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| Number | 144 | | | |

MATHEMATICS — Paper II

Time Allowed : $2\frac{1}{2}$ Hours]

[Maximum Marks: 100

Note: i) The question paper consists of six Sections A, B, C, D, E and F.

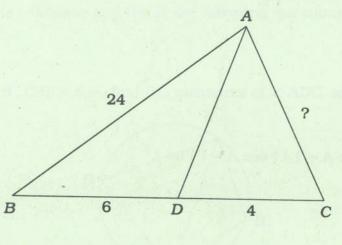
- ii) Read the instructions under each Section before you start answering.
- iii) Diagrams should be drawn, wherever necessary.
- iv) Rough work and calculations should be shown legibly at the bottom of the pages in the answer-book.

SECTION - A

Note: Answer all the ten questions.

 $10 \times 1 = 10$

1. In the given figure, AD bisects \angle BAC. If AB = 24, BD = 6, DC = 4, then AC is equal to



1) 16

2) ,22

3) 36.

- 2. Two chords PQ and RS intersect internally at M such that PM = 9, MQ = 2 and RM = 3. Then MS is equal to
 - 1) 9
 - 2) 6
 - 3) 8.
- 3. AB and CD are two perpendicular lines. The slope of AB is $\frac{2}{3}$. Then the slope of
 - 1) $-\frac{3}{2}$
 - 2) $\frac{2}{3}$
 - 3) $\frac{3}{2}$.
- 4. The centroid of the triangle whose vertices are (-3, 4), (6, 2) and (3, 6) is
 - 1) (4,2)
 - 2) (2,4)
 - 3) (4,4).
- 5. If $\sin x = \cos 2x$, then x is
 - 1) 30°
 - 2) 45°
 - 3) 60°.
- 6. The value of $(\sec A + 1)(\sec A 1)$ is
 - 1) cot 2 A
 - 2) tan 2 A
 - 3) $\cos^2 A$.

The order of

1) 2 × 3

- 2) (3, 2)
- 0 × 0. 3)

The range of 8, 12, 16, 36, 40, 32, 20 is 8.

1) 8

2) 32 3) 40.

The probability of drawing a white ball from a box containing 6 white and 4 red balls is

1)

2) $\frac{3}{5}$

3) $\frac{5}{3}$.

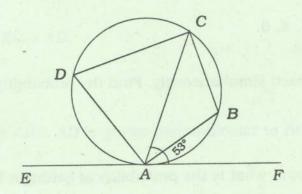
10. Which one of the following is a valid expression?

- $\frac{PNR}{100}$ 1)
- 7-2+-5 2)
- 3) A** 5.

SECTION - B

Note: Answer any ten of the following questions. $10 \times 3 = 30$

11. In the figure, if $CAF = 53^{\circ}$, find the measures of $\angle ADC$ and $\angle ABC$.



- 12. A ladder 25 m long rests on a wall of a house 20 m above the ground. Determine the distance of the foot of the ladder from the house.
- 13. ABC is an equilateral triangle and D is the mid-point of BC. If AB = 10 cm, find the length of AD.
- 14. Show that $\sin \theta$ sec $(90^{\circ} \theta) \cot \theta$ cot $(90^{\circ} \theta) = 0$.
- 15. Prove that $\cos^4 \theta + \sin^4 \theta = 1 2 \sin^2 \theta \cdot \cos^2 \theta$.
- 16. The angle of elevation of the top of a tower from a point on the ground 50 m away from the foot of the tower is 60°. Find the height of the tower.
- 17. Show that the points (-4, -2), (1, 1) and (6, 4) are collinear.
- 18. Find the slope, X-intercept and Y-intercept of the line 3x 2y 12 = 0.
- 19. The slope of the line joining (1, 4) and (-5, a) is $-\frac{1}{2}$. Find the value of a.
- 20. Given $\begin{pmatrix} x+y & x-y \\ 7 & 6 \end{pmatrix} = \begin{pmatrix} 10 & 2 \\ 7 & z \end{pmatrix}$ find the values of x, y and z.
- 21. If $A = \begin{pmatrix} 2 & 4 & 6 \\ 1 & 3 & 5 \end{pmatrix}$ and $B = \begin{pmatrix} 5 & 3 & 2 \\ -1 & -2 & -3 \end{pmatrix}$, find 3A + 2B.
- 22. Find the S.D. of 2, 4, 6.
- 23. Three coins are tossed simultaneously. Find the probability of getting exactly two heads.
- 24. If two dice are thrown, what is the probability of getting a sum of 9?

25. Write the output for the following program:

10 READ E, F, G

20 LET $A = E \wedge F + (G * E)$

30 PRINT A

40 DATA 2, 3, 4

50 END.

SECTION - C

Note: Answer all the questions, choosing either (a) o

26. a) Prove that the straight line drawn parallel to one other two sides proportionally.

OR

- b) State and prove S.A.S. similarity theorem.
- 27. a) If the sides of a quadrilateral ABCD touch a circle

28. a) Find the equation of the line through (-1, 3) and parallel to the line joining (5, -2) and (-3, 1).

OR

- b) Find the equation of the median through A of triangle ABC whose vertices are respectively (-3, 2), (5, -4) and (-1, 2).
- 29. a) Find the ratio in which the line joining the points (-4, -4) and (6, 6) is divided by the point (3, 3).

OR

b) Find the fourth vertex of a parallelogram, three of whose vertices taken in order are (4, 12), (6, -2) and (5, -10).

SECTION - D

Note: Answer all questions, choosing either (a) or (b) in each question.

 $4 \times 5 = 20$

30. a) Prove that $\frac{1}{1 + \cos \theta} + \frac{1}{1 - \cos \theta} = 2 \csc^2 \theta$.

OR

b) Two persons standing on opposite sides of a tower view the top of the tower at angles of elevation 45° and 30°. If the height of the tower is 50 m, find the distance between them.

31. a) If
$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$$
, prove that $A^2 - 5A - 2I = 0$.

b) Find X and Y if
$$3Y = \begin{pmatrix} -3 & 0 \\ 9 & 3 \\ 3 & -3 \end{pmatrix}$$
 and $3X - 2Y = \begin{pmatrix} 2 & -6 \\ 9 & -2 \\ -5 & 5 \end{pmatrix}$.

32. a) Find the Standard Deviation of the following data:

| x: | 4 | 6 | 8 | 10 | 12 |
|----|---|---|---|----|----|
| f: | 3 | 4 | 8 | 3 | 2 |

OR

- b) A two digit number is formed with the digits 2, 4, 5, 7. What is the probability that the number is divisible by 2 and by 5 (without repetition of number)?
- 33. a) Draw a flowchart to find the volume of a sphere given the radius.

OR

b) Write a BASIC program to find the area of a circle.

SECTION - E

Note: Answer the question, choosing one of the alternatives (a) or (b).

Construct triangle ABC, given BC = 6.4 cm, vertical angle A is 46° and the altitude from A to BC is of length 6 cm.

OR

b) Find the mean proportional to two given segments 7 cm and 5 cm.

SECTION - F

Note: Answer the question, choosing one of the alternatives (a) or (b). 10

35. a) Calculate median, using 'greater than Ogive' for the following frequency distribution:

| 1 | C.I: | 0-10 | 10 - 20 | 20 - 30 | 30 - 40 | 40 - 50 | 50 - 60 | 60 - 70 |
|---|------|------|---------|---------|---------|---------|---------|---------|
| Ī | f: | 7 | 12 | 15 | 20 | 12 | 10 | 4 |

OR

b) Using 'less than Ogive', calculate median for the following data:

| - | C.I: | 20 - 40 | 40 - 60 | 60 - 80 | 80 - 100 | 100 - 120 | 120 - 140 |
|---|------|---------|---------|---------|----------|-----------|-----------|
| | f: | 4 | 6 | 8 | 15 | 10 | 7 |