

## Fifth Semester Examination – 2008

## DIGITAL SIGNAL PROCESSING

Full Marks – 70

Time – 3 Hours

Answer Question No. 1 which is compulsory  
and any five from the rest.

The figures in the right-hand margin  
indicate marks.

1. A signal is represented as : 2 x 10

$$x(n) = \begin{cases} 1 + \frac{n}{2}, & -2 \leq n \leq -1 \\ 1, & 0 \leq n \leq 2 \\ 0, & \text{elsewhere} \end{cases}$$

- (a) Determine its values and sketch the signal  $x(n)$ .

- (b) Sketch the signal that results if  $x(n)$  is first folded and then delayed by three samples.

- (c) Express  $x(n)$  in terms of  $\delta(n)$ .

- (d) Sketch  $x(-n+4)$ .

- (e) Give the direct form I realization of the equation defined as

$$y(n] = -a_1 y[n-1] + b_0 x(n) + b_1 x[n-1]$$

- (f) State and prove the convolution property of the z-transform.

- (g) What is the approximate transition width of main lobe in the rectangular window? What happens to it if you double the filter length?

(h) State and prove the circular time shift property of DFT.

(i) What is a periodogram? What is its utility?

(j) How many real multiplications and real additions are required for the computation of an  $N$ -point DFT?

2. Find out the autocorrelation of the signal  $x(n) = a^n u(n)$ ,  $0 < a < 1$ . Plot the resulting signal. When does the autocorrelated signal become the highest? Why? 6+2+1+1

3 (a) Compute the convolution  $y(n)$  of two signals defined as  $x_1(n) = \{2, -3, 2\}$  and

$$x_2(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{elsewhere} \end{cases} \text{ Plot } y(n) \quad 6$$

(b) Determine the step response of the system  $y(n) = ay(n-1) + x(n)$ ,  $-1 < a < 1$  with the initial condition  $y(-1) = 1$ . 4

4. (a) Find out the impulse response of the system

$$y(n) = 0.7y(n-1) - 0.12y(n-2) + x(n-1) + x(n-2). \text{ Locate its poles and zeros. Is the system stable?} \quad 6$$

(b) Compute the DFT of two sequences given as  $x_1(n) = \left\{ \underset{\uparrow}{1}, 2, 3, 2 \right\}$  and  $x_2(n) = \left\{ \underset{\uparrow}{2}, 3, 4, 5 \right\}$ . Plot it. 4

2. (a) Determine the impulse response for the given system described by difference equation. 6

$$y(n] - 4y[n-1] + 4y[n-2] = x[n] - x[n-1]$$

- (b) Compute and sketch the step response of the system. 4

$$y[n] = \frac{1}{M} \sum_{k=0}^{N-1} x[n-k]$$

3. (a) Determine convolution of the following pairs of signal by means of ZT. 6

$$x_1[n] = 0.5^n u[n], \quad x_2[n] = \cos \pi n u[n]$$

- (b) Consider the Fir filter represented as  $y[n] = x[n] + x[n-4]$ . Compute and sketch the magnitude and phase spectrum. 4

4. (a) Let  $x[n]$  be a real valued  $N$  point sequence. Develop a method to compute a  $N$  point DFT  $X'(k)$ , which contains only the odd harmonics by using a real  $N/2$  point DFT. 5

- (b) Perform linear convolution of the following sequence by overlap add method. 5

$$x[n] = [1, -1, 2, -2, 3, -3, 4, -4]$$

$$h[n] = [-1, 1]$$

(b) Determine the magnitude response of the filter. 5

8. Describe the nonparametric method of power spectrum estimate. 10