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Con. 5613-09.

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(3 Hours)

[Total Marks: 100

N.B.:(1) Question No. 1 is compulsory.

- (2) Attempt any four questions from remaining six questions.
- (3) Assume suitable data if needed.

1. Attempt any four of the following :-

(a) A scalar non linear system is described by the differential equation-

$$x(t) = f(x(t)), x \in \mathbb{R}$$

where non linear function satisfies:

$$f(0) = 0$$

$$f(x) > 0$$
; $x < 0$.

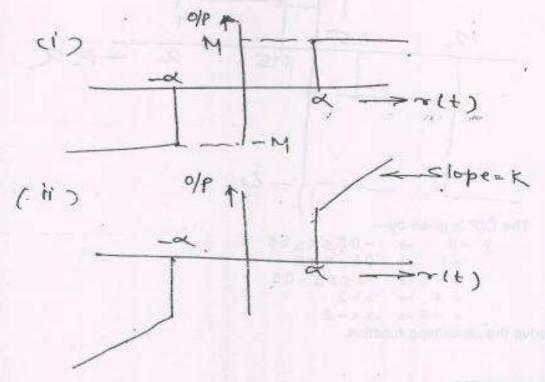
Show that x = 0 is globally asymptotically stable equilibrium point.

(b) Consider scalar differential equation-

$$\dot{x}(t) = 1 + x^2(t) ; x(0) = 0$$

Show that $x(t) = \tan(t)$ is a solution what happens as $t \to \pi/2$.

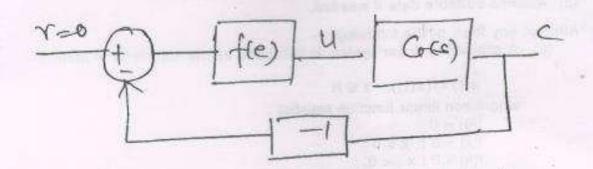
- (c) Explain jump response for soft spring with characteristics.
- (d) On what factors Robustness of the system depends.
- (e) Discuss gradient update law.
- (f) For sinusoidal input and given non-linearity draw the possible output.



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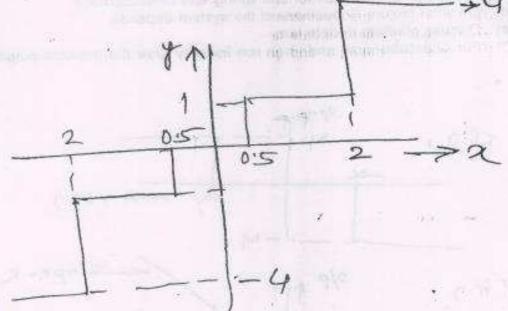
(a) Consider the feedback Icop in figure the linear system G(s) = 1/(s+1)⁴ is 10 connected to a static nonlinearity u(t) = f(e(t)) where f(0) has describing function.
 N(X jw) = X + 3X² ∠o^e



What is the amplitude and frequency of the limit cycle? Comment on stability of limit cycle.

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(b) Consider the logarithmic quantizer with two levels.



The O/P is given by-

$$y = 0 \rightarrow -0.5 \le x \le 0.5$$

$$= 1 \rightarrow 0.5 \le x \le 2$$

$$= -1 \rightarrow -2 \le x \le -0.5$$

$$= 4 \rightarrow x > 2$$

$$= -4 \rightarrow x < -2$$

Derive the describing function.

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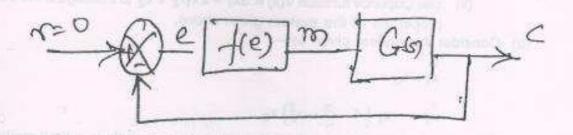
3. (a) Consider the nonlinear system described by the equations-

$$\hat{x}_1 = -3x_1 + x_2$$

$$\hat{x}_2 = x_1 - x_2 - x_2^3$$

Using Krasovskii's Method construct a Liapunov's function for the given system.

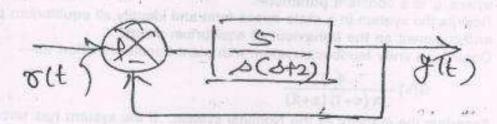
(b) For the control system shown in figure, use variable gradient method to 10 investigate stability of the system.



$$f(e) = e^3$$

$$G(s) = \frac{1}{s(s+1)}.$$

4. (a) For the block diagram shown in figure, use method of isocline to draw the 10 phase trajectory.



r(t) = 24(t) and initial conditions y(0) = -1; y(0) = 0

(b) For a system given by the differential equation-

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$$x + 3x + x = 0$$

Use delta method to plot the phase trajectory using initial conditions as (1, 0).

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(a) Consider the system:

$$x_1 = -x_1$$

$$x_2 = -2x_1 - x_2$$

- (i) Is the system asymptotically stable ?
- (ii) Use Liapunov function $V(x) = 3x_1^2 2x_1x_2 + x_2^2$ to investigate the stability properties of the system given above.

(b) Consider the system given by-

$$x_1 = x_2$$

$$\dot{x}_2 = -x_1 \left(1 - x_1^2 - x_2^2\right) x_2$$

Find the only equilibrium points show that the unit circle is a limit cycle for the system.

- 6. (a) Discuss different Adaptive control schemes.
 - (b) Explain methods for improving Robustness of the system.
- 7. (a) Consider the second order system-

 $x + 2x - x + x^3 = 0$

where 'a' is a constant parameter.

Rewrite the system in a state space form and identify all equilibrium points and comment on the behaviour of equilibrium points.

(b) Consider a unity feedback system with plant transfer function as-

$$G(s) = \frac{4 \cdot 5}{s(s+1)(s+2)}$$

Ascertain the stability of the Nominal system. If the system has uncertain coefficients.

$$4 \le a_0 \le 5$$

$$1 \le a_1 \le 3$$
 (0) y enclibrate trilling time (1) $4 = 10$

$$2 \le a_2 \le 4$$
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