

Seat No.: \_\_\_\_\_

Enrolment No. \_\_\_\_\_

## GUJARAT TECHNOLOGICAL UNIVERSITY

B.E. Sem-I Examination January 2010

Subject code: 110010

Date: 12 / 01 / 2010

Subject Name: Mechanics of solids

Time: 11.00 am – 1.30 pm

Total Marks: 70

### Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

**Q.1 (a)** Select appropriate answer from given options and rewrite the complete sentence. **07**

- (i) Moment is a \_\_\_\_\_ vector, whereas Couple is a \_\_\_\_\_ vector.  
(free, null, fixed)
- (ii) A truss is called perfect if  $m + r$  \_\_\_\_\_  $2j$ . ( $<$ ,  $=$ ,  $>$ )
- (iii) The ratio of direct stress to volumetric strain is called \_\_\_\_\_  
(Modulus of Elasticity, Modulus of rigidity, Bulk Modulus)
- (iv) At the point of contraflexure \_\_\_\_\_ changes its sign.  
(shear force, bending moment, axial force)
- (v) Impact test measures \_\_\_\_\_ of material.  
(Toughness, Hardness, Brittleness)
- (vi) Maximum possible value of Poisson's ratio is \_\_\_\_\_. (0.5, 0.75, 1.0)

(vii) Shear stress on principal plane is \_\_\_\_\_ (maximum, zero, minimum)

**(b)** A single purchase crab winch has number of teeth on pinion and spur wheel as 25 and 100 respectively. The diameter of effort wheel and load drum is 25 cm and 6.25 cm respectively. The load of 240N can be raised by 20 N. Determine (i) Velocity ratio (ii) Mechanical Advantage (iii) Efficiency (iv) Ideal effort (v) Frictional effort (vi) Ideal load (vii) Frictional load. **07**

**Q.2 (a)** State laws of Dry friction. **02**

**(b)** Derive formula from first fundamental to determine extension  $\Delta L$  of uniformly tapering circular bar of diameter  $d_1$  at one end,  $d_2$  at other end, length  $L$ , Modulus of Elasticity  $E$  and subjected to axial tensile force  $P$ . **05**

**(c)** **Fig. 1** shows a plane truss, check determinacy and calculate magnitude and nature of each member force and reactions for given loading on the truss. Tabulate all member forces showing their magnitude and nature. **07**

**OR**

**(c)** A uniform ladder  $AB$  weighing 230 N and 4m long, is supported by vertical wall at top end  $B$  and by horizontal floor at bottom end  $A$  as shown in **Fig. 2**. A man weighing 550 N stood at the top of the ladder. Determine minimum angle  $\theta$  of ladder  $AB$  with floor for the stability of ladder. Take coefficient of friction between ladder and wall as  $1/3$  and between ladder and floor as  $1/4$ . **07**

**Q.3 (a)** A system of four forces shown in **Fig. 3**, has resultant 50 kN along  $+X$  – axis. Determine magnitude and inclination of unknown force  $P$ . **04**

**(b)** Determine co ordinates of centroid with respect to 'O' of the section shown in **Fig. 4**. **04**

**(c)** Determine moment of inertia of a section shown in **Fig. 5** about horizontal centroidal axis. **06**

**OR**

- Q.3** (a) A section of a beam shown in **Fig. 6**, has moment of inertia about neutral axis is  $11.6 \times 10^6 \text{ mm}^4$ . The section is subjected to shear force of 14.5 kN. Determine value of maximum shear stress on the section. **04**
- (b) Draw neat qualitative shear stress distribution sketches of following sections, indicating position of maximum shear stress. (i) H – section (ii) Solid circular section (iii) L – section (iv) I - Section **04**
- (c) A concrete member 90 mm wide X 120 mm deep and 3m long, has central axial longitudinal hole of diameter 30 mm throughout the length of member. A steel cable of 10mm diameter is passed through the hole end to end and fitted by nuts supported on rigid plates provided at the ends of beam, such that initially cable is stress free. Now the cable is tightened by turning the nuts, to reduce the length of the cable by 6 mm. Determine stresses in steel and concrete due to reduction in length of cable. Take  $E_s = 210 \text{ GPa}$  and  $E_c = 14 \text{ GPa}$ . **06**
- Q.4** (a) Determine moment of resistance of a section of a beam shown in **Fig.7**, if allowable bending stress is 230 MPa. **07**
- (b) Calculate shear force and bending moment at points A, B, C, D and E. for the beam shown in **Fig. 8**. Also plot neat shear force and bending moment diagrams indicating values at above points. Locate point of contraflexure from support B. **07**

**OR**

- Q.4** (a) Derive condition of reversibility of a simple lifting machine with usual notations. **04**
- (b) A thin cylindrical shell of internal diameter 'd', length 'l' and thickness 't' is subjected to internal pressure 'p'. Derive formula for hoop stress and longitudinal stress. **04**
- (c) Determine magnitude, direction and perpendicular distance from 'O', of the resultant for the force system shown in **Fig. 9**. **06**
- Q.5** (a) A wire is tied straight between two rigid poles 10 m apart has initial tensile stress  $10 \text{ N/mm}^2$  at  $32^\circ \text{ C}$ . Calculate stress in wire if temperature reduces to minus  $8^\circ \text{ C}$ . Take  $E = 75 \times 10^5 \text{ N/mm}^2$  and  $\alpha = 20 \times 10^{-6} / ^\circ\text{C}$ . **03**
- (b) A square steel plate 50 mm x 50 mm and 20 mm thick is subjected to axial tensile force in horizontal and vertical direction 80 kN and 120 kN respectively as shown in **Fig10**. Calculate normal and tangential stresses on plane inclined at  $30^\circ$  to the plane carrying 80 kN force. Also calculate resultant stress and angle of obliquity. **05**
- (c) A rectangular block of size 300mm x 150mm x 100mm is subjected to forces as shown in **Fig. 11**. If  $E = 75 \text{ GPa}$  and poisson's ratio is 0.25, calculate (i) Change in volume (ii) Modulus of rigidity and (iii) Bulk modulus. **06**

**OR**

- Q.5** (a) Discuss briefly limitations of compression test on materials. **03**
- (b) A beam is loaded as shown in **Fig. 12**. Determine support reactions at supports A and B. Also identify type of beam. **05**
- (c) Calculate shear force, bending moment and axial thrust at points A, B, C and D for the beam shown **Fig. 13**. Also plot neat shear force, bending moment and axial thrust diagrams indicating values at above points. **06**

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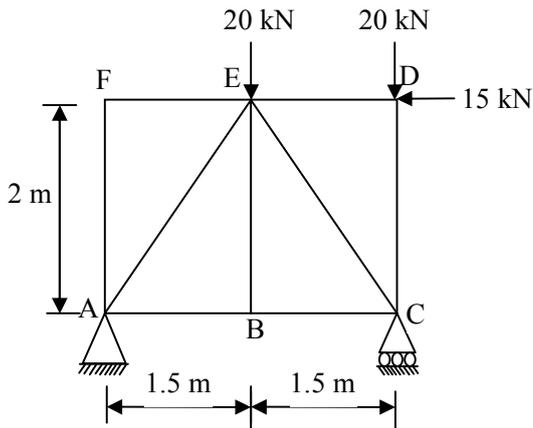


Fig. 1 Que 2(c)

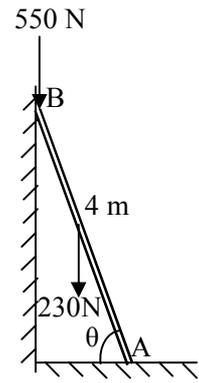


Fig. 2 Que 2(c) OR

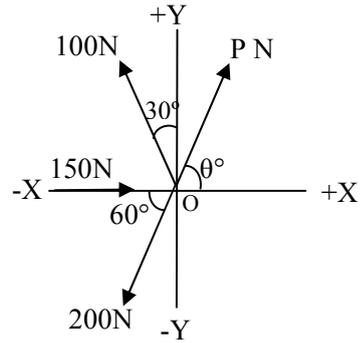


Fig. 3 Que 3(a)

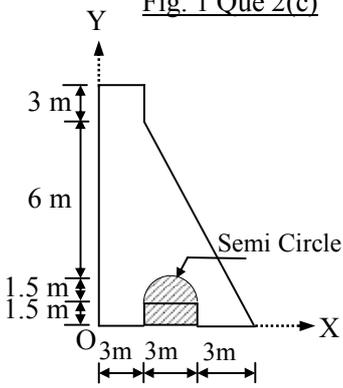


Fig. 4 Que 3(b)

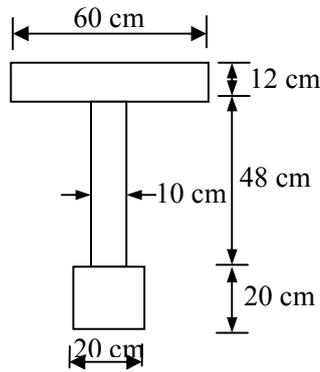


Fig. 5 Que 3(c)

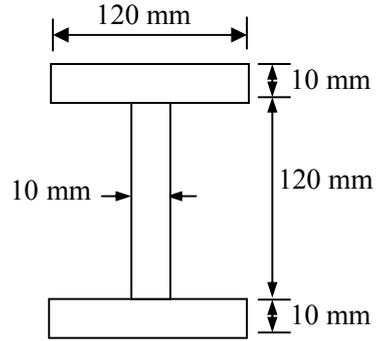


Fig. 6 Que 3(a) OR

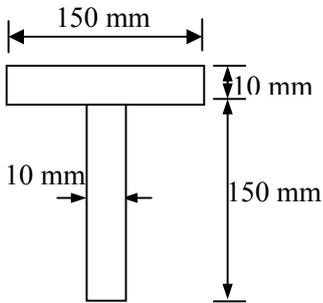


Fig. 7 Que 4(a)

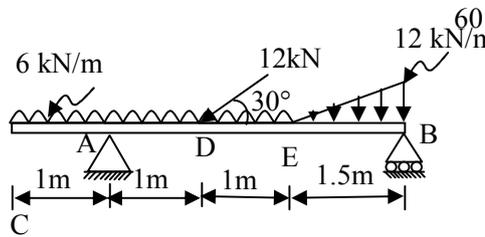


Fig. 8 Que 4(b)

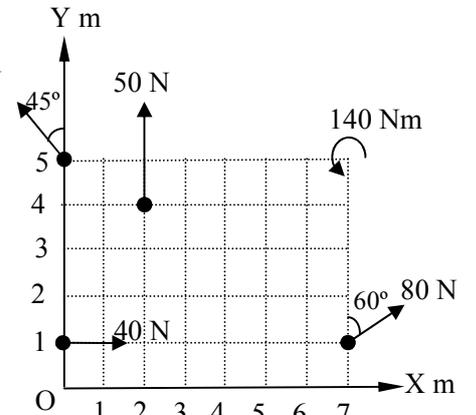


Fig. 9 Que 4(c) OR

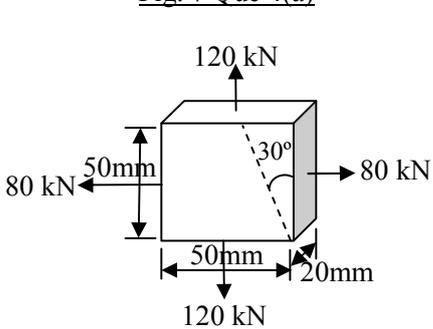


Fig. 10 Que 5(b)

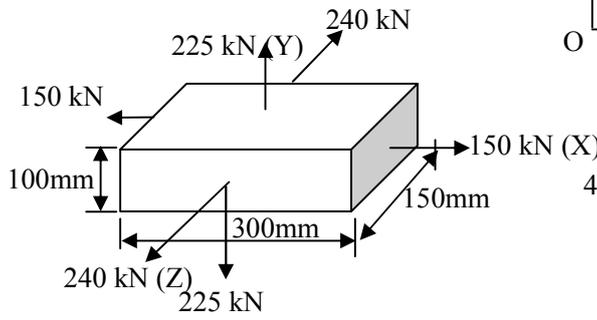


Fig. 11 Que 5(c)

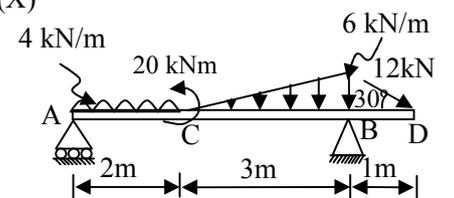


Fig. 12 Que 5(b) OR

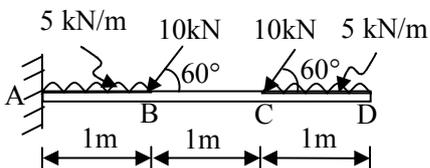


Fig. 13 Que 5(c) OR

All above figures are not to scale.