

DECEMBER 2007

Code: AE08

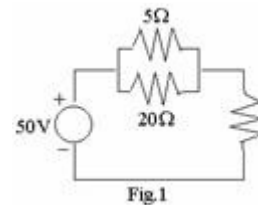
Subject: CIRCUIT THEORY & DESIGN

Time: 3 Hours

Max. Marks: 100

NOTE: There are 9 Questions in all.

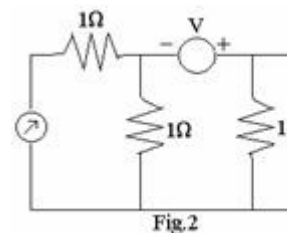
- Question 1 is compulsory and carries 20 marks. Answer to Q. 1. must be written in the space provided for it in the answer book supplied and nowhere else.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.



Q.1 Choose the correct or best alternative in the following: (2x10)

- a. Power in 5Ω resistor is 20W. The resistance R is
- (A) 10Ω .
 - (B) 20Ω .
 - (C) 16Ω .
 - (D) 8Ω .

b.



The Thevenin's equivalent circuit to the left of AB in Fig.2 has R_{eq} given by

- (A) $\frac{1}{3}\Omega$
- (B) $\frac{1}{2}\Omega$

(C) $1\ \Omega$

(D) $\frac{3}{2}\ \Omega$

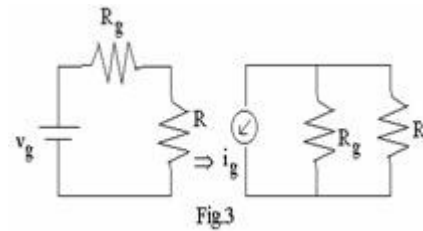
c. The energy stored in a capacitor is

(B) $\frac{1}{2} ci^2$

(B) $\frac{1}{2} \frac{1}{c} i^2$

(C) $\frac{1}{2} \frac{v^2}{c}$

(D) $\frac{1}{2} cv^2$



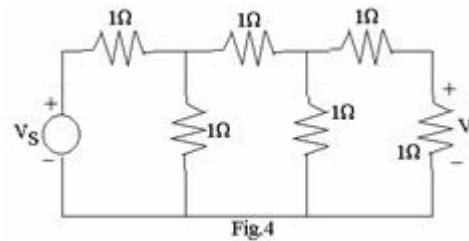
d. The Fig. 3 shown are equivalent of each other then

(A) $i_g = -\frac{v_g}{R_g}$

(B) $i_g = \frac{v_g}{R_g}$

(C) $i_g = v_g R_g$

(D) $i_g = \frac{R_g}{v_g}$



e. For the circuit shown in Fig. 4, the voltage across the last resistor is V . All resistors are of $1\ \Omega$.

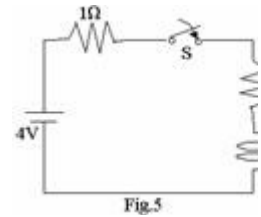
The V_s is given by

(A) 13V.

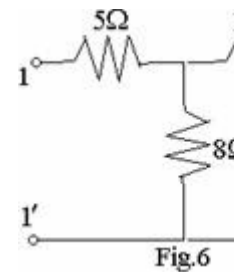
(B) 8V.

(C) 4V.

(D) 1V.



- f. In the circuit shown in Fig.5, the switch s is closed at $t = 0$ then the steady state value of the current is
- (A) 1 Amp. (B) 2 Amp.
 (C) 3 Amp. (D) $\frac{4}{3}$ Amp.



- g. The z parameters of the network shown in Fig.6 is

- (A) $\begin{bmatrix} 5 & 8 \\ 8 & 20 \end{bmatrix}$ (B) $\begin{bmatrix} 13 & 8 \\ 8 & 20 \end{bmatrix}$
 (C) $\begin{bmatrix} 8 & 20 \\ 13 & 12 \end{bmatrix}$ (D) $\begin{bmatrix} 5 & 8 \\ 8 & 12 \end{bmatrix}$

- h. For the pure reactive network the following condition to be satisfied

- (A) $M_1(j\omega)M_2(j\omega) + N_2(j\omega)N_1(j\omega) = 0$
 (B) $M_1(j\omega)N_1(j\omega) - N_2(j\omega)M_2(j\omega) = 0$
 (C) $M_1(j\omega)M_2(j\omega) - N_1(j\omega)N_2(j\omega) = 0$
 (D) $M_1(j\omega)N_2(j\omega) - N_1(j\omega)M_2(j\omega) = 0$

Where $M_1(j\omega)$ & $M_2(j\omega)$ even part of the numerator and denominator and N_1 N_2 are odd parts of the numerator & denominator of the network function.

- i. The network has a network function $Z(s) = \frac{s(s+2)}{(s+3)(s+4)}$. It is

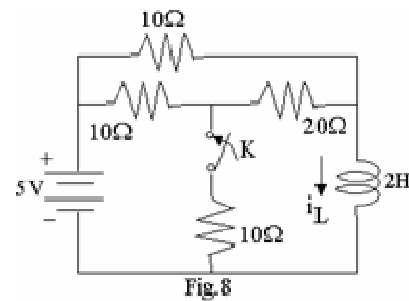
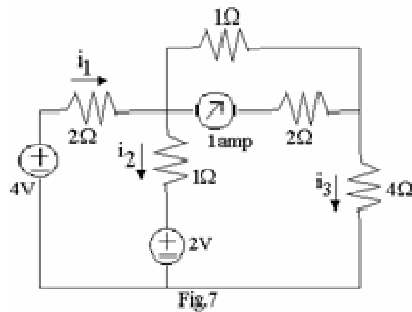
- (A) not a positive real function. (B) RL network.
 (C) RC network. (D) LC network.

j. The Q factor for an inductor L in series with a resistance R is given by

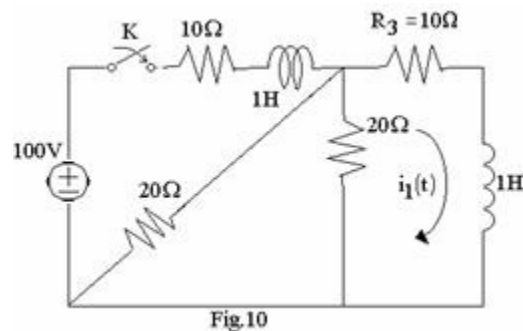
- (A) $\frac{\omega L}{R}$ (B) $\frac{R}{\omega L}$
 (C) ωLR (D) $\frac{1}{\omega LR}$

**Answer any FIVE Questions out of EIGHT Questions.
 Each question carries 16 marks.**

Q.2 a. For the circuit shown in Fig.7. Determine the current i_1, i_2 and i_3
 (8)



b. In the network of the Fig.8, the switch K is open and network reaches a steady state. At $t=0$, switch K is closed. Find the current in the inductor for $t > 0$.
 (8)



- Q.3** a. The network shown in the accompanying Fig.9 is in the steady state with the switch K closed. At $t = 0$ the switch is opened. Determine the voltage across the switch v_k and $\frac{dv_k}{dt}$ at $t = 0_+$. (6)

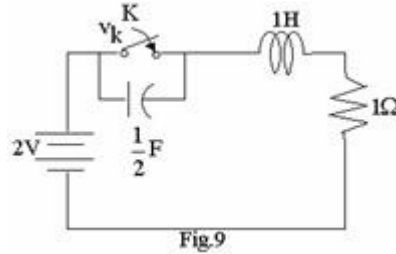


Fig.9

- b. Define Thevenin's theorem. (4)
- c. It is required to find the current $i_1(t)$ in the resistor R_3 , by using Thevenin's theorem: The network shown in Fig.10 is in zero state until $t = 0$ when the switch is closed. (6)

- Q.4** a. For the given network in Fig.11, determine the value of R_L that will cause the power in R_L to have a maximum value. What will be the value of power under this condition. (8)

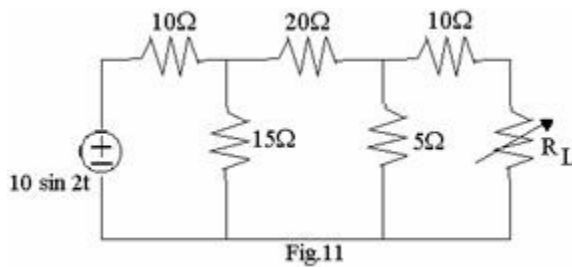


Fig.11

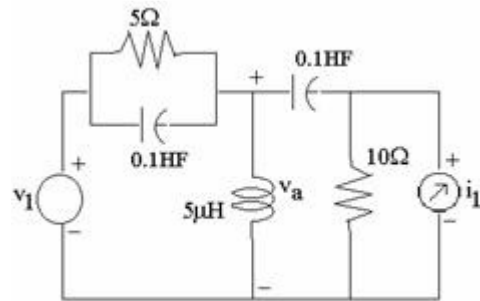


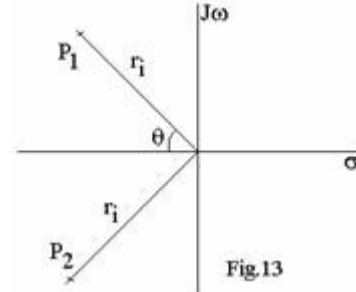
Fig.12

- b. In the network shown in Fig.12 $v_1 = 10 \sin 10^6 t$ and $i_1 = 10 \cos 10^6 t$ and the network is operating in the steady state – For the element values as given, determine the node to datum voltage $v_a(t)$. (8)

Q.5 a. Determine the amplitude and phase for F(J4) from the pole zero plot

$$F(s) = \frac{s^2 + 4}{(s + 2)(s^2 + 9)}$$

in s-plane for the network function . (8)



b. A network function consists of two poles at $P_{1,2} = r_1 e^{\pm j(\pi - \theta)} = -\sigma_1 \pm j\omega_1$ as given in the Fig.13. Show that the square of the amplitude response $M^2(\omega)$ is maximum at $\omega_m^2 = r_1^2 |\cos 2\theta|$. (8)

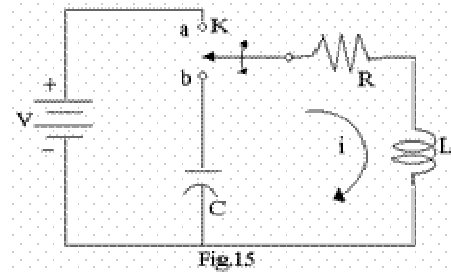
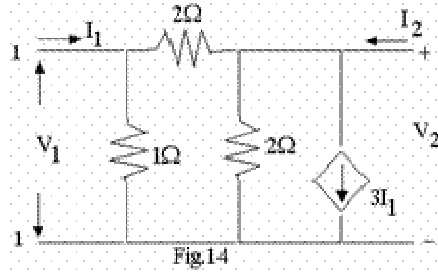
Q.6 a. Following short circuit currents and voltages are obtained experimentally for a two port network

(i) with output short circuited $I_1 = 5\text{mA}$ $I_2 = -0.3\text{mA}$ $V_1 = 25\text{V}$

(ii) with input short circuited $I_1 = -5\text{mA}$ $I_2 = 10\text{mA}$ $V_2 = 30\text{V}$

Determine Y-parameters. (8)

b. The network of the Fig.14 contains a current controlled current source. For the network find the z-parameters. (8)



Q.7 a. In the network of Fig.15, K is changed from position a to b at $t = 0$. Solve for i , $\frac{di}{dt}$, and $\frac{d^2i}{dt^2}$ at $t = 0 +$ if $R = 1000\Omega$, $L=1H$, $C=0.1 \mu F$, and $V = 100 V$. (8)

b. Given $z(s) = \frac{s^2 + Xs}{s^2 + 5s + 4}$ what are the restrictions on 'X'. For $z(s)$ to be a positive real function and find 'X' for $\text{Re}[z(j\omega)]$ to have second order zero at $\omega = 0$. (8)

Q.8 a. List out the properties of LC immittance function and then realize the network having the driving point impedance function $z(s) = \frac{2s^5 + 12s^3 + 16s}{s^4 + 4s^2 + 3}$ by continued fraction method. (8)

b. For the network function $Y(s) = \frac{2(s+1)(s+3)}{(s+2)(s+4)}$ synthesize in one Foster and one Cauer form. (8)

Q.9 a. The voltage ratio transfer function of a constant-resistance bridged-T network is given by $\frac{v_2}{v_1} = \frac{s^2 + 1}{s^2 + 2s + 1}$ synthesize the network that terminated in a 1Ω resistor. (8)

b. Find the poles of system functions for low-pass filter with $n = 3$ and $n = 4$ Butterworth characteristics. (Do not use the tables) (8)

