

## DiplETE – ET / CS (OLD SCHEME)

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Code: DE01 / DC01  
Time: 3 Hours

**JUNE 2011**

Subject: MATHEMATICS - I  
Max. Marks: 100

**NOTE:** There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
  - The answer sheet for the Q.1 will be collected by the invigilator after 45 Minutes of the commencement of the examination.
  - Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
  - Any required data not explicitly given, may be suitably assumed and stated.
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**Q.1** Choose the correct or the best alternative in the following: (2 × 10)

a. How many terms are there in the sequence

3, 6, 9, 12 ....., 111?

- (A) 34 (B) 36  
(C) 37 (D) 33

b. If  $\sin A = \frac{3}{5}$  and  $\cos B = \frac{9}{41}$ ,  $0 < A < \frac{\pi}{2}$ ,  $0 < B < \frac{\pi}{2}$ , find the value of  $\sin(A + B)$

- (A)  $-\frac{133}{205}$  (B)  $\frac{187}{205}$   
(C)  $\frac{156}{205}$  (D)  $-\frac{84}{205}$

c. The area of triangle whose vertices are (6, 3), (-3, 5) & (4, -2) is :

- (A) 24.5 sq. unit (B) 24 sq. unit  
(C) 25.5 sq. unit (D) 25 sq unit

d. Evaluate  $\lim_{x \rightarrow 0} \frac{\cos 2x - 1}{\cos x - 1}$

- (A) 2 (B)  $\frac{1}{2}$   
(C) 4 (D)  $\frac{1}{4}$

e. If  $y = \tan^{-1}\left(\frac{1 + \tan x}{1 - \tan x}\right)$  then  $\frac{dy}{dx}$  is :

- (A) 1 (B) -1  
(C) 0 (D)  $\frac{1}{2}$

f. Evaluate  $\int \frac{1}{16 + 9x^2} dx$

- (A)  $\frac{1}{6} \tan^{-1}\left(\frac{3x}{4}\right) + C$  (B)  $\frac{1}{12} \tan^{-1}\left(\frac{3x}{4}\right) + C$   
(C)  $\tan^{-1}\left(\frac{3x}{4}\right) + C$  (D)  $-\frac{1}{12} \tan^{-1}\left(\frac{3x}{4}\right) + C$

g. Evaluate  $\int_0^1 xe^x dx$

- (A) 0 (B) -1  
(C) 2 (D) 1

h. If  $\frac{dy}{dx} = x \log x$  then the value of  $y$  will be:

- (A)  $\frac{x^2}{2} \log x + \frac{1}{2} \left(\frac{x^2}{2}\right) + C$  (B)  $\frac{x^2}{2} \log x - \frac{1}{2} \left(\frac{x^2}{2}\right) + C$   
(C)  $\frac{x}{2} \log x + \frac{1}{2} \left(\frac{x^2}{2}\right) + C$  (D)  $\frac{x^2}{2} \log x - \frac{x^2}{2} + C$

i. From a class of 32 students, 4 are to be chosen for a competition. In how many ways can this be done?

- (A) 35960 (B) 35900  
(C) 35940 (D) 35980

j. Find the equation of the line which makes intercepts -4 & 5 on the axes.

- (A)  $5x + 4y - 20 = 0$  (B)  $5x + 4y + 20 = 0$   
(C)  $5x - 4y + 20 = 0$  (D)  $-5x + 4y + 20 = 0$

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**Answer any FIVE Questions out of EIGHT Questions.**  
**Each question carries 16 marks.**

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**Q.2** a. Find three numbers in G.P. whose sum is 13 and the sum of whose squares is 91. (8)

- b. If  $x$  is numerically so small that  $x^2$  and higher power of  $x$  may be neglected then prove that  $\frac{(1-2x)^{2/3}(4+5x)^{3/2}}{\sqrt{1-x}} \approx 8 + \frac{25x}{3}$  (8)

**Q.3** a. Prove that:

$$\frac{\sin A - \sin 3A + \sin 5A - \sin 7A}{\cos A - \cos 3A - \cos 5A + \cos 7A} = \cot 2A \quad (8)$$

b. In any triangle ABC, prove that:

$$(b-c)\cot \frac{A}{2} + (c-a)\cot \frac{B}{2} + (a-b)\cot \frac{C}{2} = 0 \quad (8)$$

**Q.4** a. Prove by the principle of mathematical induction that for all  $n \in \mathbb{N}$ :

$$1+4+7+\dots+(3n-2) = \frac{1}{2}n(3n-1) \quad (8)$$

- b. If  $p$  be the length of perpendicular from the origin to the line whose intercepts on the axes are  $a$  &  $b$  respectively then show that  $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$  (8)

**Q.5** a. Find the equation of circle which passes through the points  $(5,-8), (2,-9)$  &  $(2, 1)$ . Find also the co-ordinates of its centre & radius. (8)

b. Find the equation of the parabola whose focus is  $(1,-1)$  and whose vertex is  $(2,1)$ . Also find its axis. (8)

**Q.6** a. Differentiate  $y = a^x$  w.r.t. ' $x$ ' from first principle. (8)

b. If  $y = \log \sqrt{\frac{a+b \sin x}{a-b \sin x}}$ , then find  $\frac{dy}{dx}$  (8)

**Q.7** a. Find all the points of maxima minima and the corresponding maximum and minimum values of the function:

$$f(x) = -x^3 + 12x^2 - 5 \quad (8)$$

b. Evaluate  $\int \frac{\log x}{x^2} dx$  (8)

**Q.8** a. Evaluate  $\int_0^{\pi/4} \log(1 + \tan x) dx$  (8)

b. Evaluate  $\int \frac{x-1}{x^3+1} dx$  (8)

**Q.9** a. Find the area of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, a > b$  **(8)**

b. Solve the differential equation

$$(x + y + 1) \frac{dy}{dx} = 1 \quad \text{(8)}$$