16E (A)

# MATHEMATICS, Paper-II

(English Version)
Parts A and B

Time: 21/2 Hours

Maximum Marks: 50

# Instructions:

1. Answer the questions under Part 'A' on a separate answer book.

2. Write the answers to the questions under **Part** 'B' on the question paper itself and attach it to the answer book of **Part** 'A'.

### Part A

Time: 2 Hours

Marks: 35

#### SECTION I

 $5 \times 2 = 10$ 

**Note:** 1. Answer any five questions, choosing at least **two** from each of the following groups, i.e. **A** and **B**.

2. Each question carries two marks.

# Group - A

### (Geometry, Analytical Geometry and Statistics)

- 1. Prove that the lengths of the two tangents drawn from an external point to a circle are equal.
- 2. Find the coordinates of the point which divides the join of (2, -4) and (5, 6) in the ratio 5:3 externally.
- 3. Find the equation of the straight line passing through (4, 3) and having a slope 3.
- 4. The mean of a data is 9. If each observation is multiplied by 3 and then 1 is added to each result, find the mean of the new observations so obtained.

# Group - B

# (Trigonometry, Matrices and Computing)

5. Prove that 
$$\sqrt{\frac{1 + Cos\theta}{1 - Cos\theta}} = Cosec\theta + Cot \theta$$
.

- **6.** If  $A \times \begin{bmatrix} 1 & 1 \\ 0 & 2 \end{bmatrix} = \begin{pmatrix} 1 & 2 \end{pmatrix}$ , find the order of matrix A and determine matrix A.
- 7. Define an Algorithm.
- 8. What are the different boxes used in a flowchart?

# SECTION II

 $4 \times 1 = 4$ 

Note: 1. Answer any four of the following six questions.

- 2. Each question carries one mark.
- 9. State the converse of the Pythagoras theorem.
- 10. Find the slope and y-intercept for the line  $\frac{x}{a} + \frac{y}{b} = 1$ ;  $a, b \neq 0$ .
- 11. Define a Radian.
- 12. Write two demerits of an Arithmetic mean.

13. Given that 
$$A = \begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix}$$
 and  $B = \begin{bmatrix} 1 & 2 \\ -3 & 0 \end{bmatrix}$ , find  $(A + B)(A - B)$ .

14. What is meant by stepwise refinement?

**Note**: 1. Answer **any four** questions, choosing at least **two** from each of the following groups, i.e. Group **A** and **B**.

2. Each question carries four marks.

### Group - A

### (Geometry, Analytical Geometry and Statistics)

- 15. State and prove the Basic Proportionality theorem.
- 16. Find the equation of the line which passes through the point (1, -6) and whose product of the intercepts on the coordinate axes is one.
- 17. If the area of the triangle formed with the vertices (t, 2t), (-2, 6), (3, 1) is 5 square units, find 't'.
- 18. Find the mean of the following frequency distribution by the shortcut method.

Class interval	0-19	20-39	40-59	60-79	80-99	100-119
Frequency	9	16	24	15	4	2

### Group - B

# (Trigonometry, Matrices and Computing)

19. Solve 
$$\frac{\cos^2\theta - 3\cos\theta + 2}{\sin^2\theta} = 1$$

**20.** If 
$$A = \begin{pmatrix} -2 & 1 \\ 3 & -1 \end{pmatrix}$$
;  $B = \begin{pmatrix} 2 & 0 \\ 5 & -3 \end{pmatrix}$ , show that  $(AB)^{-1} = B^{-1}$ .  $A^{-1}$ 

21. Solve the following equations using Cramer's method.

$$4x - y = 16$$
,  $\frac{3x - 7}{2} = y$ .

22. Execute the flowchart to obtain the total amount to be paid at the end of 6 years if P = Rs. 1,000 and R = 12%.

- Note: 1. Answer any one of the following questions.
  - 2. The question carries five marks.
- 23. Construct a triangle similar to a given  $\triangle ABC$  such that each of its side is  $\frac{2}{3}$  of the corresponding sides of  $\triangle ABC$ . Given that AB=4.5 cm, BC=6 cm and AC=6.5 cm.
- 24. From the ground and first floor of a building, the angle of elevation of the top of the spire of a church was found to be 60° and 45° respectively. The first floor is 5 mts high. Find the height of the spire.

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