

Q. No. 1 – 25 Carry One Mark Each

1. Consider an undirected random graph of eight vertices. The probability that there is an edge between a pair of vertices is $\frac{1}{2}$. What is the expected number of unordered cycles of length three?

(A) $\frac{1}{8}$ (B) 1 (C) 7 (D) 8

Answer: (C)

2. Which of the following statements is/are **TRUE** for undirected graphs?

P: Number of odd degree vertices is even.

Q: Sum of degrees of all vertices is even.

(A) P only (B) Q only
(C) Both P and Q (D) Neither P nor Q

Answer: (C)

3. Function f is known at the following points:

x	0	0.3	0.6	0.9	1.2	1.5	1.8	2.1	2.4	2.7	3.0
f(x)	0	0.09	0.36	0.81	1.44	2.25	3.24	4.41	5.76	7.29	9.00

The value of $\int_0^3 f(x) dx$ computed using the trapezoidal rule is

(A) 8.983 (B) 9.003 (C) 9.017 (D) 9.045

Answer: (D)

4. Which one of the following functions is continuous at $x = 3$?

$$(A) f(x) = \begin{cases} 2, & \text{if } x = 3 \\ x - 1, & \text{if } x > 3 \\ \frac{x+3}{3}, & \text{if } x < 3 \end{cases}$$

$$(B) f(x) = \begin{cases} 4, & \text{if } x = 3 \\ 8 - x, & \text{if } x \neq 3 \end{cases}$$

$$(C) f(x) = \begin{cases} x + 3, & \text{if } x \leq 3 \\ x - 4, & \text{if } x > 3 \end{cases}$$

$$(D) f(x) = \frac{1}{x^3 - 27}, \text{ if } x \neq 3$$

Answer: (A)

5. Which one of the following expressions does **NOT** represent exclusive NOR of x and y ?

(A) $xy + x'y'$ (B) $x \oplus y'$ (C) $x' \oplus y$ (D) $x' \oplus y'$

Answer: (D)

6. In a k -way set associative cache, the cache is divided into v sets, each of which consists of k lines. The lines of a set are placed in sequence one after another. The lines in set s are sequenced before the lines in set $(s+1)$. The main memory

blocks are numbered 0 onwards. The main memory block numbered j must be mapped to any one of the cache lines from

- (A) $(j \bmod v) * k$ to $(j \bmod v) * k + (k - 1)$
- (B) $(j \bmod v)$ to $(j \bmod v) + (k - 1)$
- (C) $(j \bmod k)$ to $(j \bmod k) + (v - 1)$
- (D) $(j \bmod k) * v$ to $(j \bmod k) * v + (v - 1)$

Answer: (B)

7. What is the time complexity of Bellman-Ford single-source shortest path algorithm on a complete graph of n vertices?

- (A) $\Theta(n^2)$
- (B) $\Theta(n^2 \log n)$
- (C) $\Theta(n^3)$
- (D) $\Theta(n^3 \log n)$

Answer: (C)

8. Which of the following statements are **TRUE**?

- (1) The problem of determining whether there exists a cycle in an undirected graph is in P.
 - (2) The problem of determining whether there exists a cycle in an undirected graph is in NP.
 - (3) If a problem A is NP-Complete, there exists a non-deterministic polynomial time algorithm to solve A.
- (A) 1, 2 and 3 (B) 1 and 2 only (C) 2 and 3 only (D) 1 and 3 only

Answer: (A)

9. Which of the following statements is/are **FALSE**?

- (1) For every non-deterministic Turing machine, there exists an equivalent deterministic Turing machine.
 - (2) Turing recognizable languages are closed under union and complementation.
 - (3) Turing decidable languages are closed under intersection and complementation
 - (4) Turing recognizable languages are closed under union and intersection.
- (A) 1 and 4 only (B) 1 and 3 only (C) 2 only (D) 3 only

Answer: (C)

10. Three concurrent processes X, Y, and Z execute three different code segments that access and update certain shared variables. Process X executes the P operation (i.e., wait) on semaphores a, b and c; process Y executes the P operation on semaphores b, c and d; process Z executes the P operation on semaphores c, d, and a before entering the respective code segments. After completing the execution of its code segment, each process invokes the V operation (i.e., signal) on its three semaphores. All semaphores are binary semaphores initialized to one. Which one of the following represents a deadlock-free order of invoking the P operations by the processes?

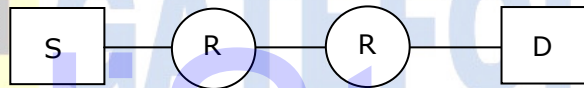
- (A) X : P(a)P(b)P(c) Y : P(b)P(c)P(d) Z : P(c)P(d)P(a)
 (B) X : P(b)P(a)P(c) Y : P(b)P(c)P(d) Z : P(a)P(c)P(d)
 (C) X : P(b)P(a)P(c) Y : P(c)P(b)P(d) Z : P(a)P(c)P(d)
 (D) X : P(a)P(b)P(c) Y : P(c)P(b)P(d) Z : P(c)P(d)P(a)

Answer: (B)

11. An index is clustered, if
 (A) it is on a set of fields that form a candidate key.
 (B) it is on a set of fields that include the primary key.
 (C) the data records of the file are organized in the same order as the data entries of the index.
 (D) the data records of the file are organized not in the same order as the data entries of the index.

Answer: (C)

12. Assume that source S and destination D are connected through two intermediate routers labeled R. Determine how many times each packet has to visit the network layer and the data link layer during a transmission from S to D.



- (A) Network layer – 4 times and Data link layer-4 times
 (B) Network layer – 4 times and Data link layer-3 times
 (C) Network layer – 4 times and Data link layer-6 times
 (D) Network layer – 2 times and Data link layer-6 times

Answer: (C)

13. The transport layer protocols used for real time multimedia, file transfer, DNS and email, respectively are
 (A) TCP, UDP, UDP and TCP (B) UDP, TCP, TCP and UDP
 (C) UDP, TCP, UDP and TCP (D) TCP, UDP, TCP and UDP

Answer: (C)

14. Using public key cryptography, X adds a digital signature σ to message M, encrypts $\langle M, \sigma \rangle$, and sends it to Y, where it is decrypted. Which one of the following sequences of keys is used for the operations?
 (A) Encryption: X's private key followed by Y's private key; Decryption: X's public key followed by Y's public key
 (B) Encryption: X's private key followed by Y's public key; Decryption: X's public key followed by Y's private key
 (C) Encryption: X's public key followed by Y's private key; Decryption: Y's public key followed by X's private key
 (D) Encryption: X's private key followed by Y's public key; Decryption: Y's private key followed by X's public key

Answer: (D)

15. Match the problem domains in **Group I** with the solution technologies in **Group II**.

Group I	Group II
(p) Services oriented computing	(1) Interoperability
(q) Heterogeneous communicating systems	(2) BPMN
(R) Information representation	(3) Publish-find bind
(S) Process description	(4) XML
(A) P - 1, Q - 2, R - 3, S - 4	(B) P - 3, Q - 4, R - 2, S - 1
(C) P - 3, Q - 1, R - 4, S - 2	(D) P - 4, Q - 3, R - 2, S - 1

Answer: (C)

16. A scheduling algorithm assigns priority proportional to the waiting time of a process. Every process starts with priority zero (the lowest priority). The scheduler re-evaluates the process priorities every T time units and decides the next process to schedule. Which one of the following is TRUE if the processes have no I/O operations and all arrive at time zero?

- (A) This algorithm is equivalent to the first-come-first-serve algorithm.
 (B) This algorithm is equivalent to the round-robin algorithm.
 (C) This algorithm is equivalent to the shortest-job-first algorithm.
 (D) This algorithm is equivalent to the shortest-remaining-time-first algorithm.

Answer: (B)

17. What is the maximum number of reduce moves that can be taken by a bottom-up parser for a grammar with no epsilon- and unit-production (i.e., of type $A \rightarrow \epsilon$ and $A \rightarrow a$) to parse a string with n tokens?

- (A) $n/2$ (B) $n-1$ (C) $2n-1$ (D) 2^n

Answer: (C)

18. Consider the languages $L_1 = \Phi$ and $L_2 = \{a\}$. Which one of the following represents $L_1 L_2^* U L_1^*$?

- (A) $\{\epsilon\}$ (B) Φ (C) a^* (D) $\{\epsilon, a\}$

Answer: (A)

19. Which one of the following is the tightest upper bound that represents the time complexity of inserting an object into a binary search tree of n nodes?

- (A) $O(1)$ (B) $O(\log n)$ (C) $O(n)$ (D) $O(n \log n)$

Answer: (C)

20. Which one of the following is the tightest upper bound that represents the number of swaps required to sort n numbers using selection sort?

- (A) $O(\log n)$ (B) $O(n)$ (C) $O(n \log n)$ (D) $O(n^2)$

Answer: (B)

21. In the following truth table, $V = 1$ if and only if the input is valid.

Inputs				Outputs		
D_0	D_1	D_2	D_3	X_0	X_1	V
0	0	0	0	X	X	0
1	0	0	0	0	0	1
X	1	0	0	0	1	1
X	X	1	0	1	0	1
X	X	X	1	1	1	1

What function does the truth table represent?

- (A) Priority encoder (B) Decoder
(C) Multiplexer (D) Demultiplexer

Answer: (A)

22. The smallest integer that can be represented by an 8-bit number in 2's complement form is

- (A) -256 (B) -128 (C) -127 (D) 0

Answer: (B)

23. Which one of the following does **NOT** equal

$$\begin{vmatrix} 1 & x & x^2 \\ 1 & y & y^2 \\ 1 & z & z^2 \end{vmatrix} ?$$

(A) $\begin{vmatrix} 1 & x(x+1) & x+1 \\ 1 & y(y+1) & y+1 \\ 1 & z(z+1) & z+1 \end{vmatrix}$

(B) $\begin{vmatrix} 1 & x+1 & x^2+1 \\ 1 & y+1 & y^2+1 \\ 1 & z+1 & z^2+1 \end{vmatrix}$

(C) $\begin{vmatrix} 0 & x-y & x^2-x^2 \\ 0 & y-z & y^2-z^2 \\ 1 & z & z^2 \end{vmatrix}$

(D) $\begin{vmatrix} 2 & x+y & x^2+y^2 \\ 2 & y+z & y^2+z^2 \\ 1 & z & z^2 \end{vmatrix}$

Answer: (A)

24. Suppose p is number of cars per minute passing through a certain road junction between 5 PM and 6PM, and p has a Poisson distribution with mean 3. What is

the probability of observing fewer than 3 cars during any given minute in this interval?

- (A) $8 / (2e^3)$ (B) $9 / (2e^3)$ (C) $17 / (2e^3)$ (D) $26 / (2e^3)$

Answer: (C)

25. A binary operation \oplus on a set of integers is defined as $x \oplus y = x^2 + y^2$. Which one of the following statements is **TRUE** about \oplus ?

- (A) Commutative but not associative (B) Both commutative and associative
(C) Associative but not commutative (D) Neither commutative nor associative

Answer: (A)

Q. No. 26 – 55 Carry Two Marks Each

26. Which one of the following is **NOT** logically equivalent to $\neg \exists x (\forall y (\alpha) \wedge \forall z (\beta))$?

- (A) $\forall x (\exists z (\neg \beta) \rightarrow \forall y (\alpha))$ (B) $\forall x (\forall z (\beta) \rightarrow \exists y (\neg \alpha))$
(C) $\forall x (\forall y (\alpha) \rightarrow \exists z (\neg \beta))$ (D) $\forall x (\exists y (\neg \alpha) \rightarrow \exists z (\neg \beta))$

Answer: (A)

27. A RAM chip has a capacity of 1024 words of 8 bits each ($1K \times 8$). The number of 2×4 decoders with enable line needed to construct a $16K \times 16$ RAM from $1K \times 8$ RAM is

- (A) 4 (B) 5 (C) 6 (D) 7

Answer: (D)

28. Consider an instruction pipeline with five stages without any branch prediction: Fetch Instruction (FI), Decode Instruction (DI), Fetch Operand (FO), Execute Instruction (EI) and Write Operand (WO). The stage delays for FI, DI, FO, EI and WO are 5 ns, 7 ns, 10 ns, 8 ns and 6 ns, respectively. There are intermediate storage buffers after each stage and the delay of each buffer is 1 ns. A program consisting of 12 instructions $I_1, I_2, I_3, \dots, I_{12}$ is executed in this pipelined processor. Instruction I_4 is the only branch instruction and its branch target is I_9 . If the branch is taken during the execution of this program, the time (in ns) needed to complete the program is

- (A) 132 (B) 165 (C) 176 (D) 328

Answer: (A)

29. Consider the following operation along with Enqueue and Dequeue operations on queues, where k is a global parameter

```

MultiDequeue(Q) {
    m = k
    while (Q is not empty) and (m > 0) {
        Dequeue (Q)
        m = m - 1
    }
}

```

What is the worst case time complexity of a sequence of n queue operations on an initially empty queue?

- (A) $\Theta(n)$ (B) $\Theta(n+k)$ (C) $\Theta(nk)$ (D) $\Theta(n^2)$

Answer: (C)

30. The preorder traversal sequence of a binary search tree is 30, 20, 10, 15, 25, 23, 39, 35, 42. Which one of the following is the postorder traversal sequence of the same tree?

- (A) 10,20,15,23,25,35,42,39,30 (B) 15,10,25,23,20,42,35,39,30
 (C) 15,20,10,23,25,42,35,39,30 (D) 15,10,23,25,20,35,42,39,30

Answer: (D)

31. What is the return value of $f(p,p)$ if the value of p is initialized to 5 before the call? Note that the first parameter is passed by reference, whereas the second parameter is passed by value.

```

int f (int & x, int c) {
    c = c - 1;
    if (c == 0) return 1;
    x = x + 1;
    return f(x,c) * x;
}

```

- (A) 3024 (B) 6561 (C) 55440 (D) 161051

Answer: (B)

32. Which of the following is/are undecidable?

1. G is a CFG. Is $L(G) = \Phi$?
2. G is a CFG. IS $L(G) = \Sigma^*$?
3. M is a Turning machine. Is $L(M)$ regular?
4. A is a DFA and N is a NFA. Is $L(A) = L(N)$?

- (A) 3 only (B) 3 and 4 only (C) 1, 2 and 3 only (D) 2 and 3 only

Answer: (D)

33. Consider the following two sets of LR(1) items of an LR(1) grammar

$X \rightarrow cX, c/d$	$X \rightarrow cX, \$$
$X \rightarrow .cX, c/d$	$X \rightarrow .cX, \$$
$X \rightarrow .d, c/d$	$X \rightarrow .d, \$$

Which of the following statements related to merging of the two sets in the corresponding LALR parser is/are **FALSE**?

- Cannot be merged since look aheads are different
- Can be merged but will result in S-R conflict
- Can be merged but will result in R-R conflict
- Cannot be merged since goto on c will lead to two different sets

- (A) 1 only (B) 2 only (C) 1 and 4 only (D) 1, 2, 3 and 4

Answer: (D)

34. A certain computation generates two arrays a and b such that $a[i] = f(i)$ for $0 \leq i < n$ and $b[i] = g(a[i])$ for $0 \leq i < n$. Suppose this computation is decomposed into two concurrent processes X and Y such that X computes the array a and Y computes the array b. The processes employ two binary semaphores R and S, both initialized to zero. The array a is shared by the two processes. The structures of the processes are shown below.

<pre> Process X; private i; for (i = 0; i < n; i++) { a[i] = f(i); ExitX(R, S); } </pre>	<pre> Process Y; private i; for (i = 0; i < n; i++) { EntryY(R, S); b[i] = g(a[i]); } </pre>
---	---

Which one of the following represents the **CORRECT** implementations of ExitX and EntryY?

- | | |
|-------------------|-------------------|
| (A) ExitX(R, S) { | (B) ExitX(R, S) { |
| P(R); | V(R); |
| V(S); | V(S); |
| } | } |
| EntryY(R, S) { | EntryY(R, S) { |
| P(S); | P(R); |
| V(R); | P(S); |
| } | } |


```
(C) ExitX(R, S) {
    P(S);
    V(R);
}
```

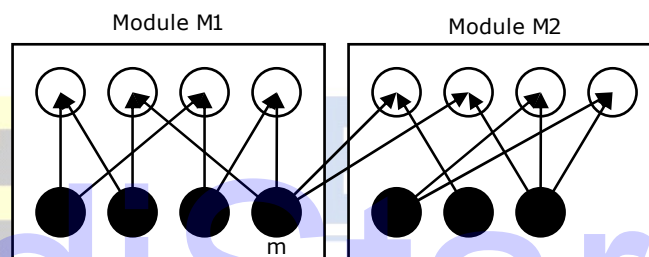
```
EntryY(R, S) {
    V(S);
    P(R);
}
```

```
(D) ExitX(R, S) {
    V(R);
    P(S);
}
```

```
EntryY(R, S) {
    V(S);
    P(R);
}
```

Answer: (D)

35. The following figure represents access graphs of two modules M1 and M2. The filled circles represent methods and the unfilled circles represent attributes. IF method *m* is moved to module M2 keeping the attributes where they are, what can we say about the average cohesion and coupling between modules in the system of two modules?



- (A) There is no change.
 (B) Average cohesion goes up but coupling is reduced
 (C) Average cohesion goes down and coupling also reduces
 (D) Average cohesion and coupling increase

Answer: (C)

36. In an IPv4 datagram, the M bit is 0, the value of HLEN is 10, the value of total length is 400 and the fragment offset value is 300. The position of the datagram, the sequence numbers of the first and the last bytes of the payload, respectively are
- (A) Last fragment, 2400 and 2789 (B) First fragment, 2400 and 2759
 (C) Last fragment, 2400 and 2759 (D) Middle fragment, 300 and 689

Answer: (C)

37. Determine the maximum length of cable (in km) for transmitting data at a rate of 500 Mbps in an Ethernet LAN with frames of size 10,000 bits. Assume the signal speed in the cable to be 2,00,000 km/s
- (A) 1 (B) 2 (C) 2.5 (D) 5

Answer: (B)

4. A accepts all strings over $\{0, 1\}$ of length at least 2
 (A) 1 and 3 only (B) 2 and 4 only (C) 2 and 3 only (D) 3 and 4 only

Answer: (D)

41. Consider the following languages

$$L_1 = \{0^p 1^q 0^r \mid p, q, r \geq 0\}$$

$$L_2 = \{0^p 1^q 0^r \mid p, q, r \geq 0, p \neq r\}$$

Which one of the following statements is FALSE?

- (A) L_2 is context-free
 (B) $L_1 \cap L_2$ is context-free
 (C) Complement of L_2 is recursive
 (D) Complement of L_1 is context-free but not regular

Answer: (D)

42. Consider the following function

```
int unknown(int n){
    int i, j, k = 0;
    for (i = n / 2; i <= n; i++)
        for (j = 2; j <= n; j = j * 2)
            k = k + n / 2;
    return (k);
}
```

- (A) $\Theta(n^2)$ (B) $\Theta(n^2 \log n)$ (C) $\Theta(n^3)$ (D) $\Theta(n^3 \log n)$

Answer: (B)

43. The number of elements that can be sorted in $\Theta(\log n)$ time using heap sort is

- (A) $\Theta(1)$ (B) $\Theta(\sqrt{\log n})$ (C) $\Theta\left(\frac{\log n}{\log \log n}\right)$ (D) $\Theta(\log n)$

Answer: (A)

44. Consider a hard disk with 16 recording surfaces (0 – 15) having 16384 cylinders (0 – 16383) and each cylinder contains 64 sectors (0 – 63). Data storage capacity in each sector is 512 bytes. Data are organized cylinder-wise and the addressing format is < cylinder no., sector no.>. A file of size 42797 KB is stored in the disk

and the starting disk location of the file is $\langle 1200, 9, 40 \rangle$. What is the cylinder number of the last sector of the file, if it is stored in a contiguous manner?

- (A) 1281 (B) 1282 (C) 1283 (D) 1284

Answer: (C)

45. Consider the following sequence of micro-operations

MBR \leftarrow PC

MAR \leftarrow X

PC \leftarrow Y

Memory \leftarrow MBR

Which one of the following is a possible operation performed by this sequence?

- (A) Instruction fetch (B) Operand fetch
(C) Conditional branch (D) Initiation of interrupt service

Answer: (D)

46. The line graph $L(G)$ of a simple graph G is defined as follows:

- There is exactly one vertex $v(e)$ in $L(G)$ for each edge e in G .
- For any two edges e and e' in G , $L(G)$ has an edge between $v(e)$ and $v(e')$, if and only if e and e' are incident with the same vertex in G .

Which of the following statements is/are **TRUE**?

- (P) The line graph of a cycle is a cycle.
(Q) The line graph of a clique is a clique.
(R) The line graph of a planar graph is planar.
(S) The line graph of a tree is a tree.
- (A) P only (B) P and R only (C) R only (D) P, Q and S only

Answer:

47. What is the logical translation of the following statement?

"None of my friends are perfect."

- (A) $\exists x (F(x) \wedge \neg P(x))$ (B) $\exists x (\neg F(x) \wedge P(x))$
(C) $\exists x (\neg F(x) \wedge \neg P(x))$ (D) $\neg \exists x (F(x) \wedge P(x))$

Answer: (D)

Common Data Questions: 48 & 49

The procedure given below is required to find and replace certain characters inside an input character string supplied in array A. The characters to be replaced are supplied in array oldc, while their respective replacement characters are supplied in array newc. Array A has a fixed length of five characters, while arrays oldc and newc contain three characters each. However, the procedure is flawed

```
void find_and_replace (char * A, char * oldc, char * newc) {
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 3; j++)
            if (A[i] == oldc[j]) A[i] = newc[j];
}
```

The procedure is tested with the following four test cases

- (1) oldc = "abc", newc = "dab" (2) oldc = "cde", newc = "bcd"
 (3) oldc = "bca", newc = "cda" (4) oldc = "abc", newc = "bac"

48. The tester now tests the program on all input strings of length five consisting of characters 'a', 'b', 'c', 'd' and 'e' with duplicates allowed. If the tester carries out this testing with the four test cases given above, how many test cases will be able to capture the flaw?

- (A) Only one (B) Only two (C) Only three (D) All four

Answer: (B)

49. If array A is made to hold the string "abcde", which of the above four test cases will be successful in exposing the flaw in this procedure?

- (A) None (B) 2 only (C) 3 and 4 only (D) 4 only

Answer: (C)

Common Data Questions: 50 & 51

The following code segment is executed on a processor which allows only register operands in its instructions. Each instruction can have almost two source operands and one destination operand. Assume that all variables are dead after this code segment

```

c = a + b;
d = c * a;
e = c + a;
x = c * c;
if (x > a) {
    y = a * a;
}
else {
    d = d * d;
    e = e * e;
}

```

50. Suppose the instruction set architecture of the processor has only two registers. The only allowed compiler optimization is code motion, which moves statements from one place to another while preserving correctness. What is the minimum number of spills to memory in the compiled code?

(A) 0 (B) 1 (C) 2 (D) 3

Answer: (C)

51. What is the minimum number of registers needed in the instruction set architecture of the processor to compile this code segment without any spill to memory? Do not apply any optimization other than optimizing register allocation

(A) 3 (B) 4 (C) 5 (D) 6

Answer: (B)

Linked Answer Questions: Q.52 to Q.55 Carry Two Marks Each

Statement for Linked Answer Questions: 52 & 53

Relation R has eight attributes ABCDEFGH. Fields of R contain only atomic values.

$F = \{CH \rightarrow G, A \rightarrow BC, B \rightarrow CFH, E \rightarrow A, F \rightarrow EG\}$ is a set of functional dependencies (FDs) so that F^+ is exactly the set of FDs that hold for R

52. How many candidate keys does the relation R have?

(A) 3 (B) 4 (C) 5 (D) 6

Answer: (B)

53. The relation R is

(A) in 1NF, but not in 2NF (B) in 2NF, but not in 3NF
 (C) in 3NF, but not in BCNF (D) in BCNF

Answer: (A)

Statement for Linked Answer Questions: 54 & 55

A computer uses 46-bit virtual address, 32-bit physical address, and a three-level paged page table organization. The page table base register stores the base address of the first-level table (T_1), which occupies exactly one page. Each entry of T_1 stores the base address of a page of the second-level table (T_2). Each entry of T_2 stores the base address of a page of the third-level table (T_3). Each entry of T_3 stores a page table entry (PTE). The PTE is 32 bits in size. The processor used in the computer has a 1 MB 16 way set associative virtually indexed physically tagged cache. The cache block size is 64 bytes.

54. What is the size of a page in KB in this computer?
 (A) 2 (B) 4 (C) 8 (D) 16

Answer:

55. What is the minimum number of page colours needed to guarantee that no two synonyms map to different sets in the processor cache of this computer?
 (A) 2 (B) 4 (C) 8 (D) 16

Answer:

Q. No. 56 – 60 Carry One Mark Each

56. Complete the sentence:
 Universalism is to particularism as diffuseness is to _____
 (A) specificity (B) neutrality (C) generality (D) adaptation

Answer: (A)
 The relation is that of antonyms

57. Were you a bird, you _____ in the sky.
 (A) would fly (B) shall fly
 (C) should fly (D) shall have flown

Answer: (A)

58. Which one of the following options is the closest in meaning to the word given below?

Nadir

- (A) Highest (B) Lowest (C) Medium (D) Integration

Answer: (B)

Nadir in the lowest point on a curve

59. Choose the grammatically INCORRECT sentence:
 (A) He is of Asian origin
 (B) They belonged to Africa
 (C) She is an European
 (D) They migrated from India to Australia

Answer: (C)

60. What will be the maximum sum of 44, 42, 40, ... ?
 (A) 502 (B) 504 (C) 506 (D) 500

Answer: (C)

The maximum sum is the sum of 44, 42, - - - -2.

The sum of 'n' terms of an AP

$$= \frac{n}{2} [2a + (n-1)d]$$

In this case, $n = 22$, $a = 44$ and $d = -2$

$$\therefore \text{Sum} = 11[4 + 21 \times (-2)] = 11 \times 46 = 506$$

Q. No. 61 – 65 Carry Two Marks Each

61. Out of all the 2-digit integers between 1 and 100, a 2-digit number has to be selected at random. What is the probability that the selected number is not divisible by 7?
 (A) 13/90 (B) 12/90 (C) 78/90 (D) 77/90

Answer: (D)

The number of 2 digit multiples of 7 = 13

\therefore Probability of choosing a number

$$\text{Not divisible by 7} = \frac{90 - 13}{90} = \frac{77}{90}$$

62. A tourist covers half of his journey by train at 60 km/h, half of the remainder by bus at 30 km/h and the rest by cycle at 10 km/h. The average of the tourist in km/h during his entire journey is
 (A) 36 (B) 30 (C) 24 (D) 18

Answer: (C)

Let the total distance covered be 'D'

$$\text{Now, average speed} = \frac{D}{\text{Total time taken}}$$

$$= \frac{D}{\left(\frac{D}{60} + \frac{D}{30} + \frac{D}{40} \right)} = \frac{1}{\frac{1}{120} + \frac{1}{120} + \frac{1}{40}} = \frac{120}{5} = 24 \text{ km/hr}$$

63. Find the sum of the expression

$$\frac{1}{\sqrt{1} + \sqrt{2}} + \frac{1}{\sqrt{2} + \sqrt{3}} + \frac{1}{\sqrt{3} + \sqrt{4}} + \dots + \frac{1}{\sqrt{80} + \sqrt{81}}$$

- (A) 7 (B) 8 (C) 9 (D) 10

Answer: (B)

The expression can be written as

$$\frac{(\sqrt{2})^2 - (\sqrt{1})^2}{\sqrt{1} + \sqrt{2}} + \frac{(\sqrt{3})^2 - (\sqrt{2})^2}{\sqrt{2} + \sqrt{3}} + \dots + \frac{(\sqrt{81})^2 - (\sqrt{80})^2}{\sqrt{80} + \sqrt{81}}$$

$$= \frac{(\sqrt{2} - \sqrt{1})(\sqrt{1} + \sqrt{2})}{(\sqrt{1} + \sqrt{2})} + \dots + \frac{(\sqrt{81} - \sqrt{80})(\sqrt{81} + \sqrt{80})}{\sqrt{80} + \sqrt{81}}$$

64. The current erection cost of a structure is Rs. 13,200. If the labour wages per day increase by $\frac{1}{5}$ of the current wages and the working hours decrease by $\frac{1}{24}$ of the current period, then the new cost of erection in Rs. is
- (A) 16,500 (B) 15,180 (C) 11,000 (D) 10,120

Answer: (B)

Let 'W' be the labour wages, and 'T' be the working hours.

Now, total cost is a function of $W \times T$

Increase in wages = 20%

∴ Revised wages = 1.2 W

Decrease in labour time = $\left(\frac{100}{24}\right)\%$

∴ Revised time = $\left(1 - \frac{1}{24}\right)T = \frac{23}{24}T$

∴ Revised Total cost = $1.2 \times \frac{23}{24} WT = 1.15WT$
 $= 1.15 \times 13200 = 15180$

65. After several defeats in wars, Robert Bruce went in exile and wanted to commit suicide. Just before committing suicide, he came across a spider attempting tirelessly to have its net. Time and again, the spider failed but that did not deter it to refrain from making attempts. Such attempts by the spider made Bruce curious. Thus, Bruce started observing the near-impossible goal of the spider to have the net. Ultimately, the spider succeeded in having its net despite several failures. Such act of the spider encouraged Bruce not to commit suicide. And then, Bruce went back again and won many a battle, and the rest is history. Which one of the following assertions is best supported by the above information?
- (A) Failure is the pillar of success
 (B) Honesty is the best policy
 (C) Life begins and ends with adventures
 (D) No adversity justifies giving up hope

Answer: (D)