

Code: AE11

Subject: CONTROL ENGINEERING

Time: 3 Hours

**DECEMBER 2008**

Max. Marks: 100

**NOTE: There are 9 Questions in all.**

- Question 1 is compulsory and carries 20 marks. Answer to Q. 1. must be written in the space provided for it in the answer book supplied and nowhere else.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

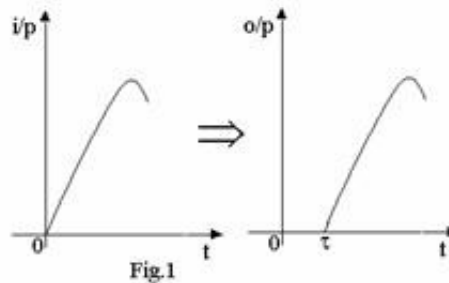
**Q.1 Choose the correct or best alternative in the following: (2x10)**

a. If force-current and velocity-voltage are analogous pairs, then mass is paired with

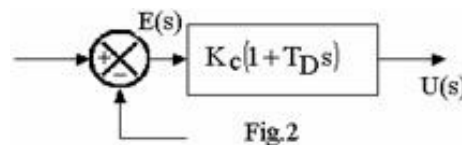
- (A) Capacitance                      (B) Inductance  
(C) Resistance                      (D) Conductance

b. The system with input-output

- (A) linear elements  
(B) active elements  
(C) dead-time elements  
(D) ideal elements

c. The controller of gain  $K_c$  and rate-time  $T_D$  as in Fig.2 refers to

- (A) PID  
(B) PD  
(C) PI  
(D) Integral controller

d. If for all possible initial states  $x(0), x(t)$  eventually decays to zero as  $t \rightarrow \infty$ , then the system is

- (A) stable                              (B) unstable  
(C) marginally stable              (D) asymptotically stable

e. The radii of constant-M circles reduce monotonically and the centres located on the negative real axis shift towards  $(-1 + j0)$  point when

- (A)  $M = 1$                               (B)  $M > 1$   
(C)  $M < 1$                               (D)  $M = 0$

f. Control applications using synchros require good sensitivity which has the units

- (A) V                                      (B) rpm

- (C)  $V/\text{rad} - s^{-1}$                       (D)  $V/\text{deg}$

g. Consider a function  $F(s) = \frac{1}{s(s+1)}$  where  $L[f(t)] = F(s)$  then  $\lim_{t \rightarrow \infty} f(t)$  equal to

- (A) zero                                      (B) one  
(C) infinite                                  (D) none of the above

h. Large power applications like earth station antenna drives for tracking satellites generally use

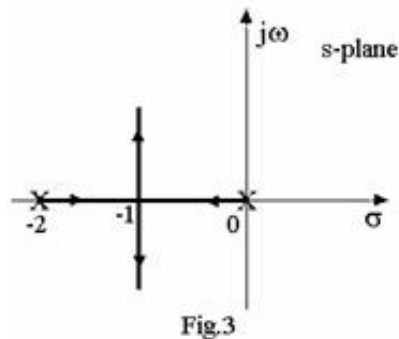
- (A) ac servo motors                      (B) dc servo motors  
(C) small motors                          (D) single-phase motors

i. For a standard second-order system described by  $s^2 + 2\zeta\omega_n s + \omega_n^2$ , the term  $1/\zeta\omega_n$  indicates

- (A) time-constant                          (B) damping factor  
(C) natural frequency                      (D) none of the above

j. The root-locus drawn in Fig.3 refers to an open-loop transfer function  $G(s) =$

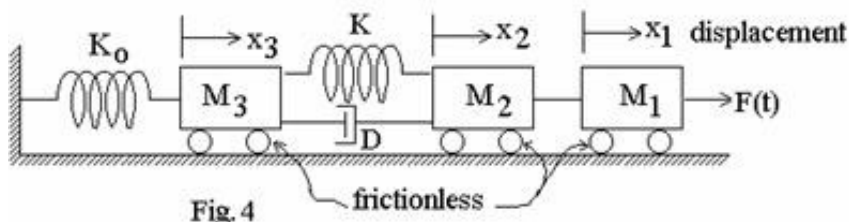
- (A)  $\frac{K}{s+1}$   
(B)  $\frac{K}{(s+1)(s+2)}$   
(C)  $\frac{K}{s(s+1)(s+2)}$   
(D)  $\frac{K}{s(s+2)}$



**Answer any FIVE Questions out of EIGHT Questions.**

**Each question carries 16 marks.**

**Q.2** a. For the mechanical system of Fig.4, draw the free body diagram and write the associated equations of motion. Draw the electrical equivalent circuit using  $F(t) \rightarrow$  voltage and  $\frac{dx}{dt} \rightarrow$  current analogy. (8)



b. Write the transfer function network of Fig.5 and derive network.

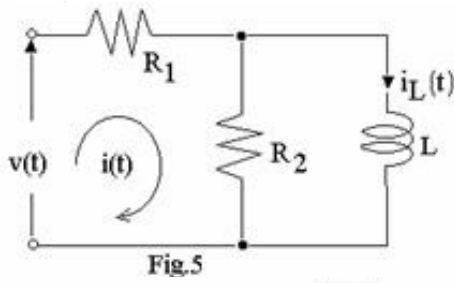


Fig.5

Q.3 a. Reduce the block-diag to find  $\frac{C(s)}{R(s)}$

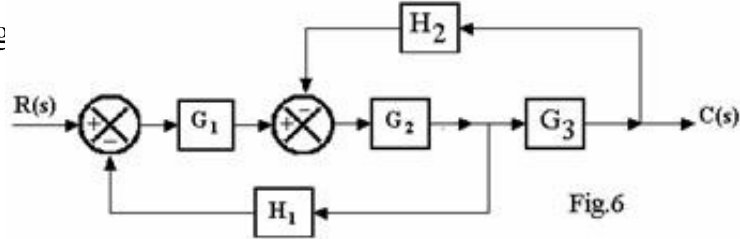


Fig.6

b. Use Mason's gain rule to obtain the overall transfer function of the signal-flow graph of the block-diagram of Fig.7. (8)

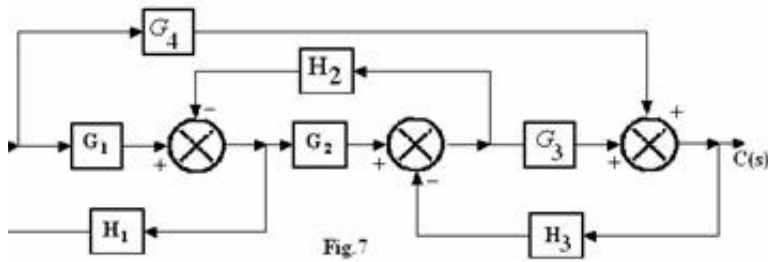


Fig.7

Q.4 a. Apply Routh-Hurwitz criterion to find the greatest value of K that can keep the system of Fig.8 stable. Also state Routh-Hurwitz criterion for stability of a feedback control system. (10)

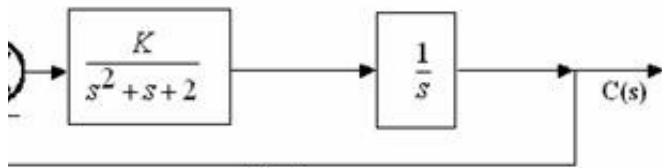


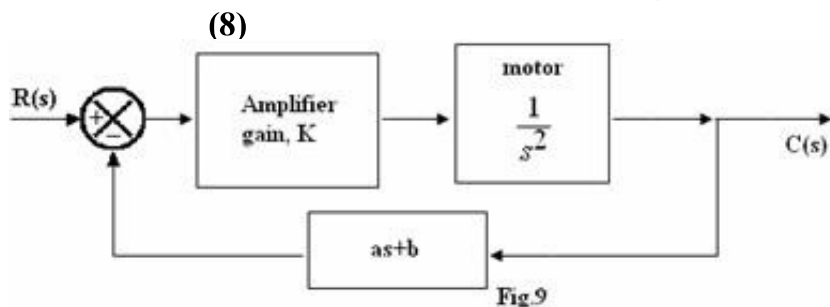
Fig.8

b. Discuss the various time domain performance specification of a typical second-order system with unit input excitation. (6)

Q.5 a. Sketch the root-locus on a graph sheet for a control system with  $G(s)H(s) = \frac{K(s+4)(s+6)}{s(s+2)}$ ,  $H(s) = 1$ . Mark the points of intersection with the real-

axis. (8)

- b. The block diagram of a servo system shown in Fig.9 has  $K = 10$ . Determine the values of  $a$  and  $b$ , if the time-constant is  $0.1s$  and damping ratio  $\zeta = 0.5$ .

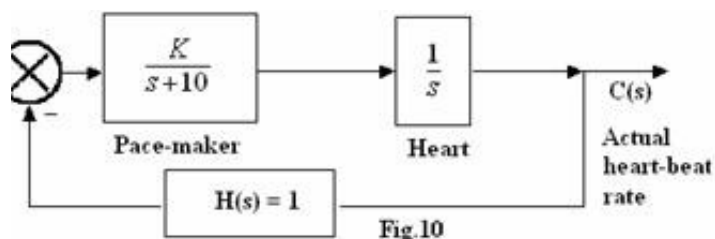


- Q.6 a. For the open-loop transfer-function  $G(s)H(s) = \frac{5}{s(s-1)}$ , draw the Nyquist plot. Verify whether the system is stable. (10)

- b. For the unity-feedback system  $G(s)H(s) = \frac{8(s+1)(s+3)}{s(s+2)(s+4)}$  find the type of the system, the error constants  $K_p, K_v, K_a$  and the corresponding steady-state errors. (6)

- Q.7 a. Draw Bode plots on a semilog graph sheet for  $G(s)H(s) = \frac{K}{s(1+0.025s)(1+0.04s)}$ ,  $H(s) = 1$ . Find the value of  $K$  if the phase-margin is to be  $45^\circ$ . What is the corresponding gain-margin? (10)

- b. An electronic pace-maker controlling the rate of heartbeat is shown in Fig.10



Determine the value of  $K$  to limit the steady-state error to  $0.02$  for a ramp input. (6)

- Q.8 a. Discuss tuning of PID controller. (6)
- b. Represent the following data on a graph sheet to show a frequency-response plot in Nichols coordinate system. Determine the phase-margin and the gain-margin. Also define the term phase-margin and gain-margin. (10)

Frequency, $\omega$ , rad/s	0.2	0.5	0.78	1.25	2.2	3.0
Gain, dB	15	5	0	-7	-15	-21

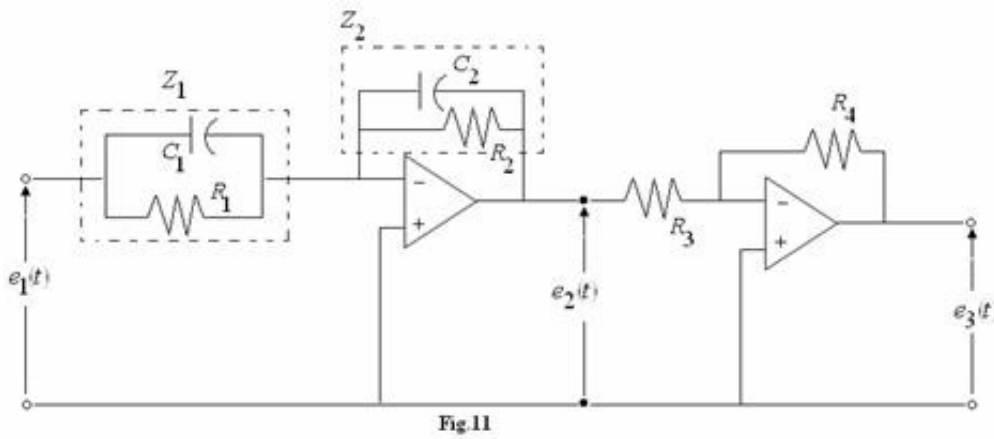
Phase, deg.	-110	-120	-140	-160	-180	-190
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**Q.9** a. Consider the opamp circuit used as a compensator. (Fig.11) Show that

(i)  $R_1 C_1 > R_2 C_2$  makes it a lead compensator.

(ii)  $R_1 C_1 < R_2 C_2$  makes it a lag compensator.

**(10)**



b. Explain phase-lead compensation.

**(6)**