabeer Bhatia                      (C) Narayan Murthy                      (D) Linus Torvalds

Q.41 IPR stands for

- (A) Intelligence Performance Ratio
- (B) Intellectual Property Rights
- (C) Intelligence Production Rights
- (D) Intellectual Performance Research

Q.42 A software is termed an open source software if

- (A) the developer company is open 24 hours
- (B) its source code is available to share, study and modify
- (C) it can be downloaded from the Internet
- (D) it is available free of cost

Q.43 The rank of the matrix  $\begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 4 & 5 & 6 & 7 \end{bmatrix}$  is

- (A) 1                      (B) 2                      (C) 3                      (D) 4

Q.44 Consider the following LPP

$$\min f = 4x + 3y$$

subject to

$$x + y \geq 12,$$

$$4x + 3y \geq 36,$$

$$x \geq 2, \quad y \geq 2.$$

The minimum value of  $f$  is

- (A) 36                      (B) 48                      (C) 46                      (D) 38

Q.45 An LPP has the following constraints:

$$\begin{aligned} 2x + 5y &\geq 10, \\ 3x + 4y &\leq 24, \\ x &\geq y, \\ x \geq 0, \quad y &\geq 0. \end{aligned}$$

Which of the following is **NOT** a feasible solution to the LPP ?

- (A) (8, 0)                      (B) (5, 0)                      (C)  $\left(\frac{10}{7}, \frac{10}{7}\right)$                       (D) (5, 3)

Q.46 Consider the following LPP:

$$\begin{aligned} \max f &= 2x + 5y \\ \text{subject to} \\ 5x + 6y &\geq 15, \\ 6x + 15y &\leq 90, \\ x &\leq 10, \\ x \geq 0, \quad y &\geq 0. \end{aligned}$$

The number of extreme points of the feasible region of the LPP is

- (A) 3                                  (B) 4                                  (C) 5                                  (D) 6

Q.47 A particular integral of the differential equation  $\frac{d^2y}{dx^2} - 16y = 4\sinh^2 2x$  is

- (A)  $\frac{1}{8}(xe^{4x} + xe^{-4x} - 1)$                       (B)  $\frac{1}{8}(xe^{4x} - xe^{-4x} + 1)$   
 (C)  $\frac{1}{4}\left(e^{4x} - xe^{-4x} + \frac{1}{2}\right)$                       (D)  $\frac{1}{4}\left(xe^{4x} + e^{-4x} + \frac{1}{2}\right)$

Q.48 The general solution of the differential equation  $\frac{d^3y}{dx^3} - 3\frac{d^2y}{dx^2} + 4y = 0$  is

- (A)  $y = c_1e^x + c_2e^{2x} + c_3xe^{2x}$                       (B)  $y = c_1e^{-x} + c_2e^{2x} + c_3xe^{2x}$   
 (C)  $y = c_1e^{-x} + c_2xe^{-x} + c_3e^{2x}$                       (D)  $y = c_1e^{-x} + c_2e^x + c_3e^{4x}$

Q.49 The area bounded by the curves  $x^2 = 4 - 2y$  and  $x^2 = y + 4$  is

- (A) 16                                  (B) 24                                  (C) 30                                  (D) 36

Q.50 The volume of the region in  $\mathbf{R}^3$  given by  $3|x| + 4|y| + 3|z| \leq 12$  is

- (A) 64                                  (B) 48                                  (C) 32                                  (D) 24

- Q.51 Let  $F(x, y, z) = x^2 + y^2 + z^2 + xy + yz + zx$ . The value of  $F_x + F_y + F_z$  at  $(1, 1, 1)$  is  
 (A) 12 (B) 10 (C) 16 (D) 8
- Q.52 Three unbiased dice of different colours are rolled. The probability that the same number appears on at least two of the three dice is  
 (A)  $\frac{5}{36}$  (B)  $\frac{1}{2}$  (C)  $\frac{5}{12}$  (D)  $\frac{4}{9}$
- Q.53 An unbiased coin is tossed eight times. The probability of obtaining at least one head and at least one tail is  
 (A)  $\frac{255}{256}$  (B)  $\frac{127}{128}$  (C)  $\frac{63}{64}$  (D)  $\frac{31}{32}$
- Q.54 Suppose the sum and the product of the mean and the variance of a binomial random variable are 10 and 24 respectively. Then the probability of success in a single trial is  
 (A)  $\frac{1}{4}$  (B)  $\frac{3}{4}$  (C)  $\frac{2}{3}$  (D)  $\frac{1}{3}$
- Q.55 A Poisson random variable  $X$  has unit mean. Then  $P(X = \text{odd})$  is  
 (A)  $\frac{1}{2} \left( 1 - \frac{1}{e} \right)$  (B)  $1 - \frac{1}{e^2}$  (C)  $\frac{1}{2} - \frac{1}{e^2}$  (D)  $\frac{1}{2} \left( 1 - \frac{1}{e^2} \right)$
- Q.56 The order of the permutation  $(12)(546)(3978)$  in the symmetric group  $S_9$  is  
 (A) 6 (B) 9 (C) 12 (D) 24
- Q.57 If  $\alpha = (13)(254)$  in the symmetric group  $S_5$ , then  $\alpha^{65}$  equals  
 (A)  $(13)(254)$  (B)  $(12)(345)$  (C)  $(32)(154)$  (D)  $(31)(245)$
- Q.58 Let  $S$  be a set with 10 elements. The number of subsets of  $S$  having odd number of elements is  
 (A) 256 (B) 512 (C) 752 (D) 1024
- Q.59 If  $\vec{a}, \vec{b}, \vec{c}$  are three vectors in  $\mathbf{R}^3$ , then  $(\vec{a} - \vec{b} + \vec{c}) \cdot ((\vec{b} - \vec{c} + \vec{a}) \times (\vec{c} - \vec{a} + \vec{b}))$  equals  
 (A) 0 (B)  $\vec{a} \cdot (\vec{b} \times \vec{c})$  (C)  $4 \vec{a} \cdot (\vec{b} \times \vec{c})$  (D)  $6 \vec{a} \cdot (\vec{b} \times \vec{c})$

- Q.60 If  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ , then  $\nabla |\vec{r}|^4$  equals
- (A)  $4|\vec{r}|$                       (B)  $4|\vec{r}|^2\vec{r}$                       (C)  $4|\vec{r}|\vec{r}$                       (D)  $4|\vec{r}|^3$
- Q.61 The area of the parallelogram in  $\mathbf{R}^2$  whose diagonals are  $3\hat{i} + \hat{j}$  and  $\hat{i} - 3\hat{j}$  is
- (A) 2.5                      (B) 5                      (C)  $\sqrt{2.5}$                       (D)  $\sqrt{5}$
- Q.62 Let  $a_0 + a_1x + a_2x^2 + a_3x^3 + \dots$  be the Taylor series for the function  $\sin(x^2 + 3x)$  about  $x = 0$ . Then  $a_3$  equals
- (A)  $-\frac{9}{2}$                       (B)  $\frac{9}{2}$                       (C)  $\frac{27}{2}$                       (D)  $-\frac{27}{2}$
- Q.63 The number of real values of  $a$  for which the set  $\{(a, a^2), (a^2, a)\}$  is **NOT** a basis of  $\mathbf{R}^2$ , is
- (A) 1                      (B) 2                      (C) 3                      (D) 4
- Q.64 The set  $(\mathbf{Q} \times \mathbf{Q}) \setminus (\mathbf{N} \times \mathbf{N})$  equals
- (A)  $(\mathbf{Q} \setminus \mathbf{N}) \times (\mathbf{Q} \setminus \mathbf{N})$                       (B)  $[(\mathbf{Q} \setminus \mathbf{N}) \times \mathbf{Q}] \cup [\mathbf{Q} \times (\mathbf{Q} \setminus \mathbf{N})]$   
 (C)  $[(\mathbf{N} \times \mathbf{Q}) \setminus (\mathbf{Q} \times \mathbf{N})] \cup [(\mathbf{Q} \times \mathbf{N}) \setminus (\mathbf{N} \times \mathbf{Q})]$                       (D)  $(\mathbf{Q} \times \mathbf{N}) \setminus (\mathbf{N} \times \mathbf{Q})$
- Q.65 Let  $f(x) = \frac{2}{1+x^2}$  for all  $x \in \mathbf{R}$ . Then  $\lim_{n \rightarrow \infty} \frac{1}{n} \left( f'\left(\frac{1}{n}\right) + f'\left(\frac{2}{n}\right) + \dots + f'\left(\frac{n}{n}\right) \right)$  equals
- (A) -2                      (B) -1                      (C) 1                      (D) 2
- Q.66 Let  $f(x) = \begin{cases} x+x^2 & \text{if } x \geq 0, \\ x^2 & \text{if } x < 0. \end{cases}$

Which one of the following is TRUE?

- (A)  $f'(0) = 1$  and  $f''(0) = 2$   
 (B)  $f'(0) = 1$  but  $f''(0)$  is not defined  
 (C)  $f'(0)$  does not exist  
 (D)  $f$  is not continuous at  $x = 0$
- Q.67 Let  $f(x) = 2x^3 + 3x^2 - 12x + 4$  for all  $x \in \mathbf{R}$ . Then
- (A)  $f$  is not one-one on  $[-1, 1]$   
 (B)  $f$  is one-one on  $[-1, 1]$  but not one-one on  $[-2, 2]$   
 (C)  $f$  is one-one on  $[0, 2]$  but not one-one on  $[-2, 0]$   
 (D)  $f$  is one-one on  $[-2, 2]$

Q.68 Let  $f(x, y) = x^3 + y^3$  for all  $(x, y) \in \mathbf{R}^2$ . Then

- (A)  $f$  has a local maximum at  $(0, 0)$
- (B)  $f$  has a local minimum at  $(0, 0)$
- (C)  $f$  has neither a local maximum nor a local minimum at  $(0, 0)$
- (D)  $f$  has both a local maximum and a local minimum at  $(0, 0)$

Q.69 Let  $F$  be a field with five elements and let  $K = \{(a, b) \mid a, b \in F\}$  with the binary operations defined component-wise. Then

- |                                     |                                     |
|-------------------------------------|-------------------------------------|
| (A) $K$ is not a field              | (B) $K$ is a field with 5 elements  |
| (C) $K$ is a field with 25 elements | (D) $K$ is a field with 32 elements |

Q.70 Let  $f(x, y) = \begin{cases} \frac{x}{|x|} \sqrt{x^2 + y^2} & \text{if } x \neq 0, \\ 0 & \text{if } x = 0. \end{cases}$

Then  $f_x(0, 0) + f_y(0, 0)$  equals

- |          |          |         |         |
|----------|----------|---------|---------|
| (A) $-2$ | (B) $-1$ | (C) $0$ | (D) $1$ |
|----------|----------|---------|---------|

Q.71 Let  $a_1, a_2, \dots, a_n$  be a finite sequence of numbers with the property  $a_i \leq a_{i+2}$  for all  $i \in \{1, \dots, n-2\}$ . Which one of the following is always TRUE?

- (A) The sequence is sorted
- (B) First  $(n-2)$  elements of the sequence are sorted
- (C) The first element of the sequence is the minimum
- (D) Either  $a_{n-1}$  or  $a_n$  is the maximum of the sequence

Q.72 Order the following memory types in increasing order of access time

M1: Cache, M2: CD-ROM, M3: Hard disk, M4: RAM, M5: Register

- |                    |                    |
|--------------------|--------------------|
| (A) M5 M1 M4 M3 M2 | (B) M5 M1 M3 M4 M2 |
| (C) M1 M5 M4 M3 M2 | (D) M1 M4 M5 M3 M2 |

Q.73 Consider the following statements about terminating (finite number of digits to the right of the point) representations

X: If the binary representation of a number terminates then its corresponding decimal representation also terminates.

Y: If the decimal representation of a number terminates then its corresponding binary representation also terminates.

Then

- |                              |                              |
|------------------------------|------------------------------|
| (A) X is true but Y is false | (B) Y is true but X is false |
| (C) both X and Y are true    | (D) neither X nor Y is true  |

Q.74 The octal equivalent of decimal 204 is

- |         |         |         |         |
|---------|---------|---------|---------|
| (A) 304 | (B) 306 | (C) 314 | (D) 316 |
|---------|---------|---------|---------|

Q.75 Consider the following C program

```
int main() {
    char str[] = "leap";
    int len = strlen(str)-1;
    int i = 0;
    while (i <= len) {
        str[i] = str[len-i];
        i++;
    }
    printf("%s", str);
    return 0;
}
```

The output of the program will be

- |          |          |          |          |
|----------|----------|----------|----------|
| (A) paal | (B) pael | (C) papa | (D) paap |
|----------|----------|----------|----------|

Q.76 Let  $f(A, B, C, D) = ABC + B(\overline{C} + \overline{D})$  be a Boolean function. The complement of  $f(A, B, C, D)$  is

- |   |   |
|---|---|
| (A) $\overline{B} + \overline{A} CD$  | (B) $A \overline{B} + \overline{A} \overline{C} \overline{D} + \overline{B} \overline{C}$ |
| (C) $B \overline{A} + \overline{B} \overline{A} \overline{D} + \overline{A} \overline{C}$ | (D) $\overline{C} \overline{D} + \overline{A} \overline{B} \overline{C}$                  |

Q.77 The number of three digit numbers greater than 100 in which digits appear in strictly increasing order is

- |        |        |        |         |
|--------|--------|--------|---------|
| (A) 36 | (B) 84 | (C) 90 | (D) 120 |
|--------|--------|--------|---------|

Q.78 Consider the following C function

```

int oddeven(int n) {
    int i = 0;
    while(n>1) {
        if (n%2)
            n = 3*n+1;
        else
            n = n/2;
        i++;
    }
    return i;
}

```

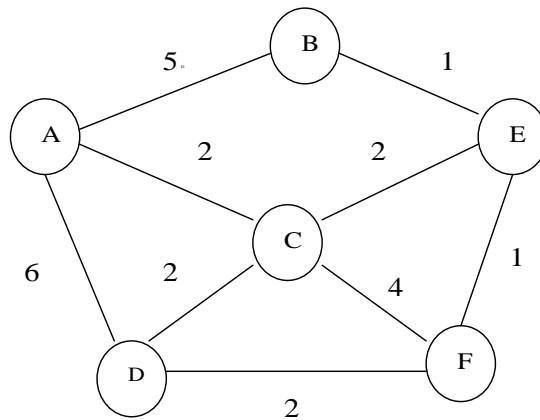
If  $n = 12$  is given as input, what is the return value?

- (A) 8                      (B) 9                      (C) 10                      (D) 12

Q.79 The next number in the sequence of binary numbers 0, 10, 100, 110, ... is

- (A) 101                      (B) 1000                      (C) 1001                      (D) 1010

Q.80 Following graph shows distances between six cities A through F.



If  $x$  and  $y$  are minimum and maximum distances from A to F where no city is visited more than once, then  $(x, y)$  is

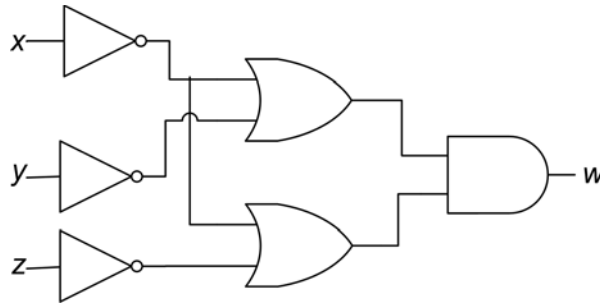
- (A) (6, 11)                      (B) (5, 12)                      (C) (4, 13)                      (D) (6, 12)

Q.81 The number of reflexive relations on a set with four elements is

- (A) 10                      (B) 1024                      (C) 4096                      (D) 8192



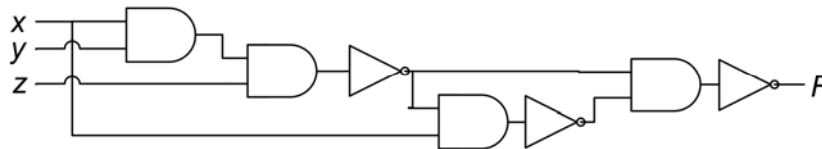
Q.82 Consider the following logic circuit:



The output  $w$  is

- (A)  $\bar{y} + \bar{x}\bar{z}$       (B)  $\bar{x} + \bar{y}\bar{z}$       (C)  $\bar{z} + \bar{x}\bar{y}$       (D)  $\bar{x}(\bar{y} + \bar{z})$

Q.83 Consider the following logic circuit:



The output  $F$  is

- (A)  $x$       (B)  $xy$       (C)  $x + y$       (D)  $xz$

Q.84 WWW stands for

- (A) World Wide Wire      (B) World With Web  
(C) World Wide Web      (D) World Wise Web

Q.85 The first Prime Minister of India was

- (A) Indira Gandhi      (B) Lal Bahadur Shastri  
(C) Rajendra Prasad      (D) Jawaharlal Nehru

Q.86 Consider the following two lists:

**List I**

1. DOS
2. P4
3. Java
4. PC

**List II**

- P. Sun Microsystems
- Q. Microsoft Corporation
- R. IBM
- S. Intel Corporation

The correct match is

- (A)  $1 \rightarrow Q, 2 \rightarrow S, 3 \rightarrow P, 4 \rightarrow R$       (B)  $1 \rightarrow Q, 2 \rightarrow R, 3 \rightarrow S, 4 \rightarrow P$   
(C)  $1 \rightarrow S, 2 \rightarrow P, 3 \rightarrow Q, 4 \rightarrow R$       (D)  $1 \rightarrow R, 2 \rightarrow P, 3 \rightarrow Q, 4 \rightarrow S$

- Q.87 The song “Vande Mataram” was written by
- (A) Bankim Chandra Chatterjee (B) Rabindranath Tagore  
(C) A. R. Rahman (D) Satyajit Ray
- Q.88 The number of gold medals won by India in the commonwealth games held in New Delhi in 2010 is
- (A) 36 (B) 37 (C) 38 (D) 40
- Q.89 When  $28^{30} - 15^{30}$  is divided by 13, the remainder is
- (A) 0 (B) 1 (C) 11 (D) 12
- Q.90 Let  $H$  be a subgroup of order 60 of a group  $G$  of order 120. If  $a \in G \setminus H$ , then which of the following is **NOT** a subgroup of  $G$ ?
- (A)  $\{ah \mid h \in H\}$  (B)  $\{h^{-1} \mid h \in H\}$   
(C)  $\{aha^{-1} \mid h \in H\}$  (D)  $H \cup \{a^{-1}h \mid h \in H\}$
- Q.91 Consider the following system of equations
- $$\begin{aligned} 2x + 3y + 4z &= 13 \\ 5x + 7y + 7z &= 26 \\ 9x + 13y + 15z &= 13\lambda \end{aligned}$$
- The value of  $\lambda$  for which the system has infinitely many solutions is
- (A) 1 (B) 2 (C) 3 (D) 4
- Q.92 Let  $x * y = 3xy$  for all  $x, y \in \mathbf{R} \setminus \{0\}$ . The inverse of the element 2 in the group  $(\mathbf{R} \setminus \{0\}, *)$  is
- (A)  $\frac{1}{2}$  (B)  $\frac{1}{3}$  (C)  $\frac{1}{6}$  (D)  $\frac{1}{18}$
- Q.93 The number of subsets of  $\{1, 2, \dots, 10\}$  which are disjoint from  $\{3, 7, 8\}$  is
- (A) 128 (B) 1021 (C) 1016 (D) 7
- Q.94 If  $Q$  and  $Q^+$  denote the outputs during the current and the next clock cycles of a  $JK$  flip-flop, which one of the following is its characteristic equation?
- (A)  $Q^+ = J\bar{Q} + \bar{K}Q$  (B)  $Q^+ = JQ + \bar{K}\bar{Q}$  (C)  $Q^+ = \bar{J}Q + \bar{K}Q$  (D)  $Q^+ = \bar{J}\bar{Q} + KQ$

Q.95 The number of functions taking two Boolean variables as input and providing three Boolean variables as output is

- (A) 12                      (B) 32                      (C) 4096                      (D) 65536

Q.96 The Boolean expression  $(X + Y)(\bar{X} + Z)$  equals

- (A)  $X Y + \bar{X} Z$               (B)  $Z Y + Z \bar{X}$               (C)  $\bar{X} Z + Y \bar{Z}$               (D)  $X Z + \bar{X} Y$

Q.97 Consider the following algorithm

```

gcd(a, b)
begin
  if b equals 0 then return a
  else return gcd(b, X)
end

```

Which of the following expressions for  $X$  returns the gcd of positive integers  $a$  and  $b$ ?

- (A)  $a / b$                       (B)  $b / a$                       (C)  $a \bmod b$                       (D)  $b \bmod a$

Q.98 Let  $P, Q, R$  and  $S$  be statements, each of which can be either true or false. It is known that if  $P$  is true or  $Q$  is true then  $R$  is true and  $S$  is false. Suppose it is given that  $R$  is false. Then which one of the following will certainly be TRUE?

- (A) Both  $P$  and  $Q$  are true  
 (B)  $P$  is true and  $Q$  is false  
 (C)  $P$  is false and  $Q$  is true  
 (D) Both  $P$  and  $Q$  are false

Q.99 A  $JK$  flip-flop runs on a clock of period 20 KHz. If we set  $J = K = 1$ , the output  $Q$  is a

- (A) constant LOW                      (B) constant HIGH  
 (C) 10 KHz wave                      (D) 20 KHz wave

Q.100 HIV stands for

- (A) Human Immunodeficiency Virus  
 (B) Hypersensitive Internal Vein  
 (C) Human Interactive Virus  
 (D) Human Immune Virus



**SPACE FOR ROUGH WORK**



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